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A PRACTICAL THREE DIMENSIONAL, 11 STATE EXTENDED KALMAN FILTER --ETC(U)
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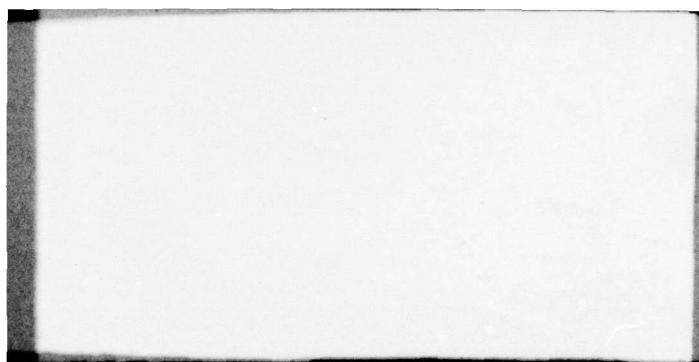
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AFIT/06C/EE/78-7-VOL-2

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(6) A PRACTICAL THREE DIMENSIONAL, 11
STATE EXTENDED KALMAN FILTER FOR
USE IN A FIRE CONTROL SYSTEM
AGAINST NON-THRUSTING MISSILES.

(9) Master's THESIS VOLUME II

(14) AFIT/GGC/EE/78-7

(10) Charles W. Hlavaty
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(11) Dec 78
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A PRACTICAL THREE DIMENSIONAL, 11
STATE EXTENDED KALMAN FILTER FOR
USE IN A FIRE CONTROL SYSTEM
AGAINST NON-THRUSTING MISSILES

THESIS VOLUME II

Presented to the Faculty of the School of Engineering
of the Air Force Institute of Technology
Air Training Command
in Partial Fulfillment of the
Requirements for the Degree of
Master of Science

by

Charles W. Hlavaty, B.S.E.E., M.S.

Capt

USAF

Graduate Electrical Engineering

December 1978

Approved for public release; distribution unlimited.

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Volume II .

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Appendix C

The appendix contains the graphical results of the Monte Carlo analyses of the Double Filter. In each test, the filter states are initialized to the initial true values. The tuning parameters used in the filter are (Note: The state vector is

$$[V_{mx}, \theta_t, R, \dot{R}, A_1, n, \tau_f, m/s]^T :$$

$$R = \begin{bmatrix} 3.E-5 & 0 & 0 \\ 0 & 500 & 0 \\ 0 & 0 & 100 \end{bmatrix}$$

where the measurements are on θ_t , R , and \dot{R} . For angle measurements only,

$$R = 3.E-5$$

$$P_o = \begin{bmatrix} 100 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1.E-8 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 101 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 4 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & .4 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & .009 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 5 \end{bmatrix}$$

$$Q = \begin{bmatrix} 250 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1.E-6 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 500 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 200 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 10 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & .5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 101 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & .009 \end{bmatrix}$$

The results of the trajectories tested are arranged as follows:

<u>Figure</u>	<u>Subject</u>
	Double Filter with four measurements
C-1 to C-18	K Set One
C-19 to C-36	K Set Four, Three Dimensional
C-37 to C-54	K Set Four, Two Dimensional
	Double Filter with two measurements
C-55 to C-72	K Set Four

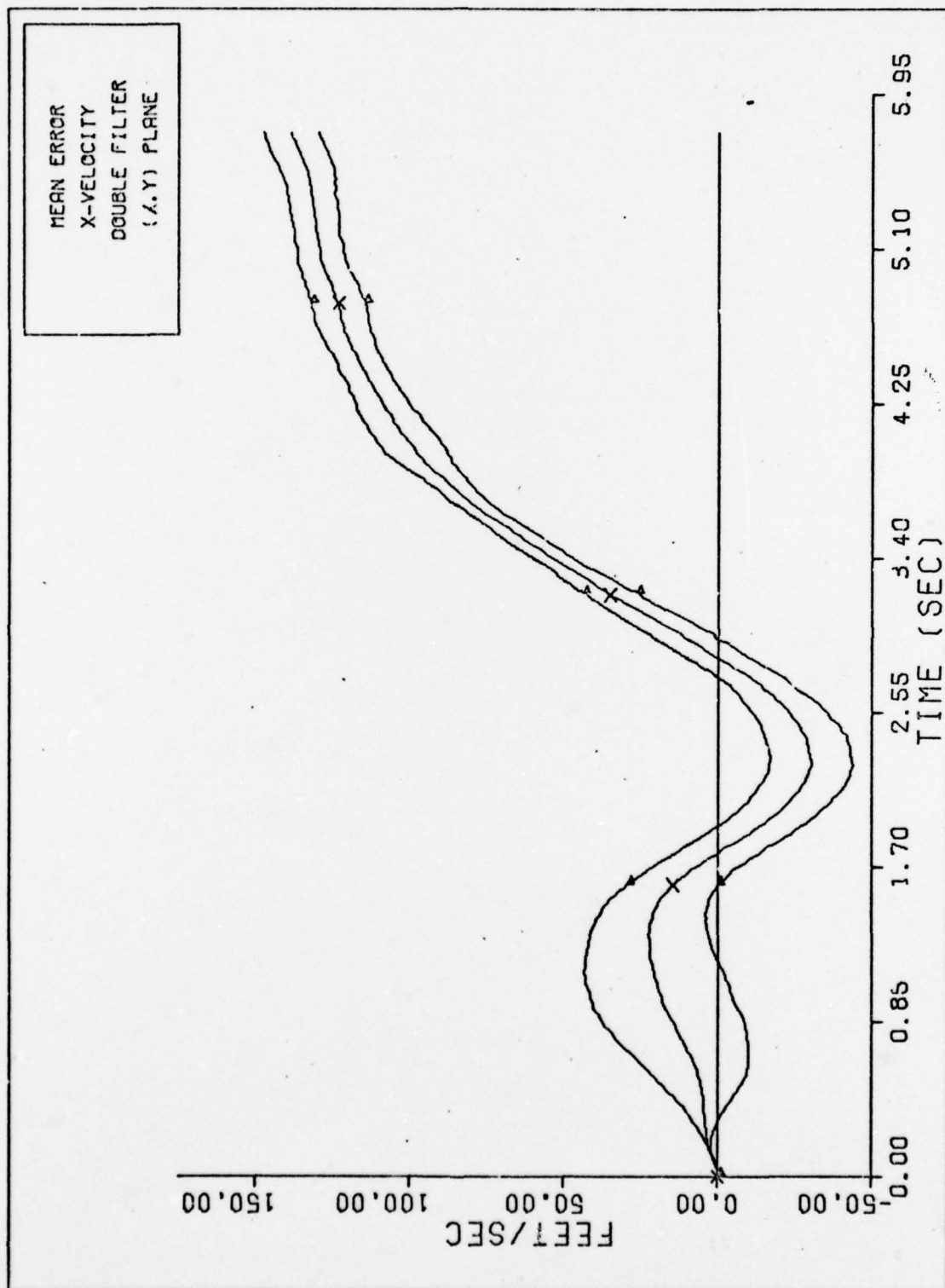


Fig. C-1

X-VELOCITY DOUBLE FILTER

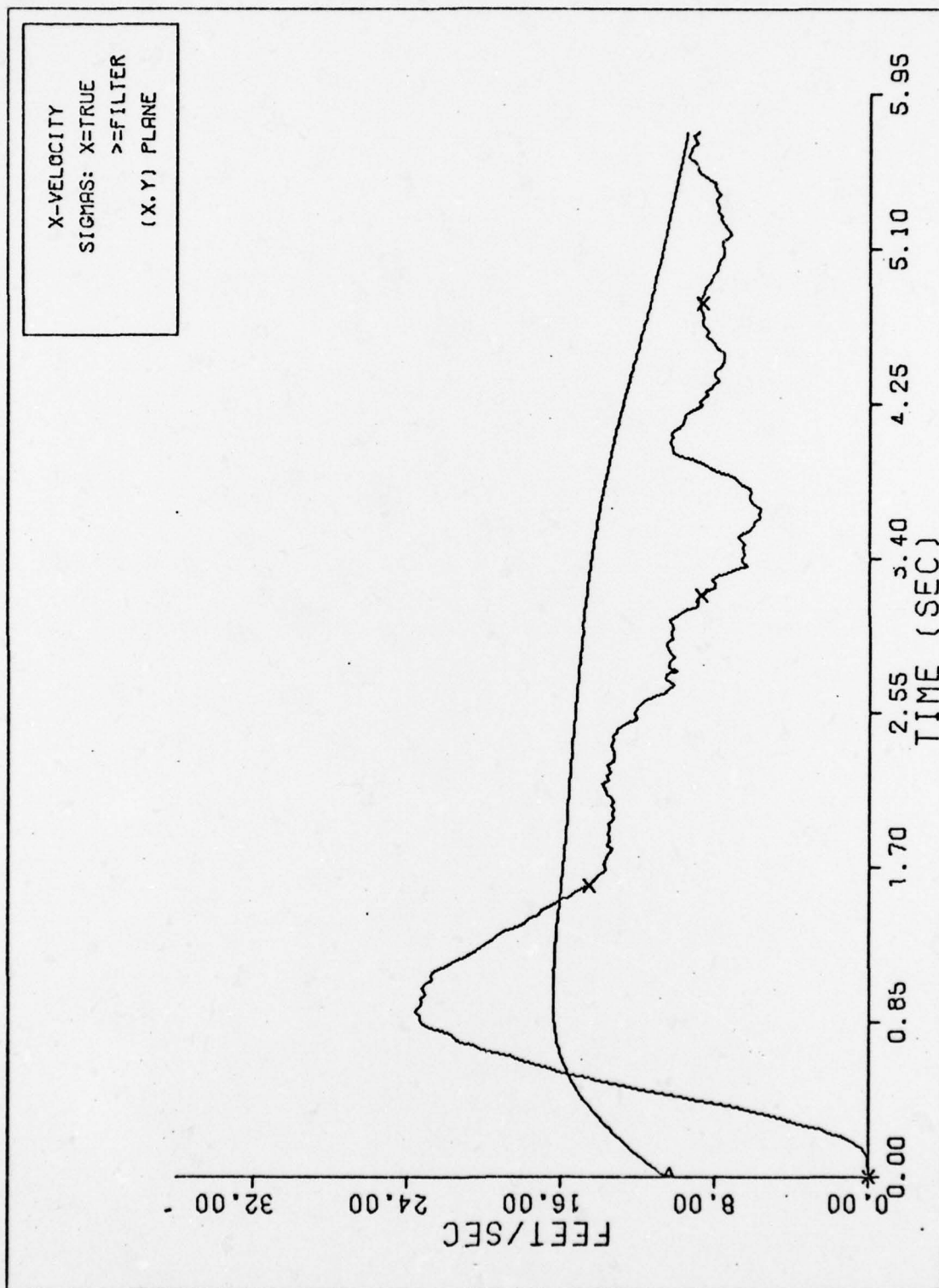


Fig. C-2

X-VELOCITY SIGMAS DOUBLE FILTER

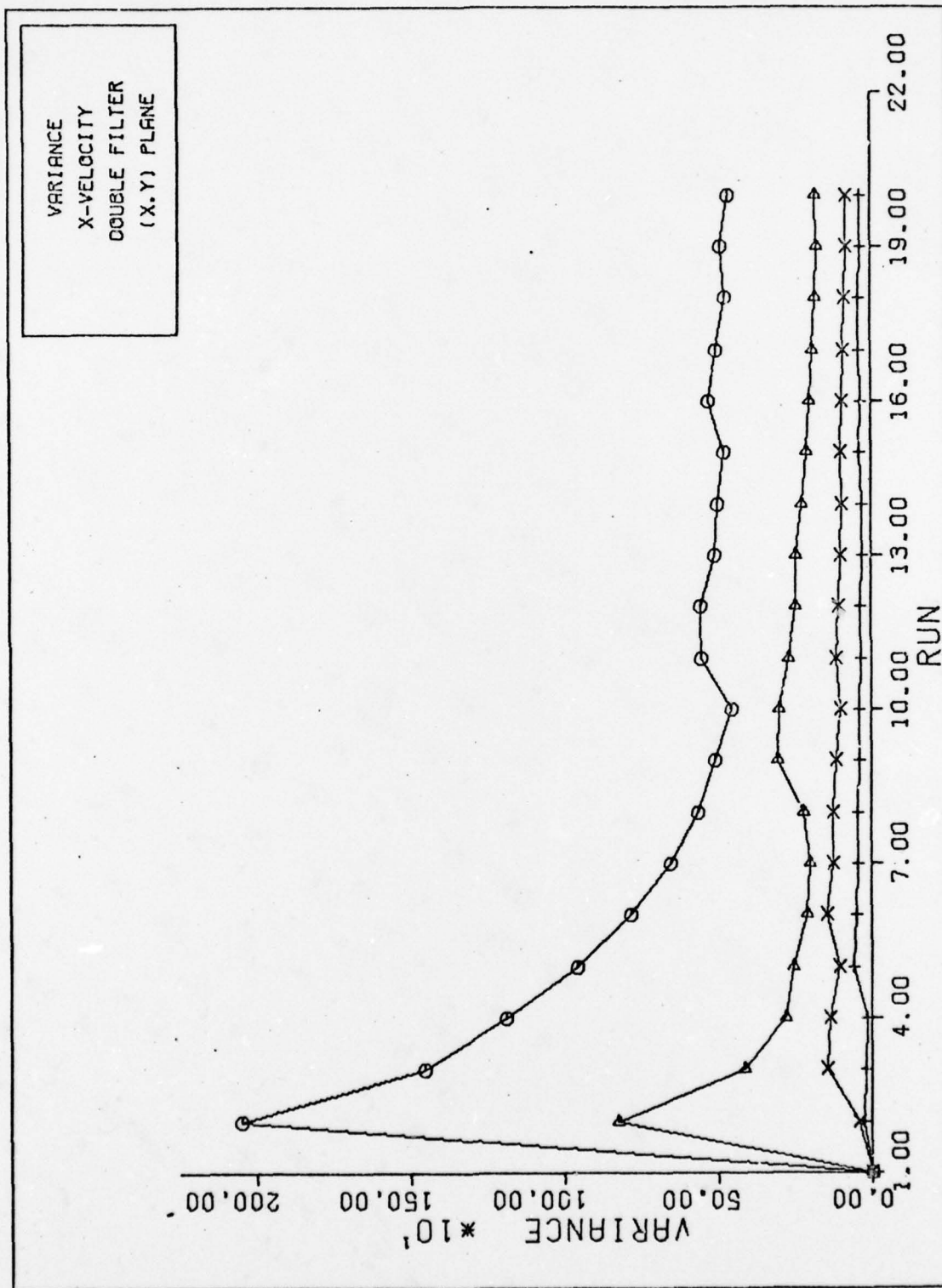


Fig. C-3

VARIANCE CONVERGENCE

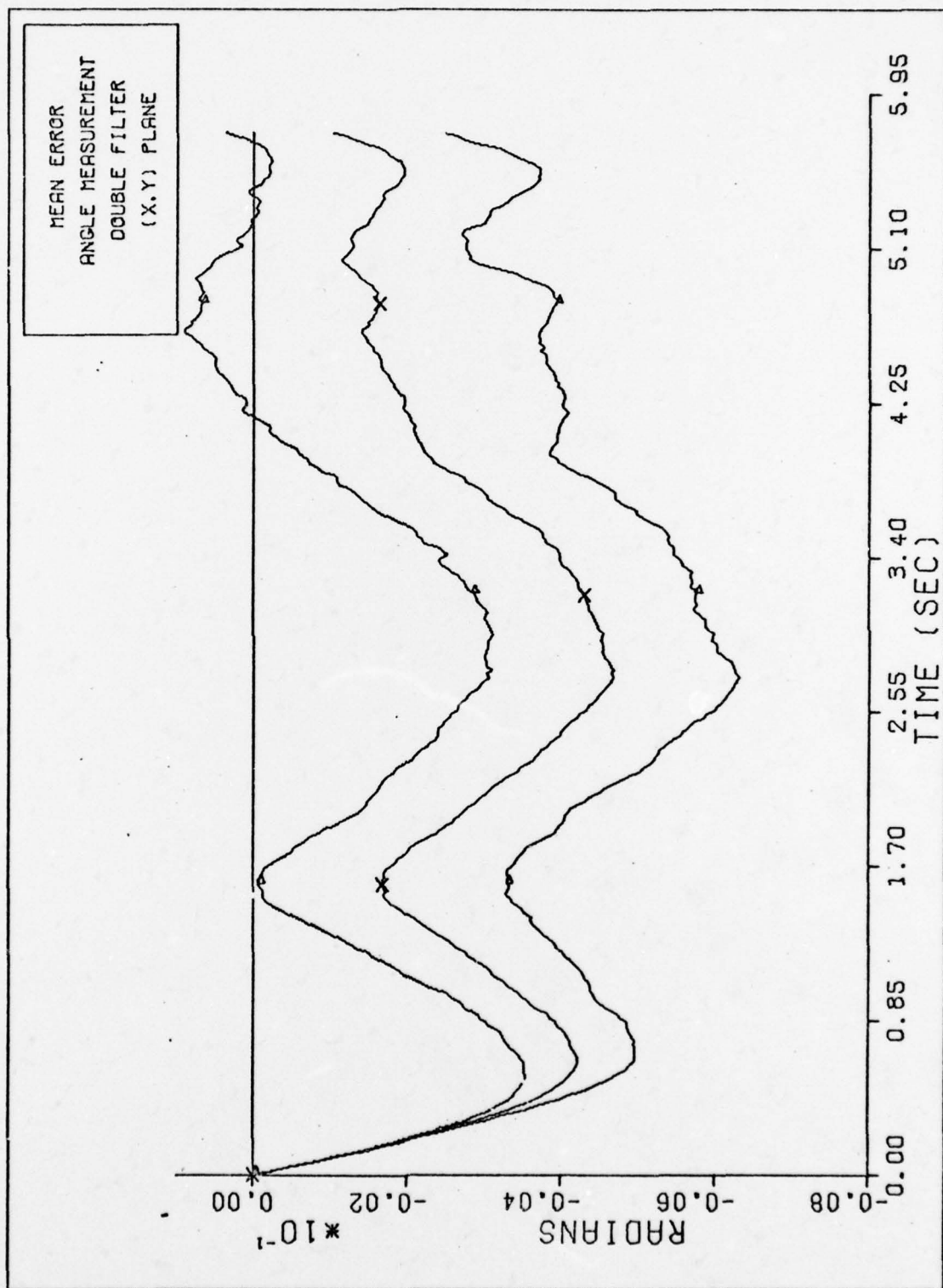


Fig. C-4 ANGLE MEASUREMENT DOUBLE FILTER

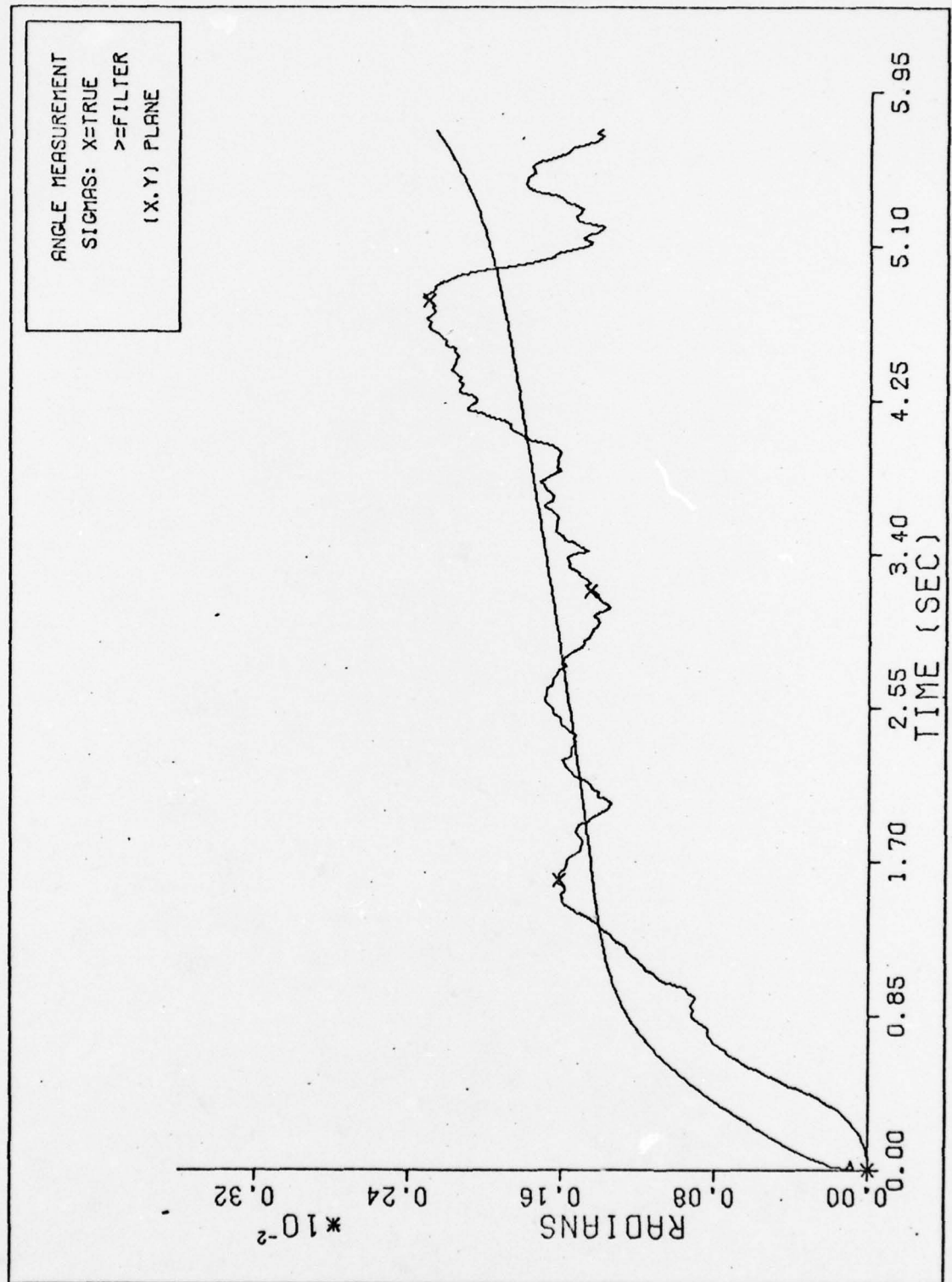


Fig. C-5 ANGLE MEASUREMENT SIGMAS DOUBLE FILTER

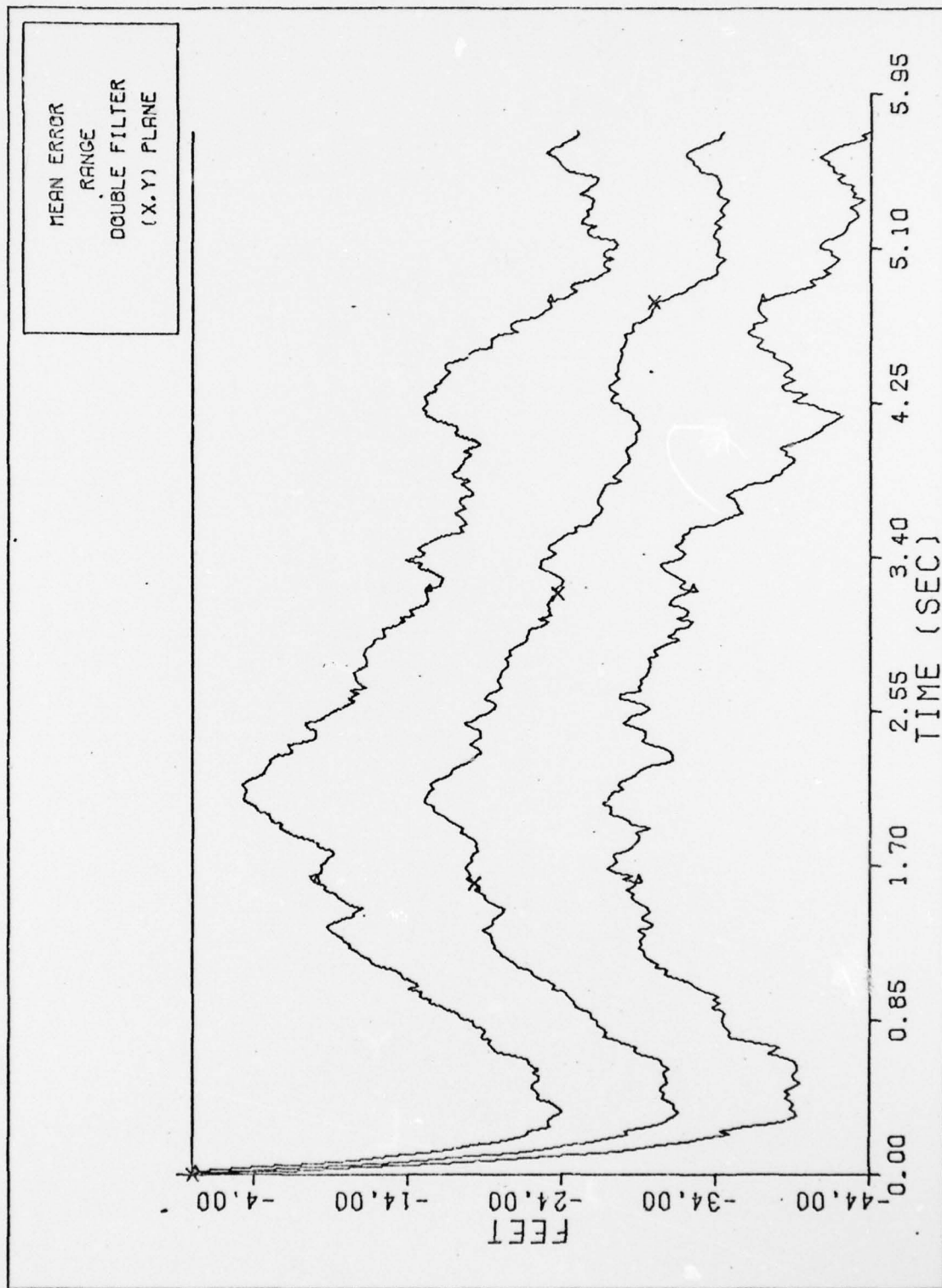


Fig. C-6

RANGE DOUBLE FILTER

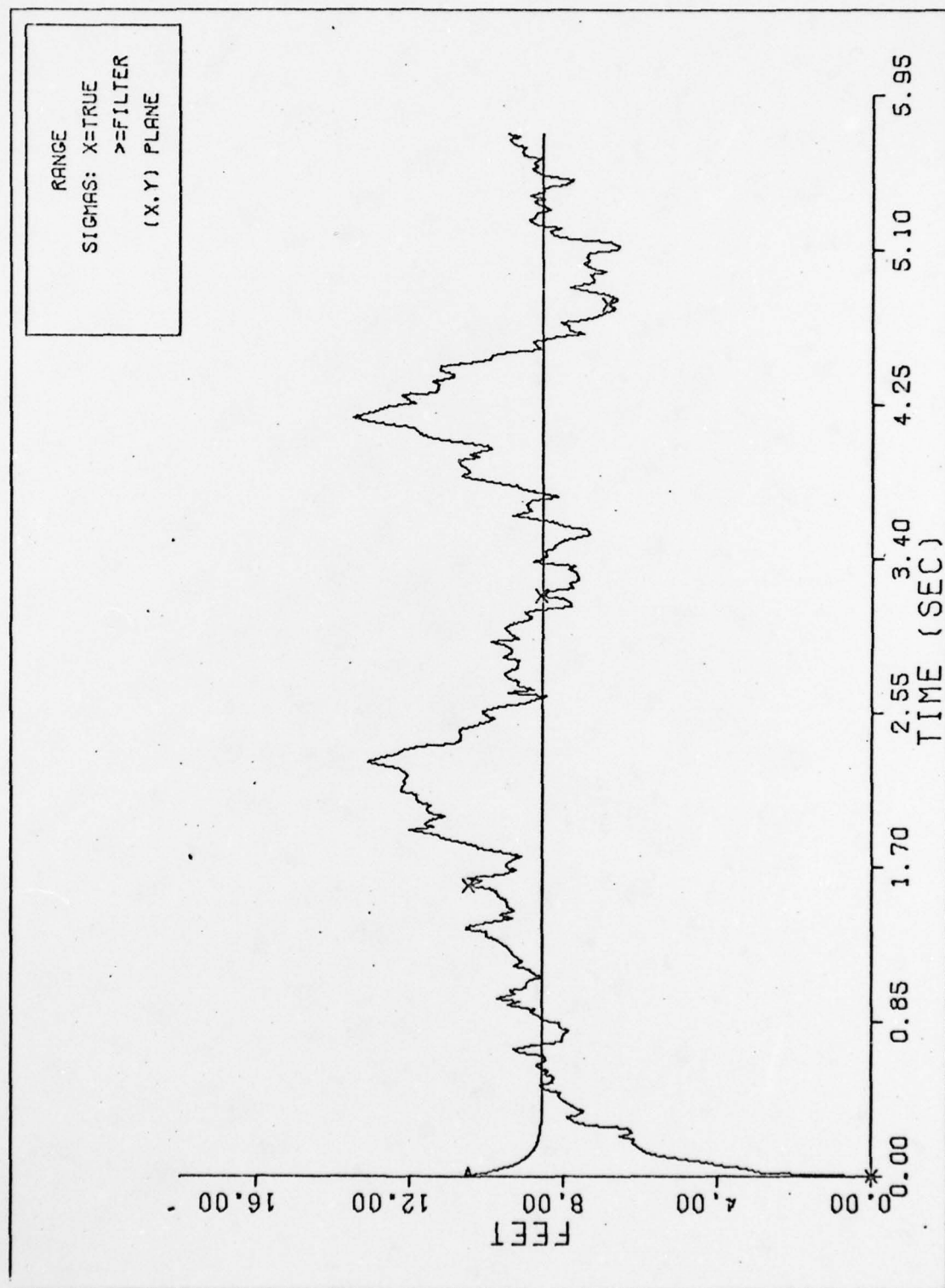


Fig. C-7

RANGE SIGMAS DOUBLE FILTER

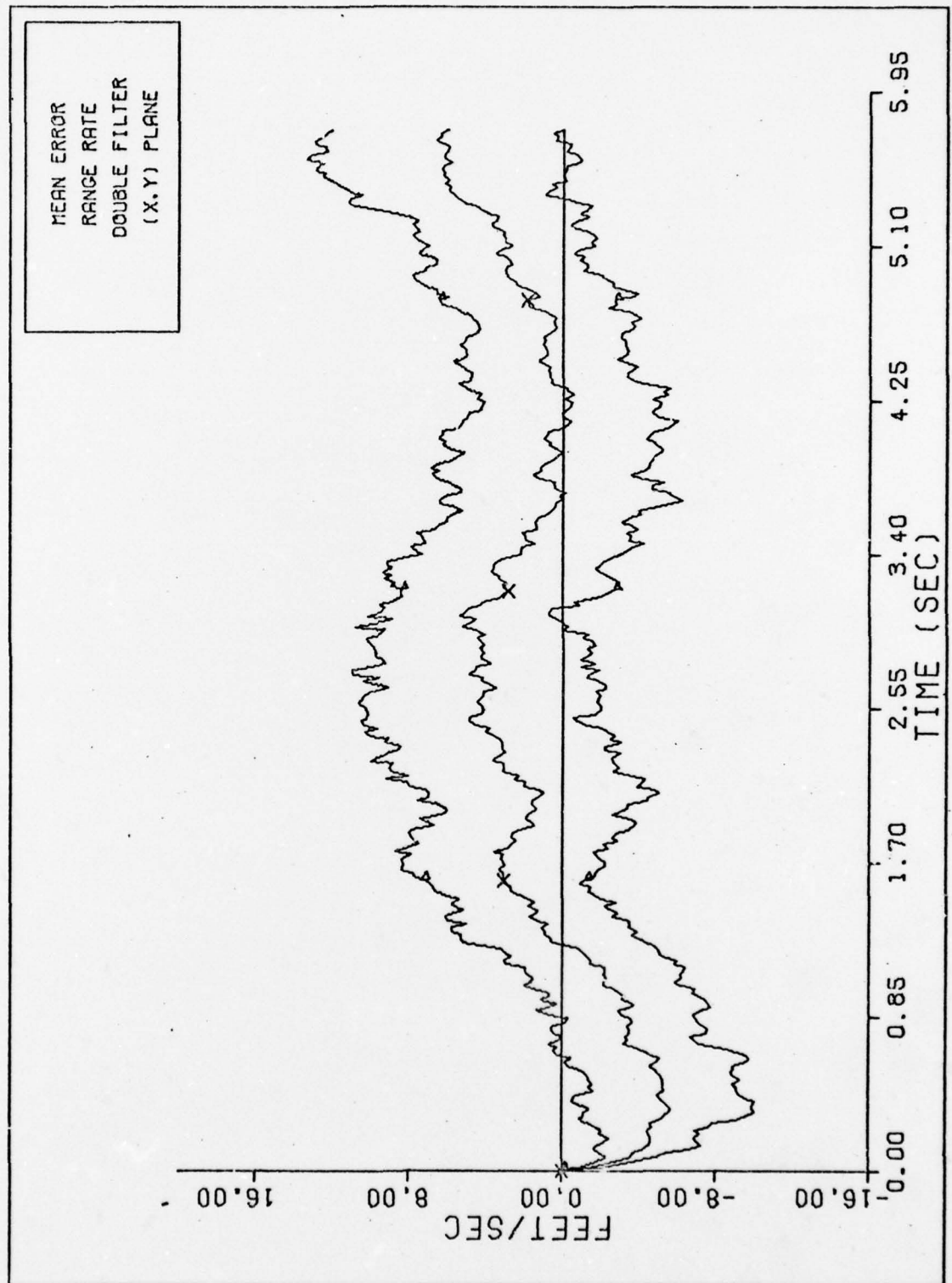


Fig. C-8

RANGE RATE DOUBLE FILTER

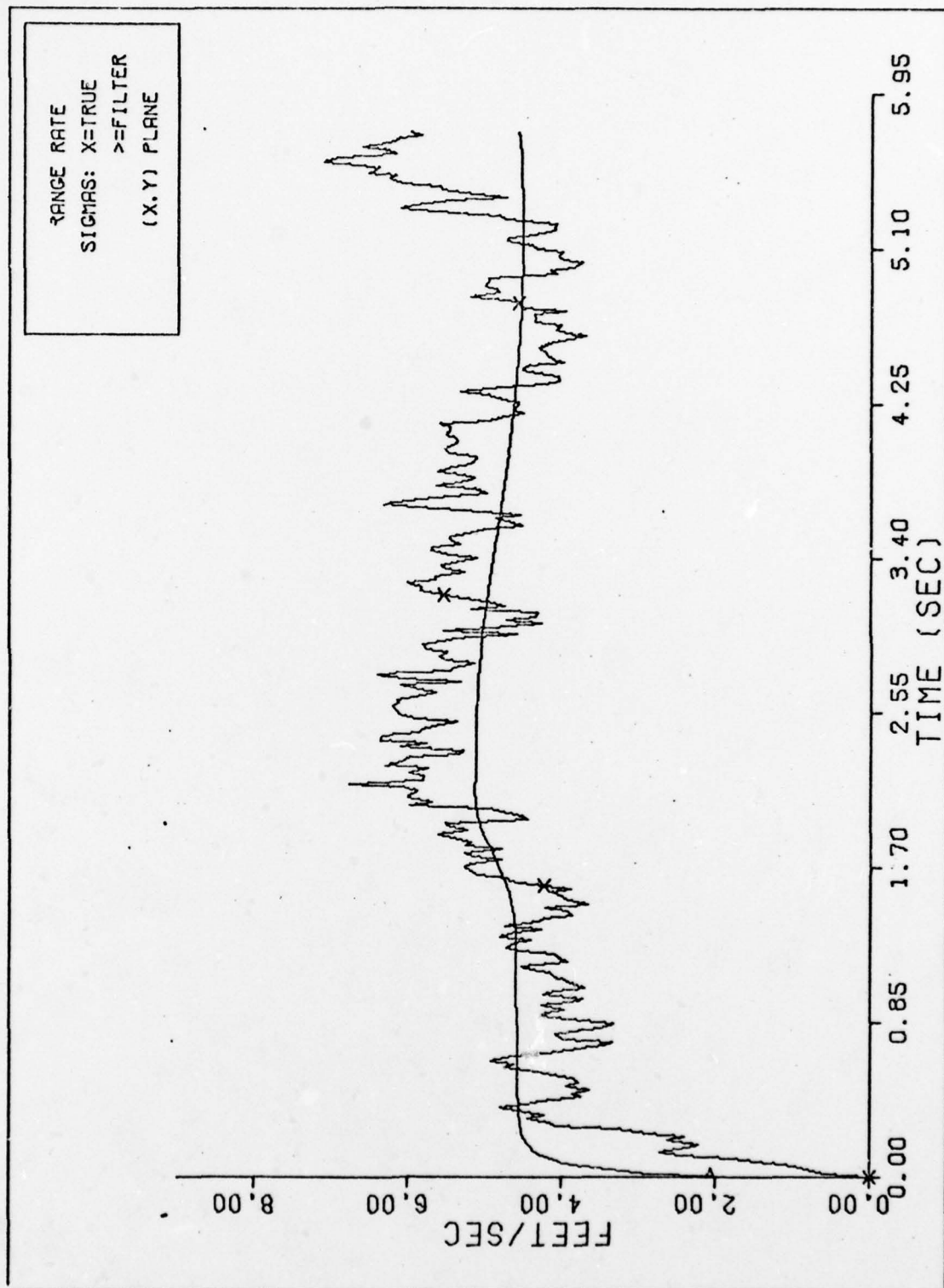


Fig. C-9

RANGE RATE SIGMAS DOUBLE FILTER

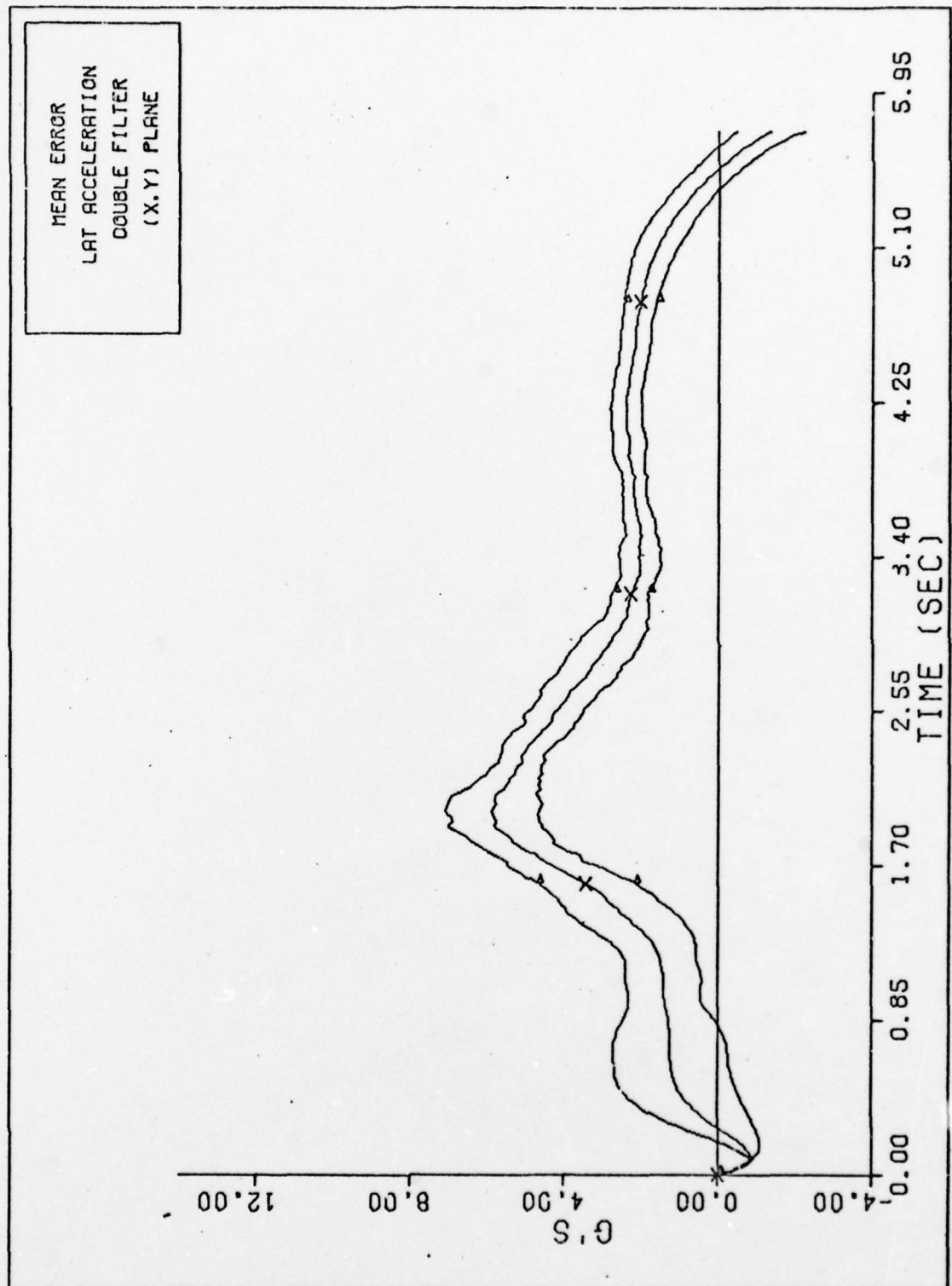


Fig. C-10 LAT ACCELERATION DOUBLE FILTER

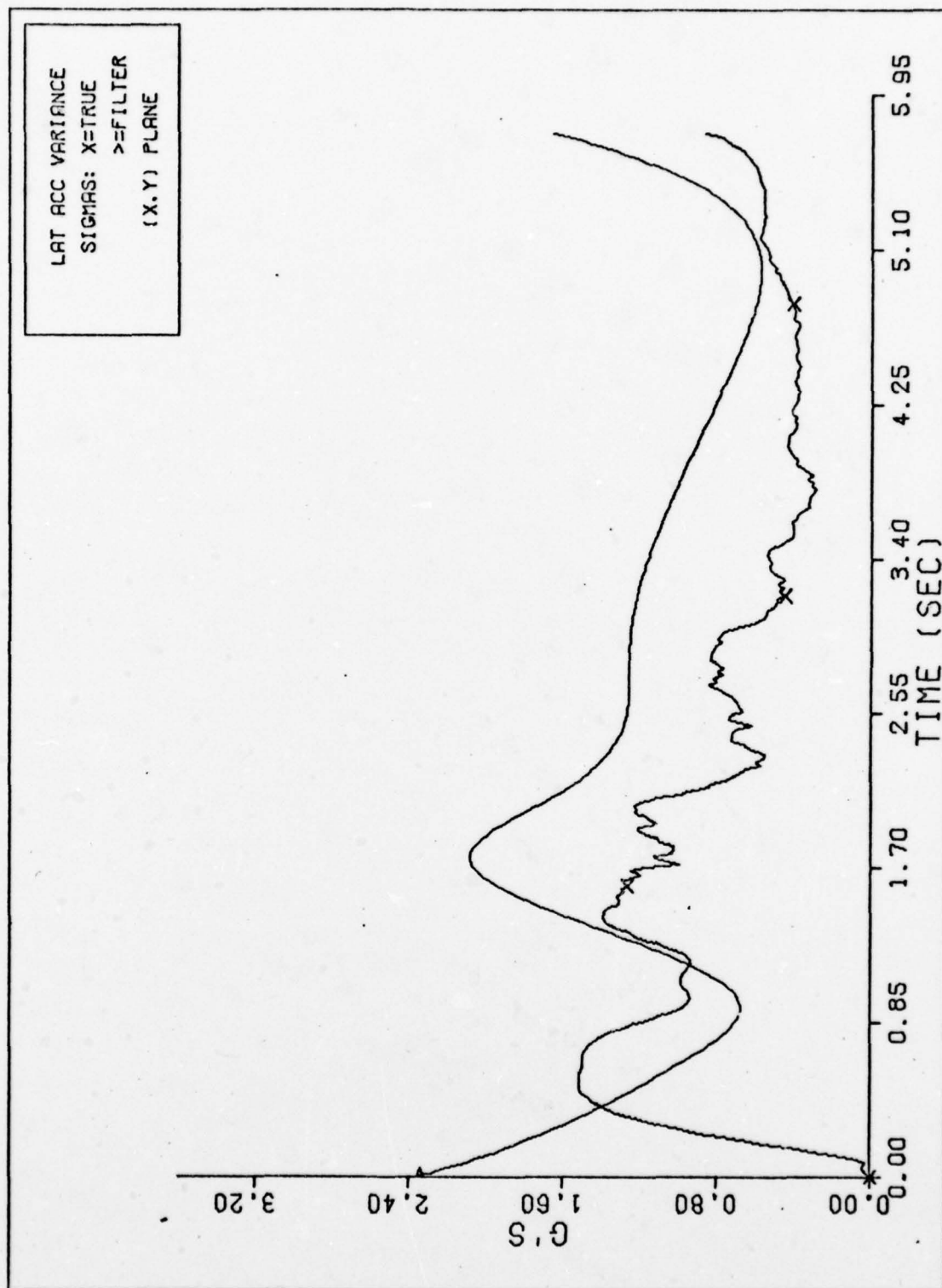


Fig. C-11 LAT ACCELERATION SIGMAS DOUBLE FILTER

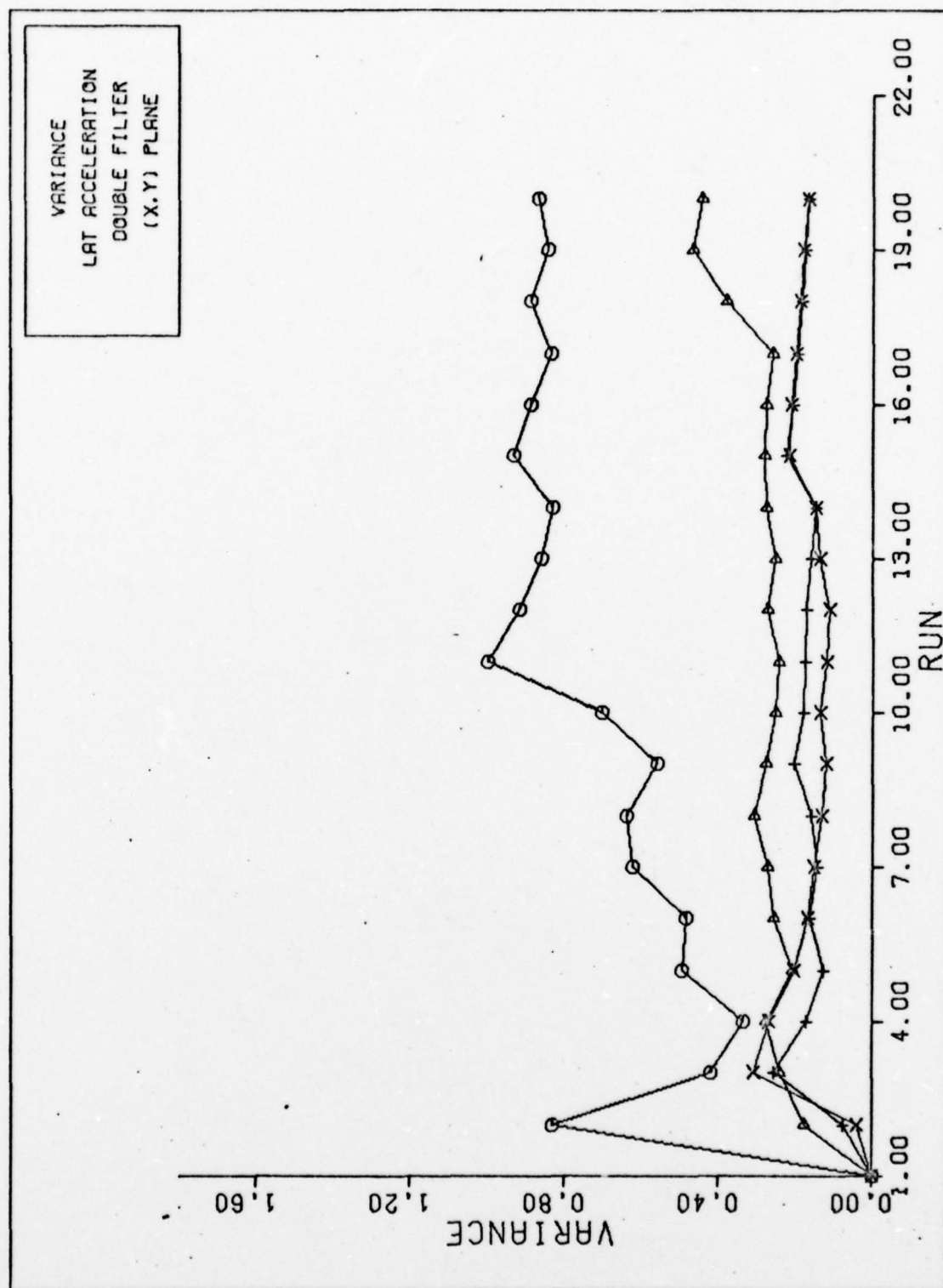


Fig. C-12

VARIANCE CONVERGENCE

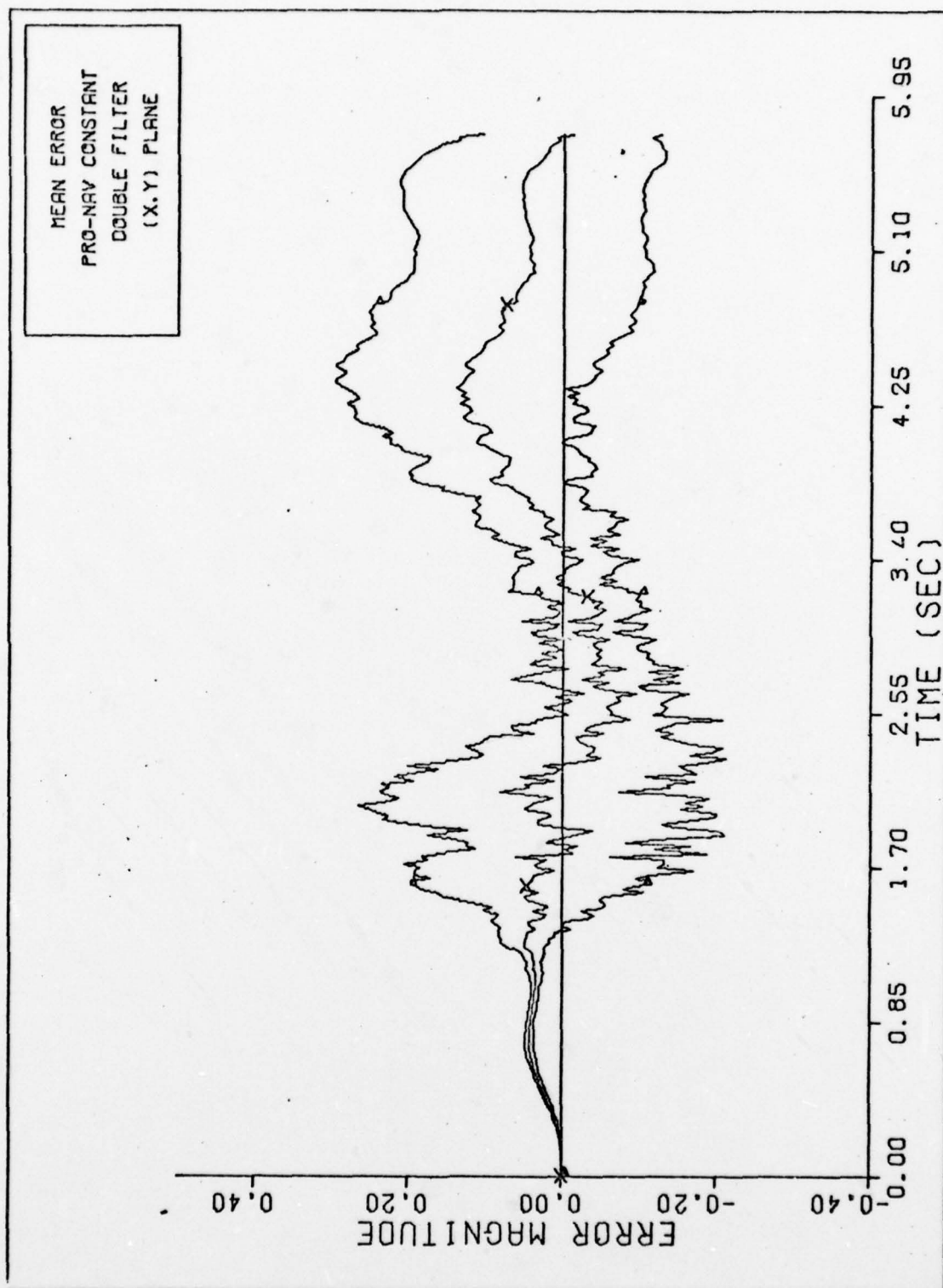


Fig. C-13 PRO-NAV CONSTANT DOUBLE FILTER

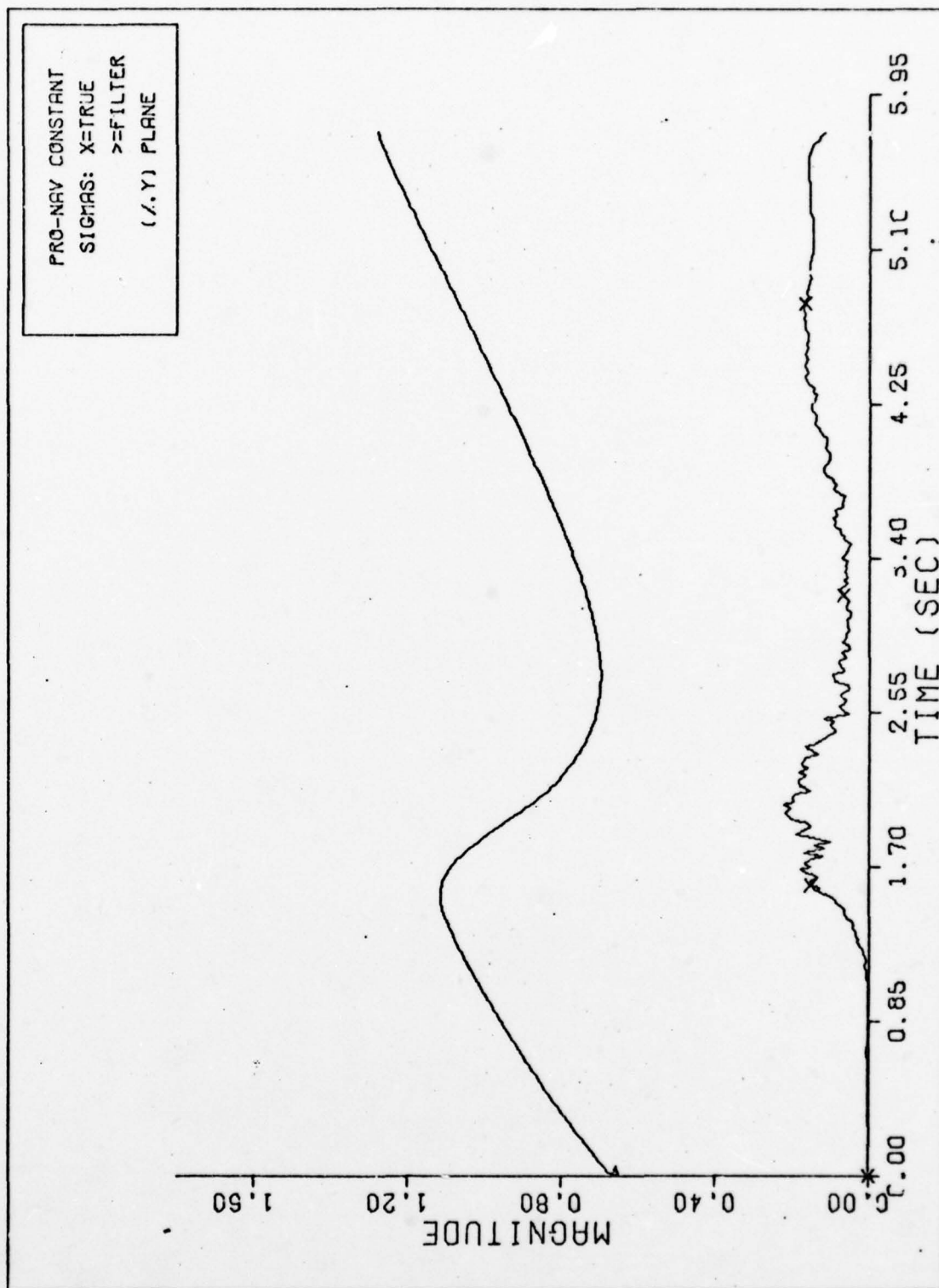


Fig. C-14 PRO-NAV CONSTANT SIGMAS DOUBLE FILTER

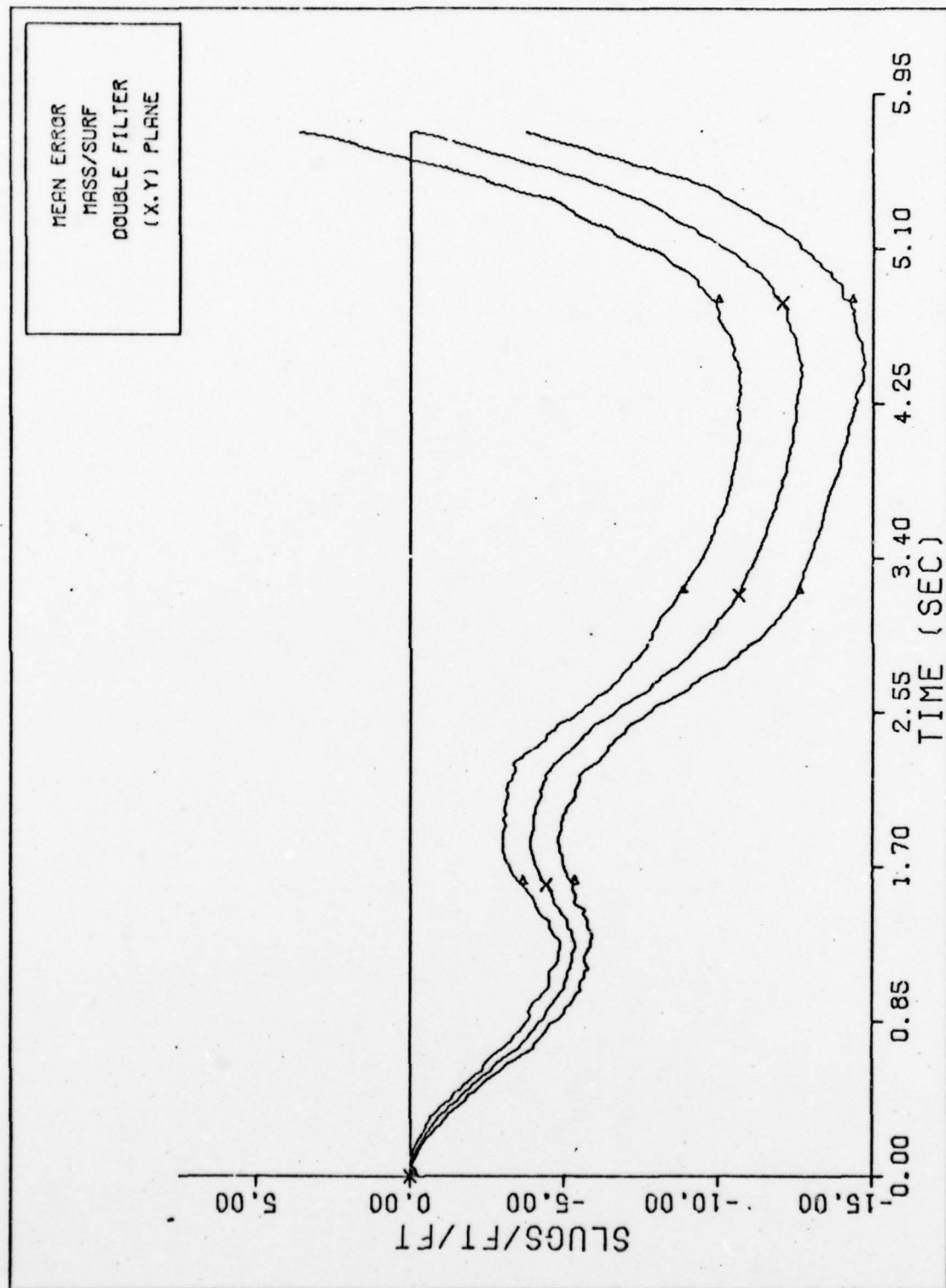


Fig. C-15

MASS/SURF DOUBLE FILTER

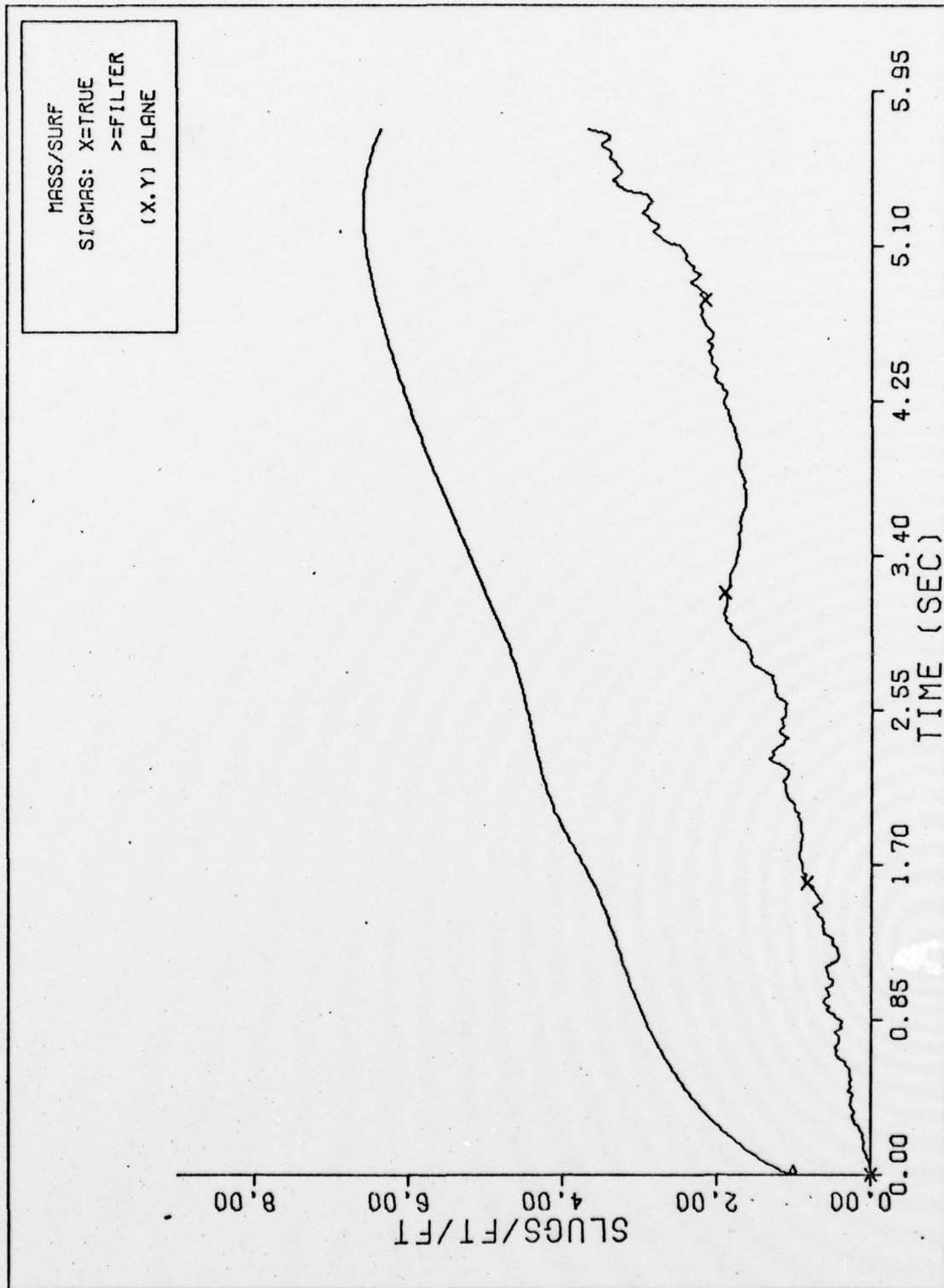


Fig. C-16

MASS/SURF SIGMAS DOUBLE FILTER

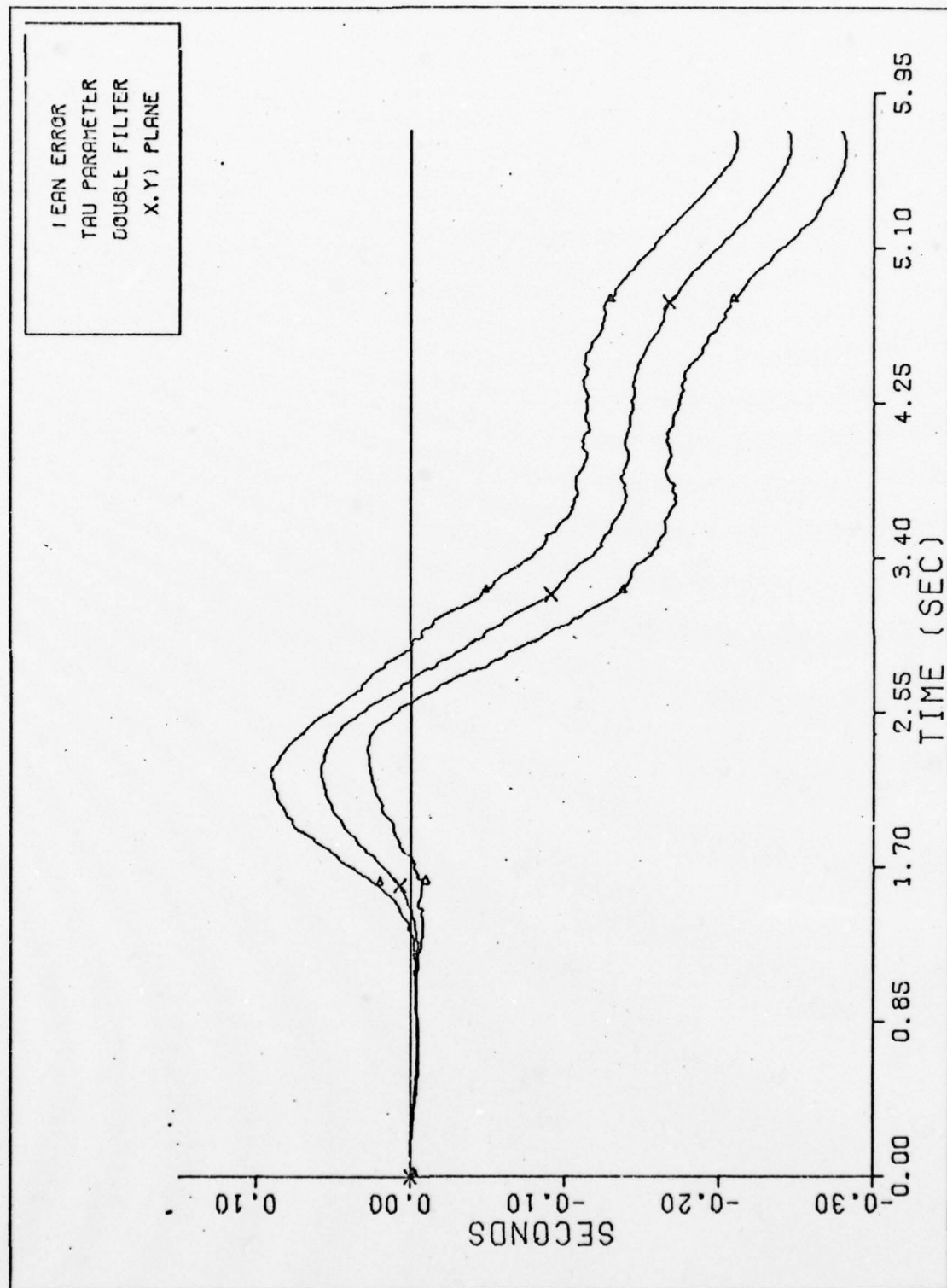


Fig. C-17

TAU PARAMETER DOUBLE FILTER

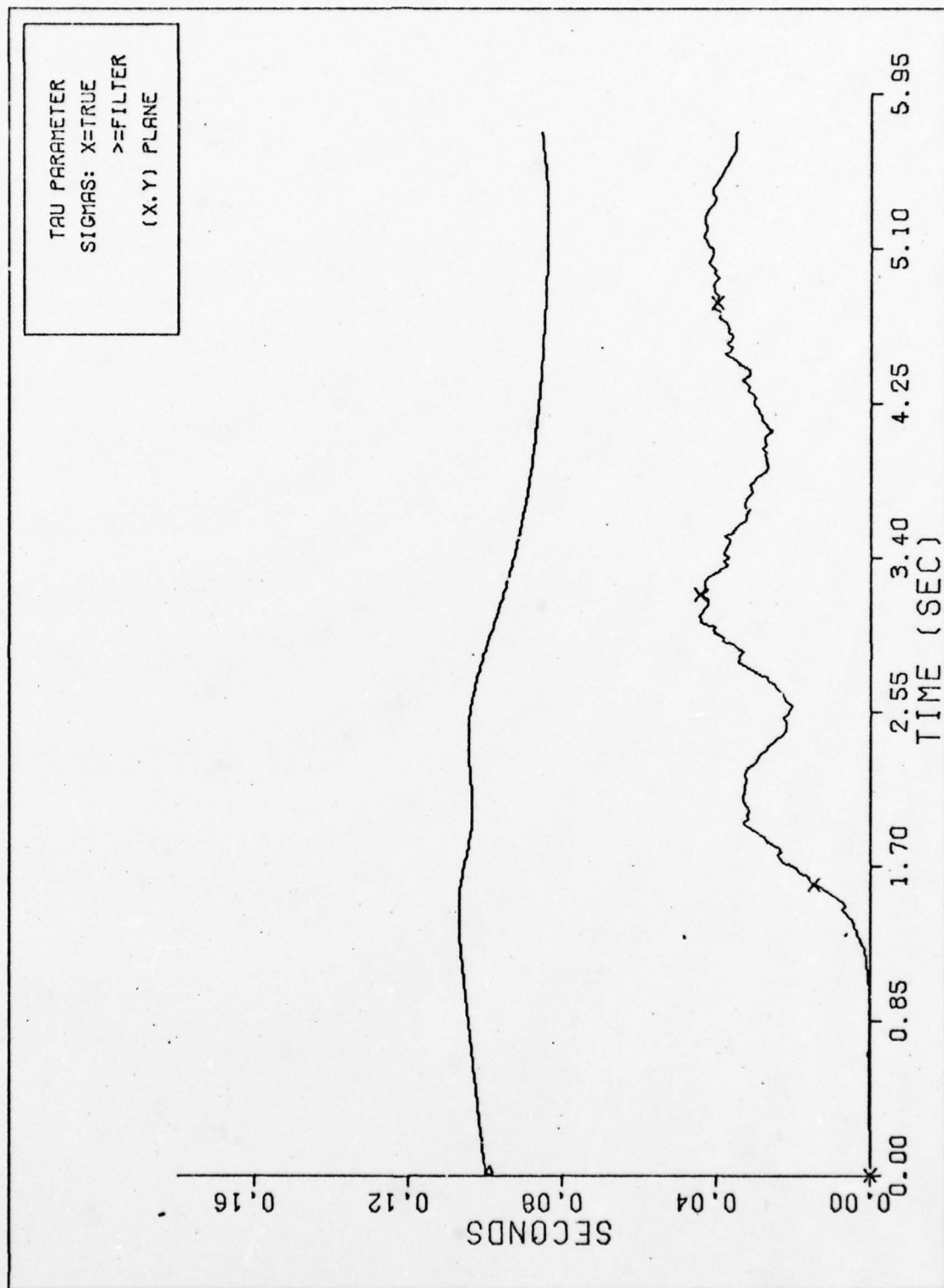


Fig. C-18

TAU PARAMETER SIGMAS DOUBLE FILTER

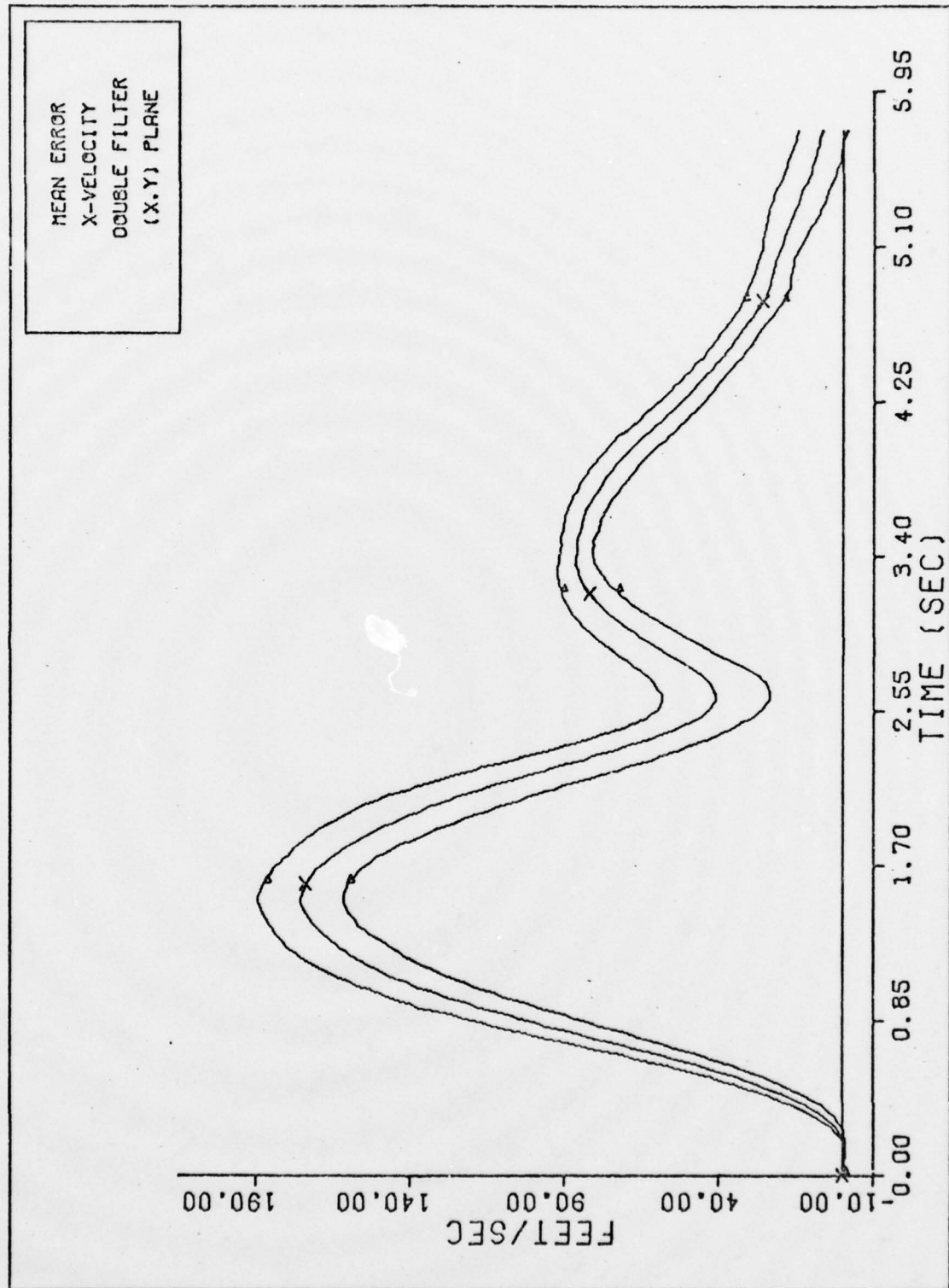


Fig. C-19

X-VELOCITY DOUBLE FILTER

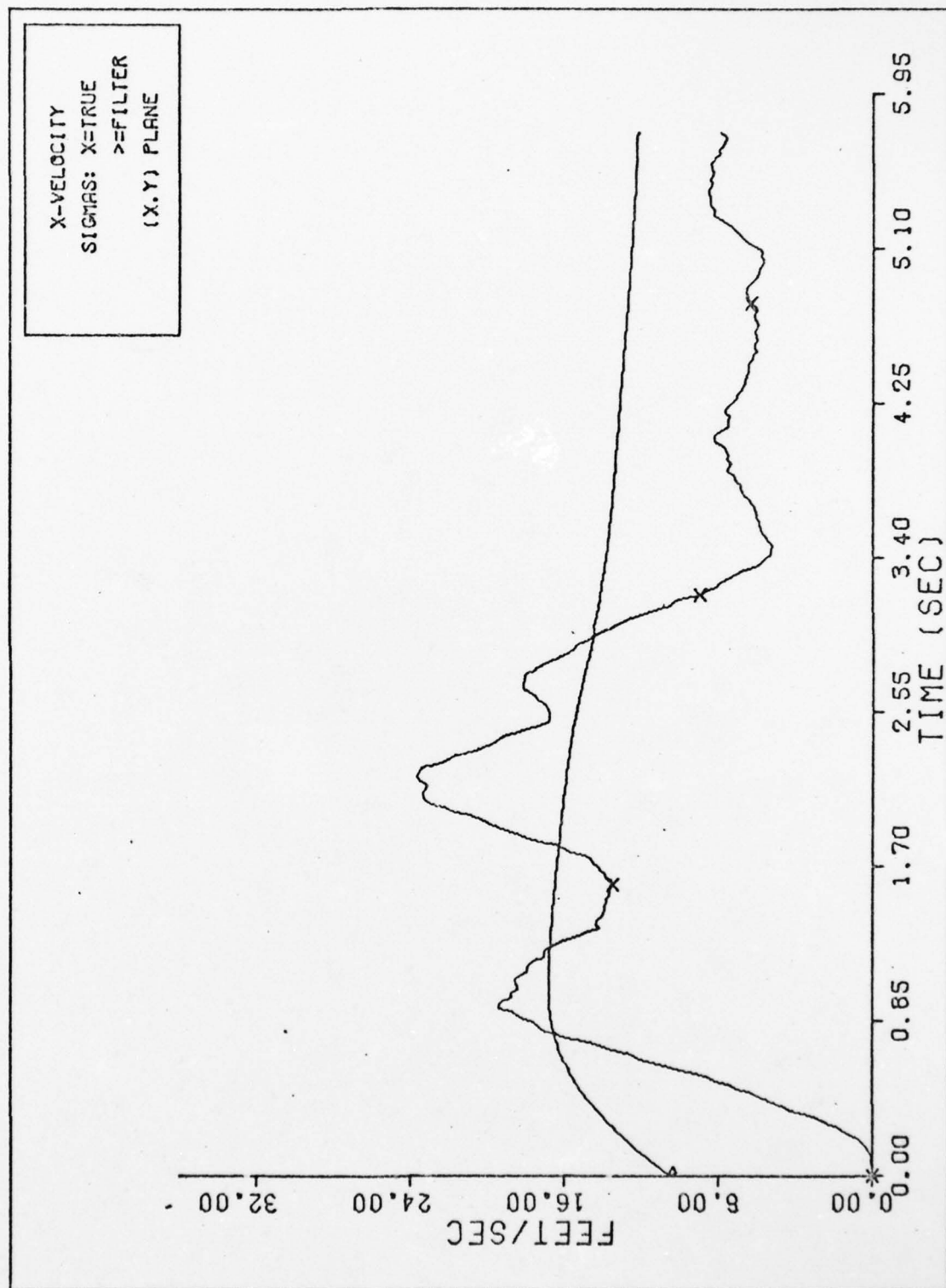


Fig. C-20

X-VELOCITY SIGMAS DOUBLE FILTER

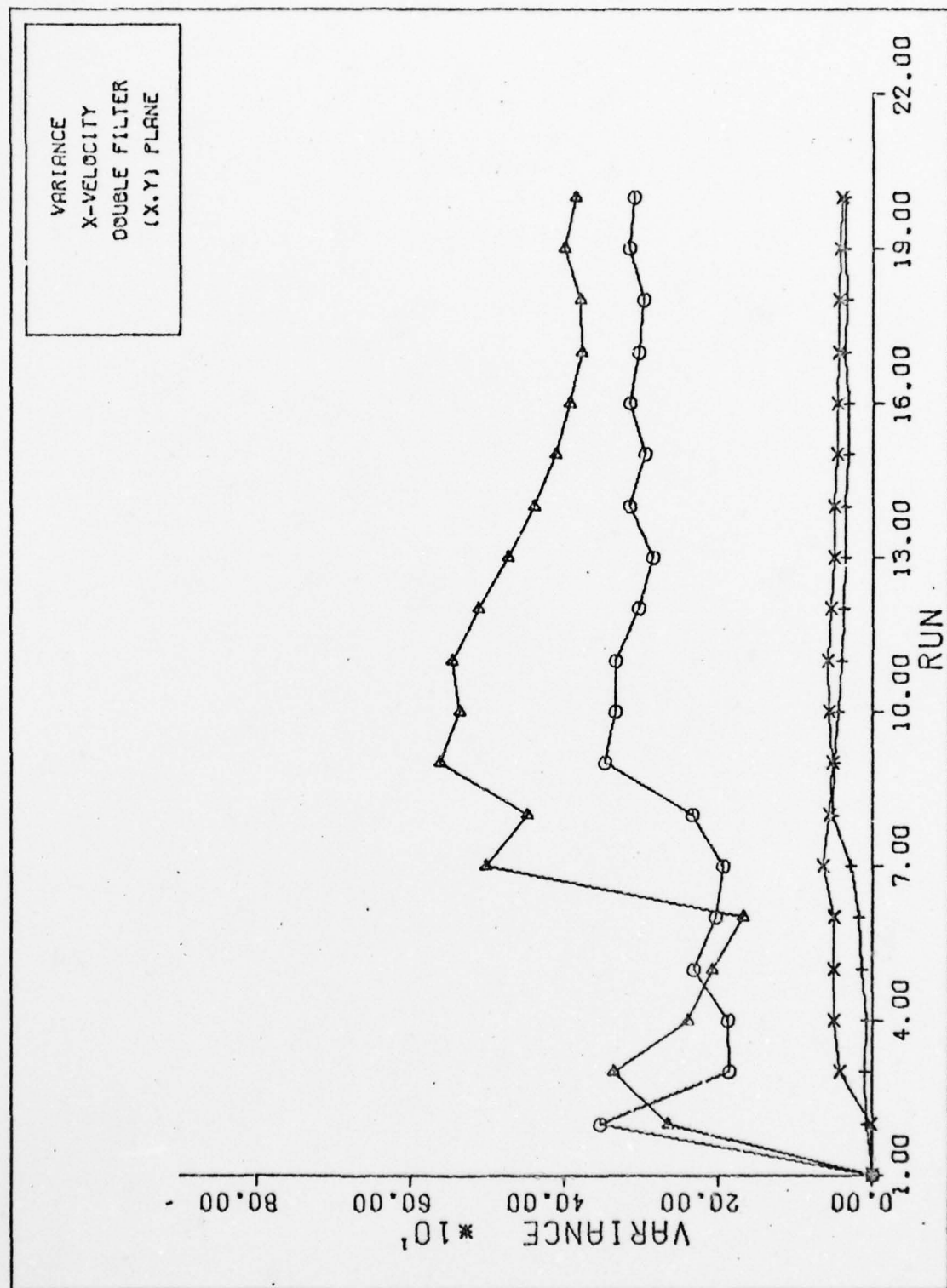


Fig. C-21

VARIANCE CONVERGENCE

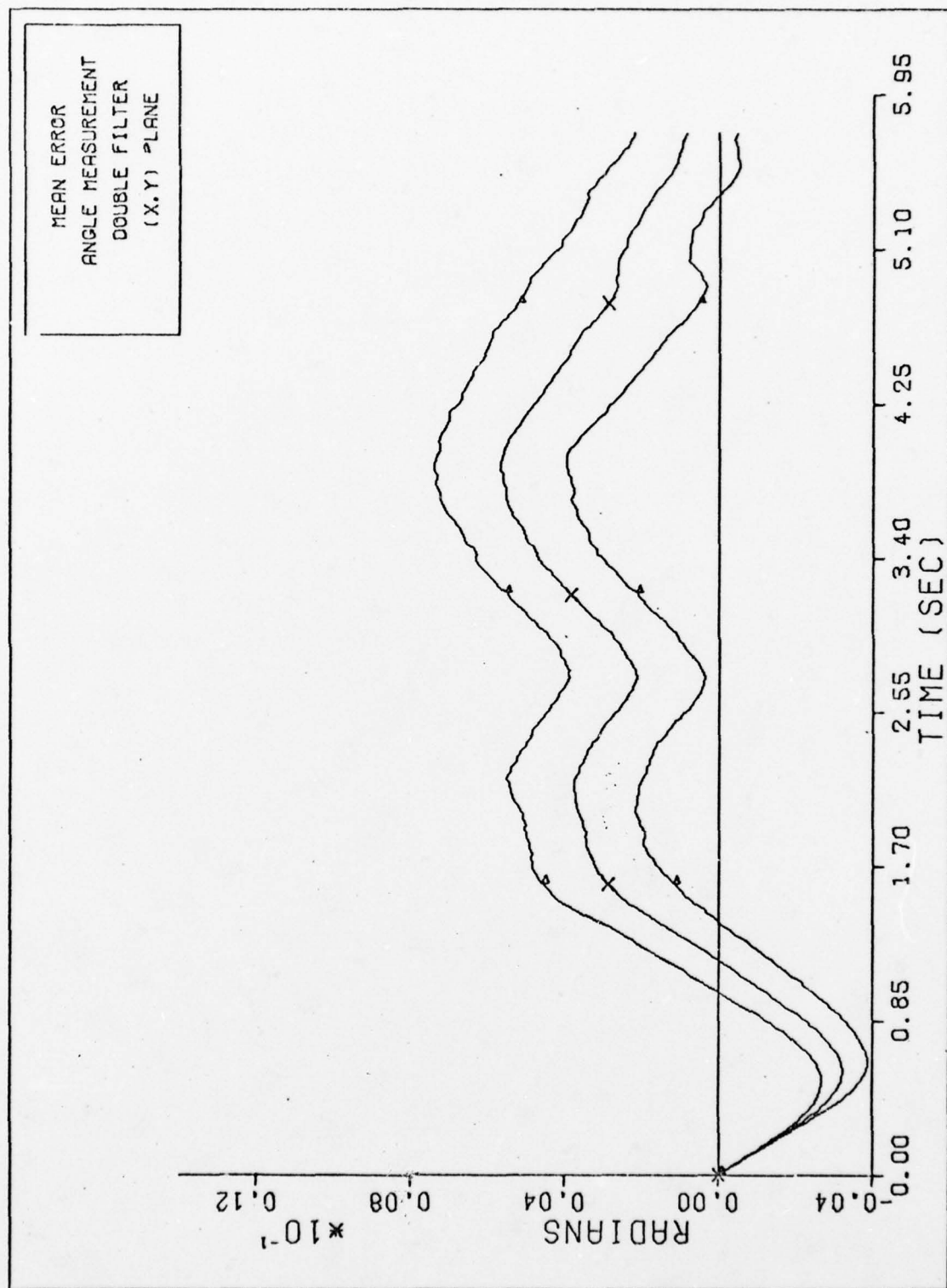


Fig. C-22

ANGLE MEASUREMENT DOUBLE FILTER

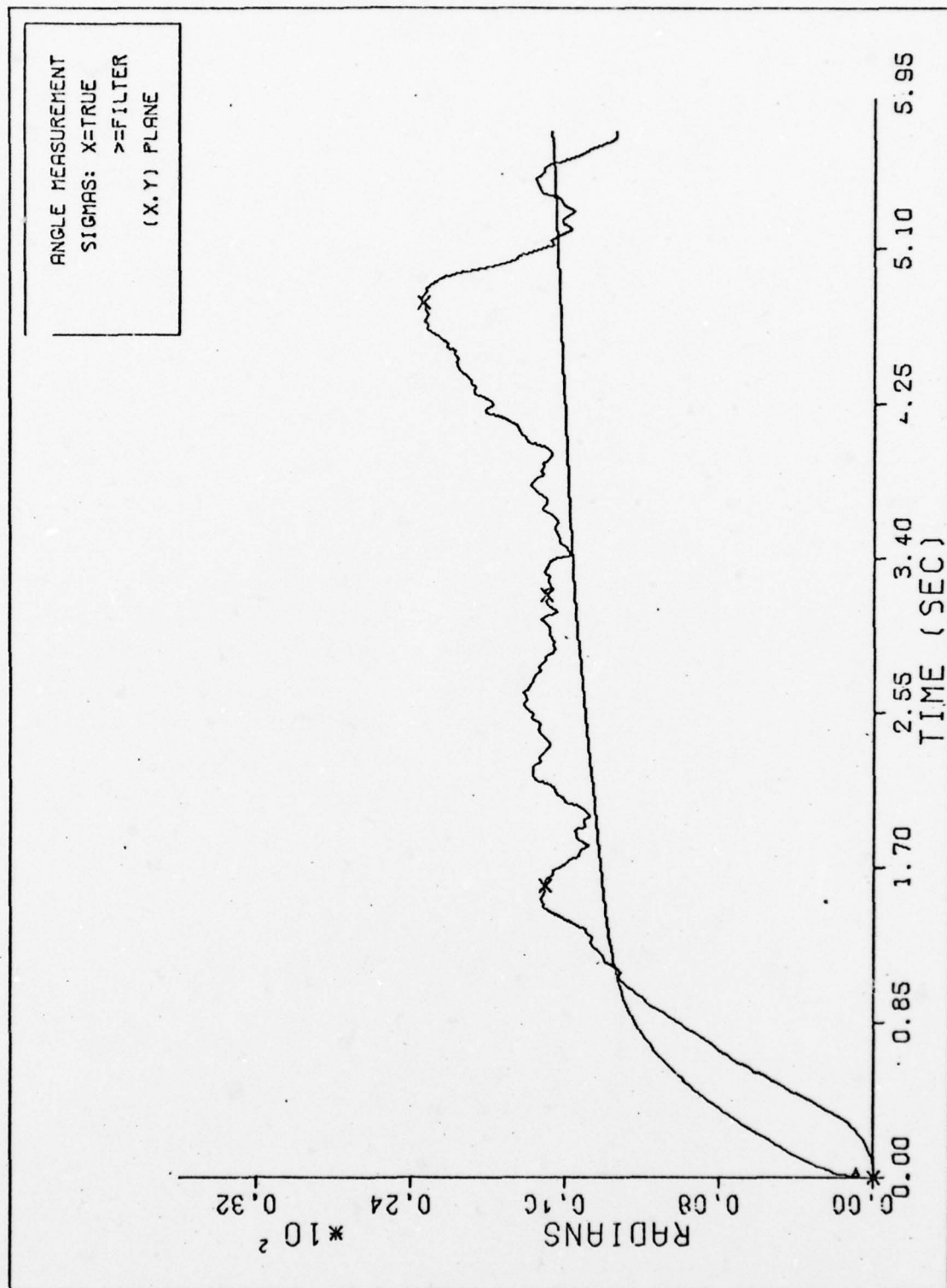


Fig. C-23 ANGLE MEASUREMENT SIGMAS DOUBLE FILTER

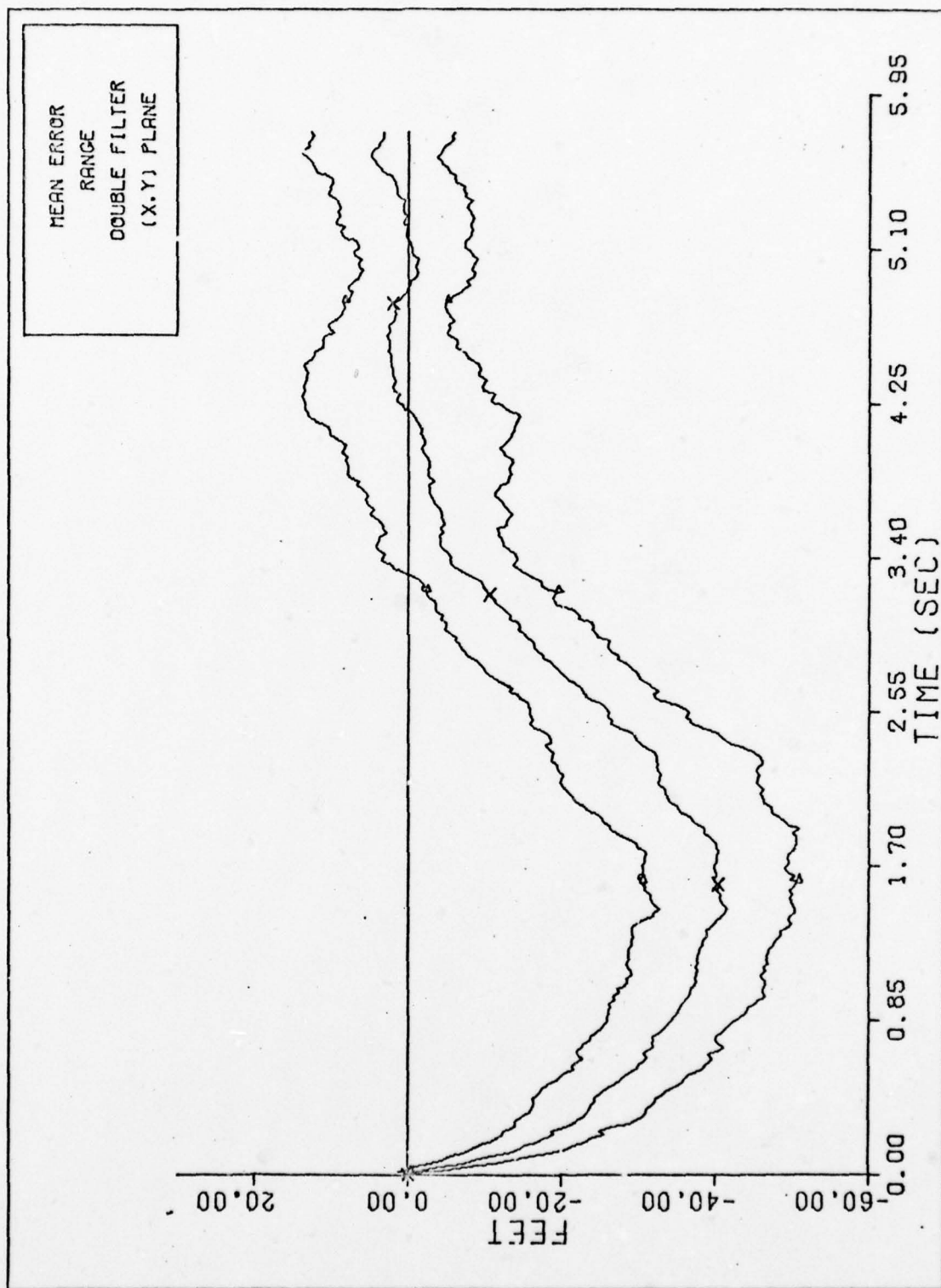


Fig. C-24

RANGE DOUBLE FILTER

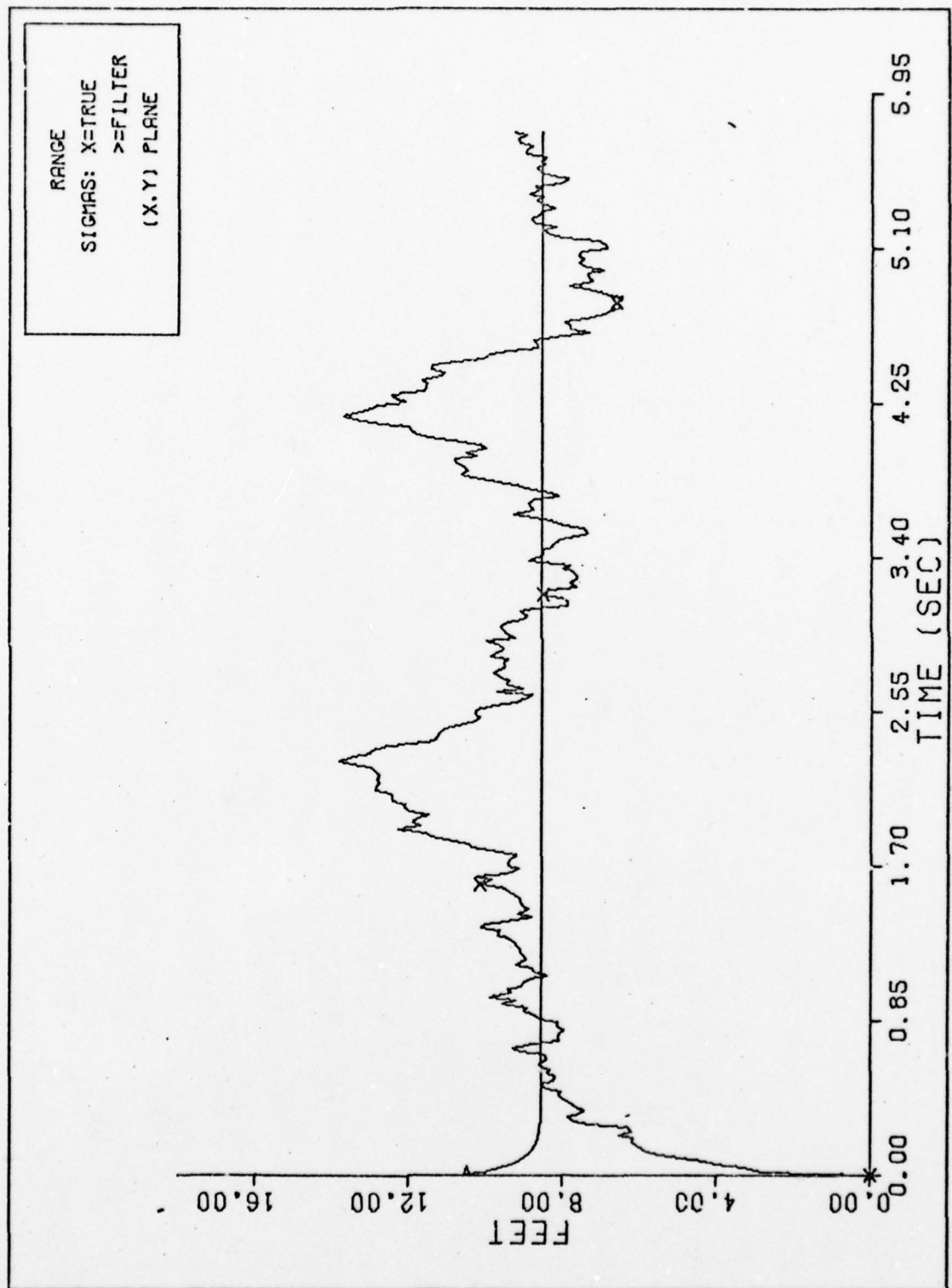


Fig. C-25

RANGE SIGMAS DOUBLE FILTER

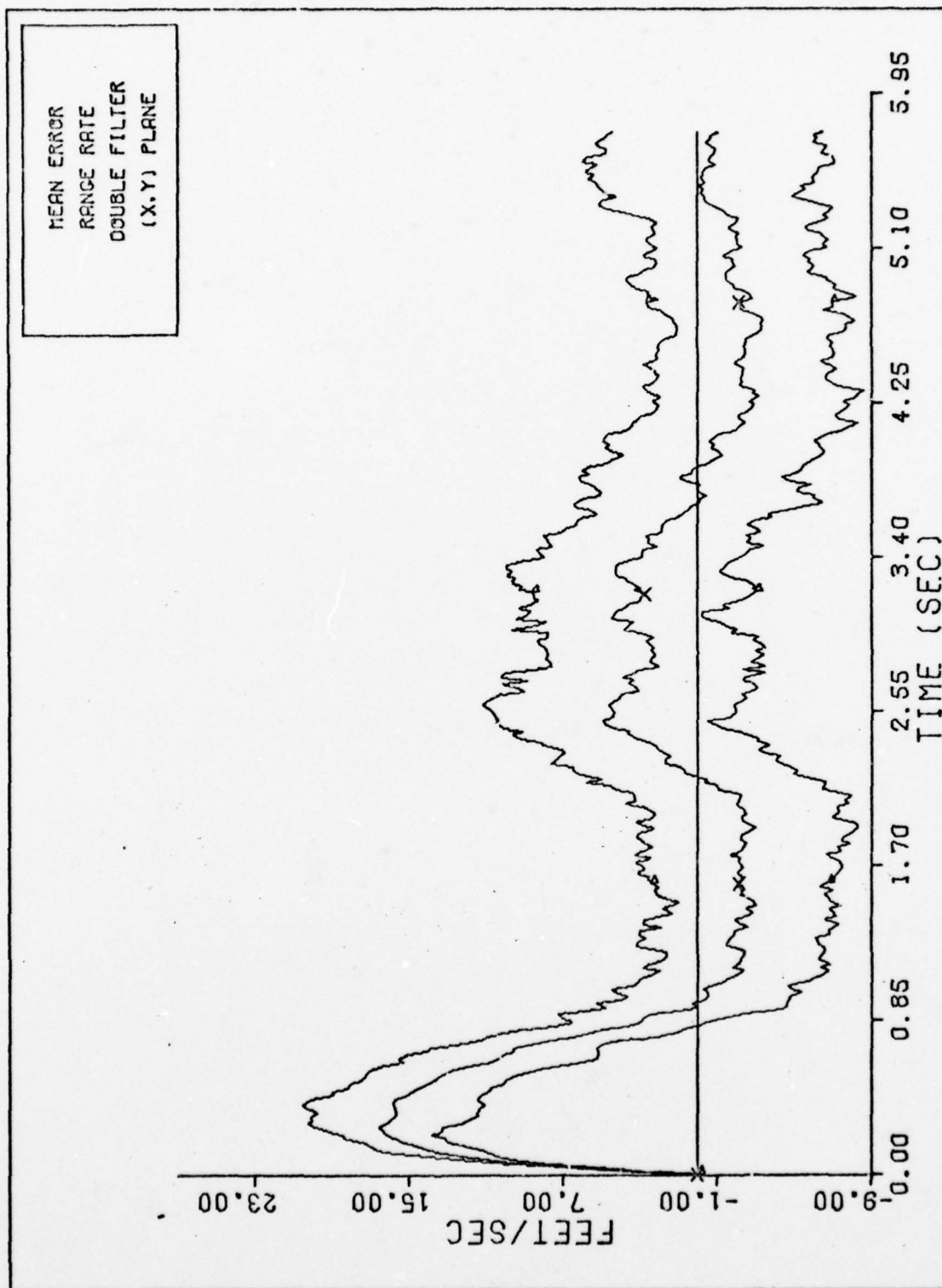


Fig. C-26

RANGE RATE DOUBLE FILTER

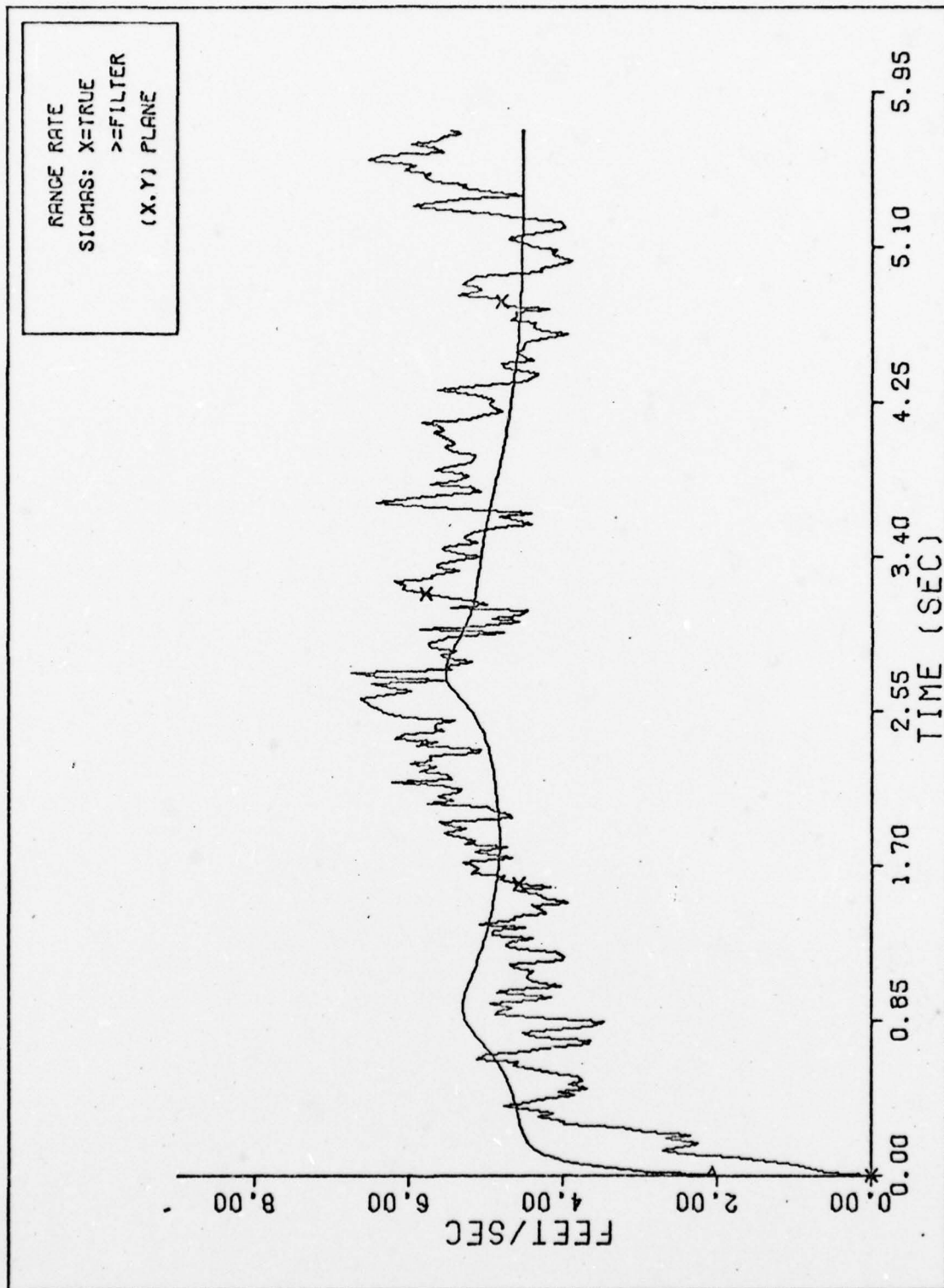


Fig. C-27

RANGE RATE SIGMAS DOUBLE FILTER

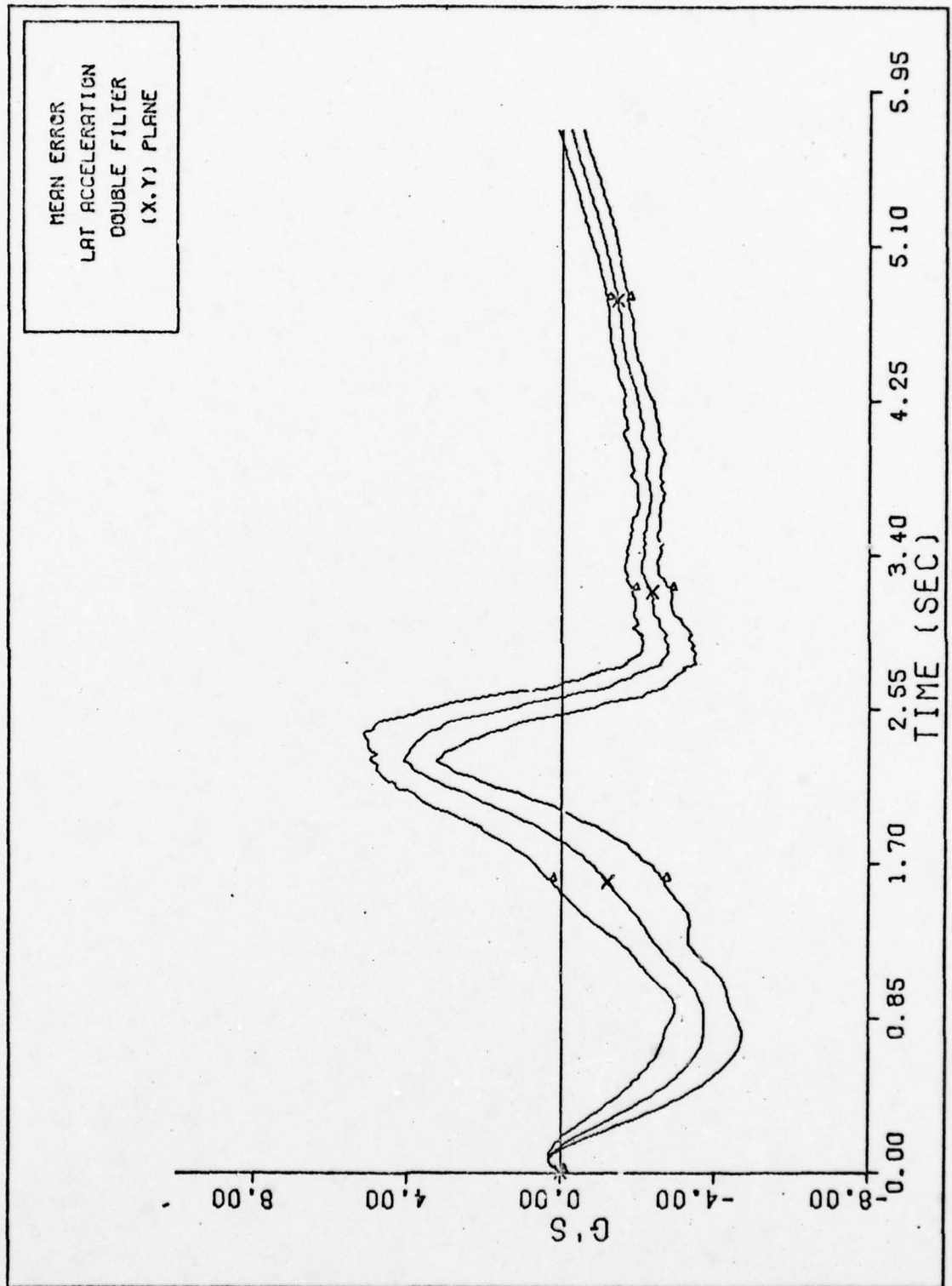


Fig. C-28 LAT ACCELERATION DOUBLE FILTER

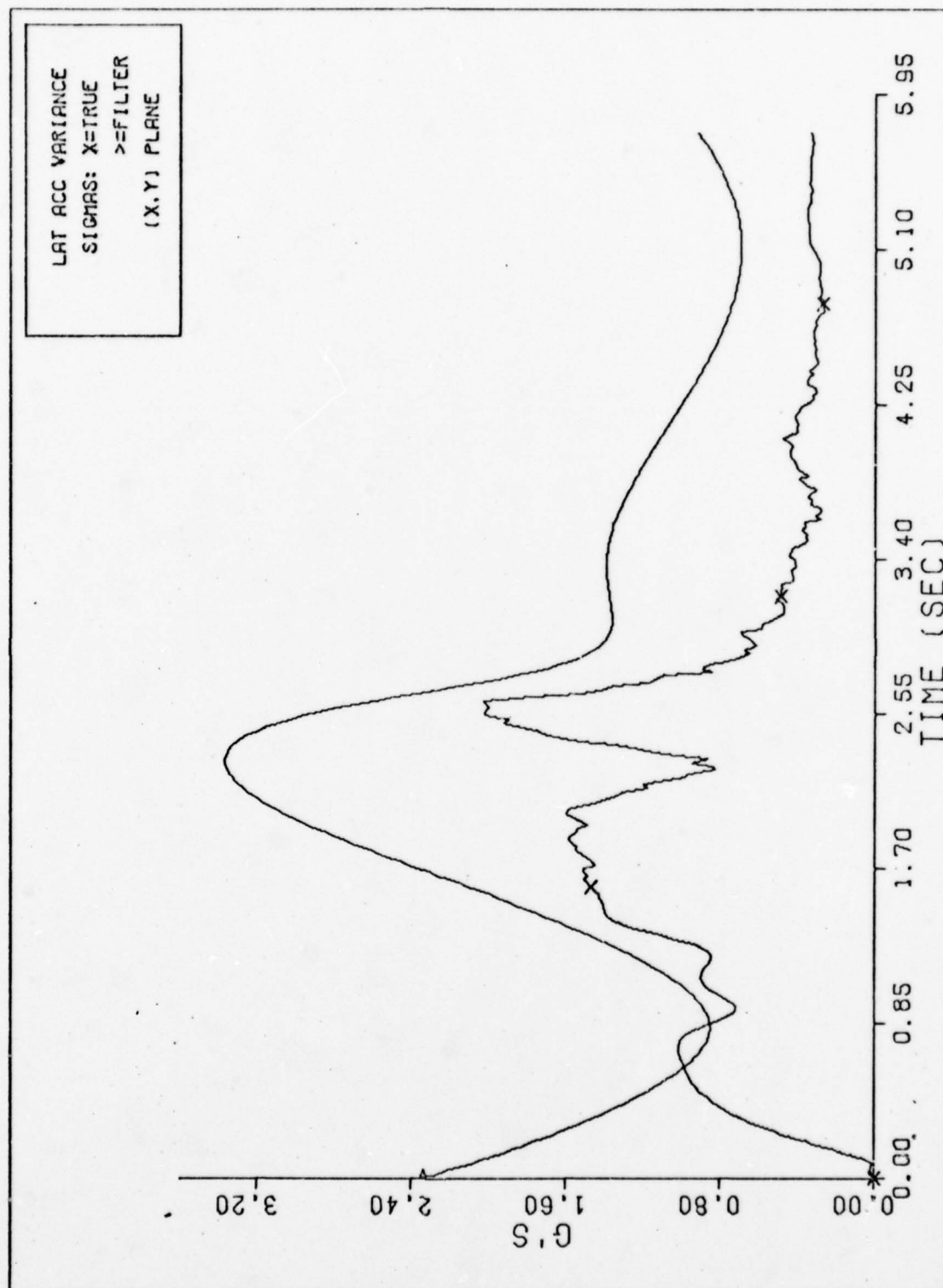


Fig. C-29 LAT ACCELERATION SIGMAS DOUBLE FILTER

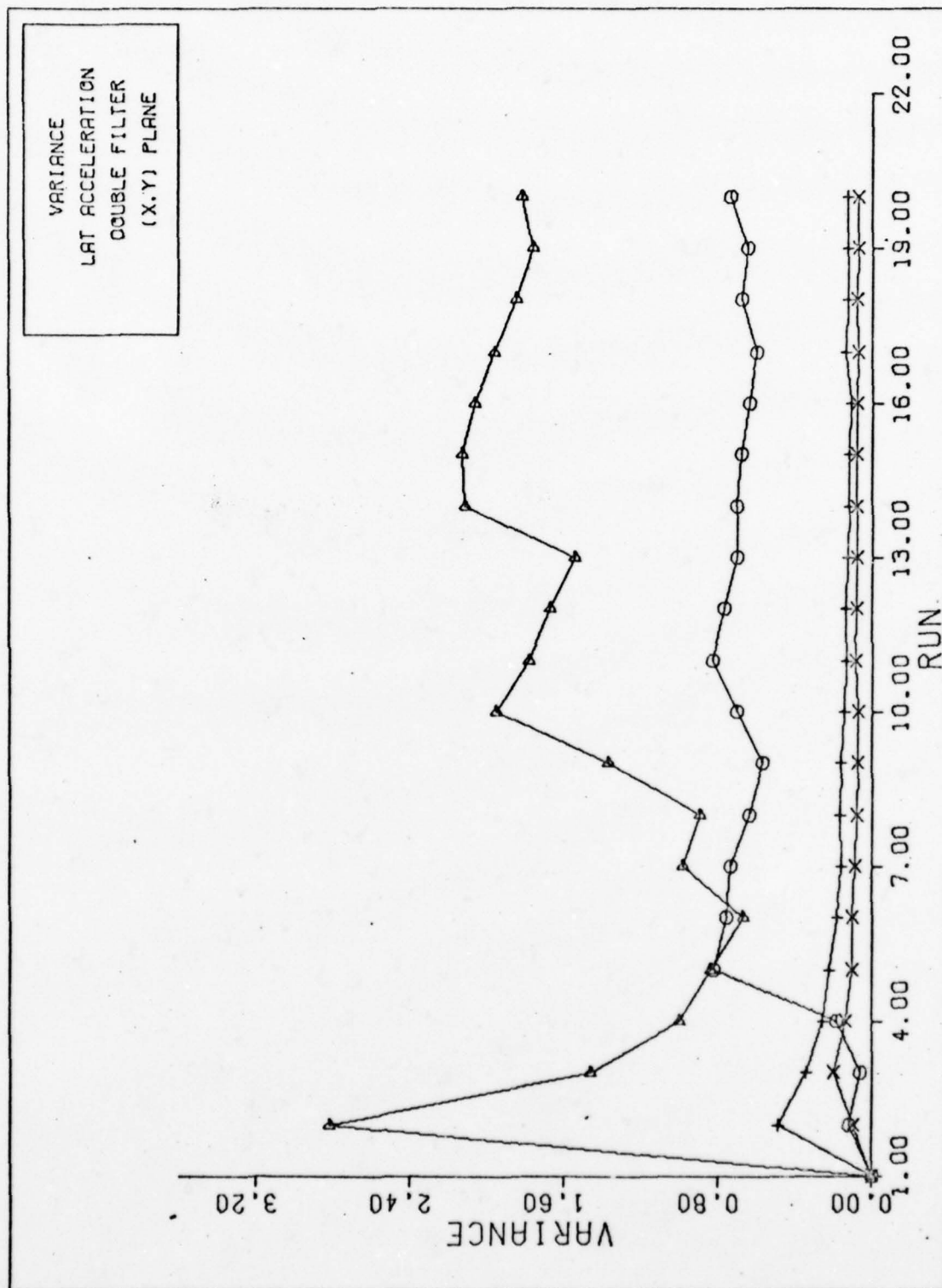


Fig. C-30

VARIANCE CONVERGENCE

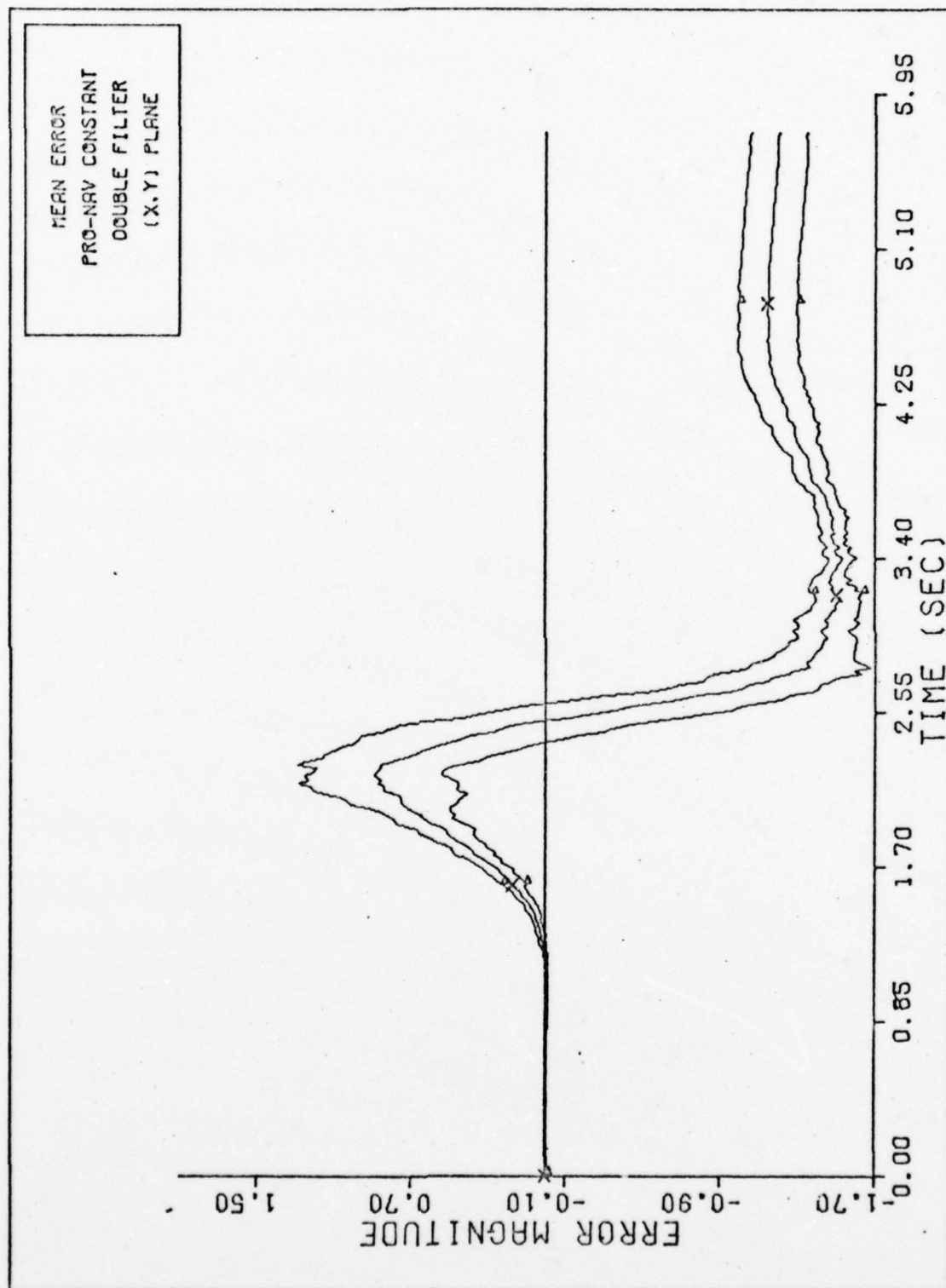


Fig. C-31 PRO-NAV CONSTANT DOUBLE FILTER

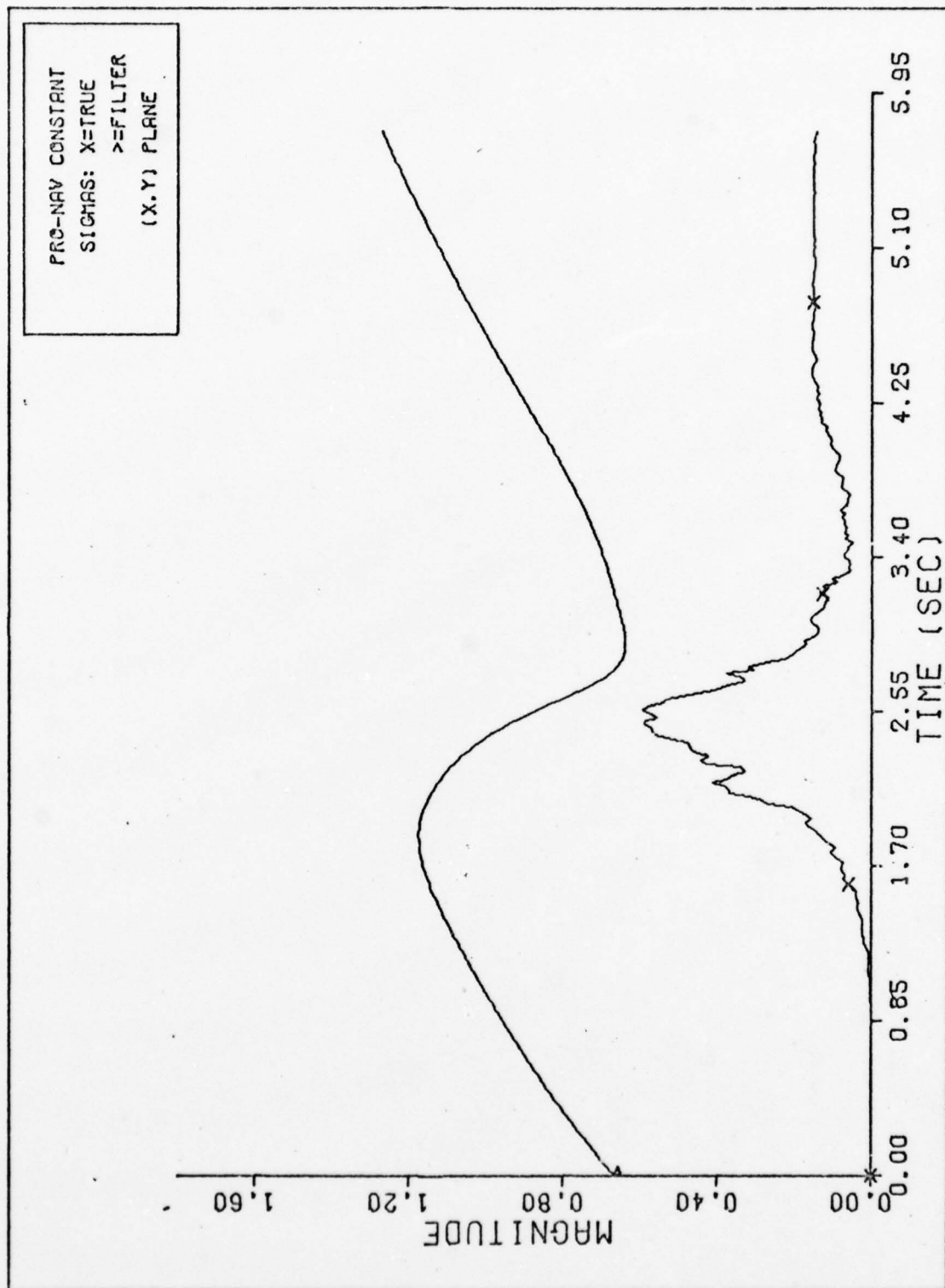


Fig. C-32 PRO-NAV CONSTANT SIGMAS DOUBLE FILTER

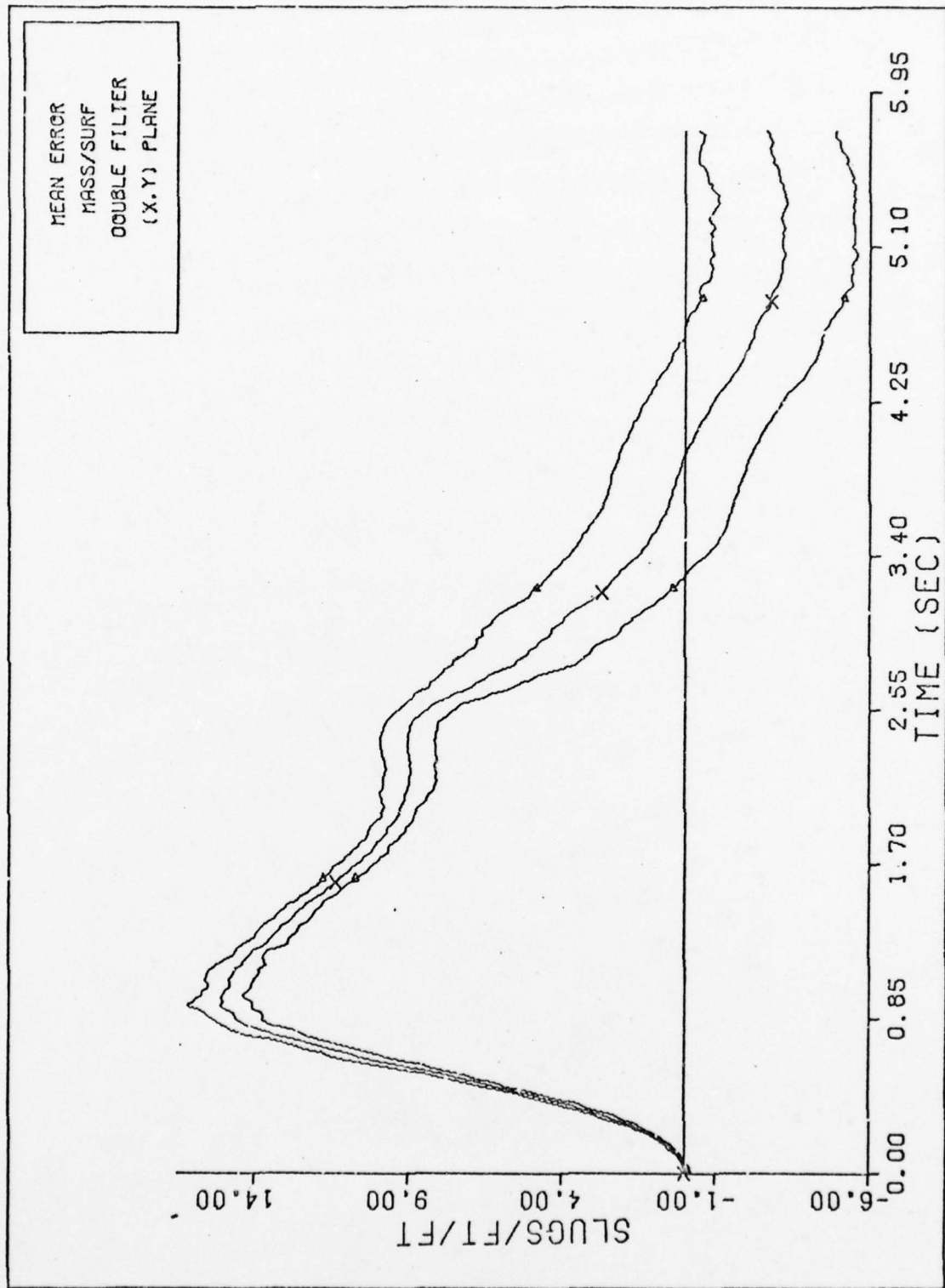


Fig. C-33

MASS/SURF DOUBLE FILTER

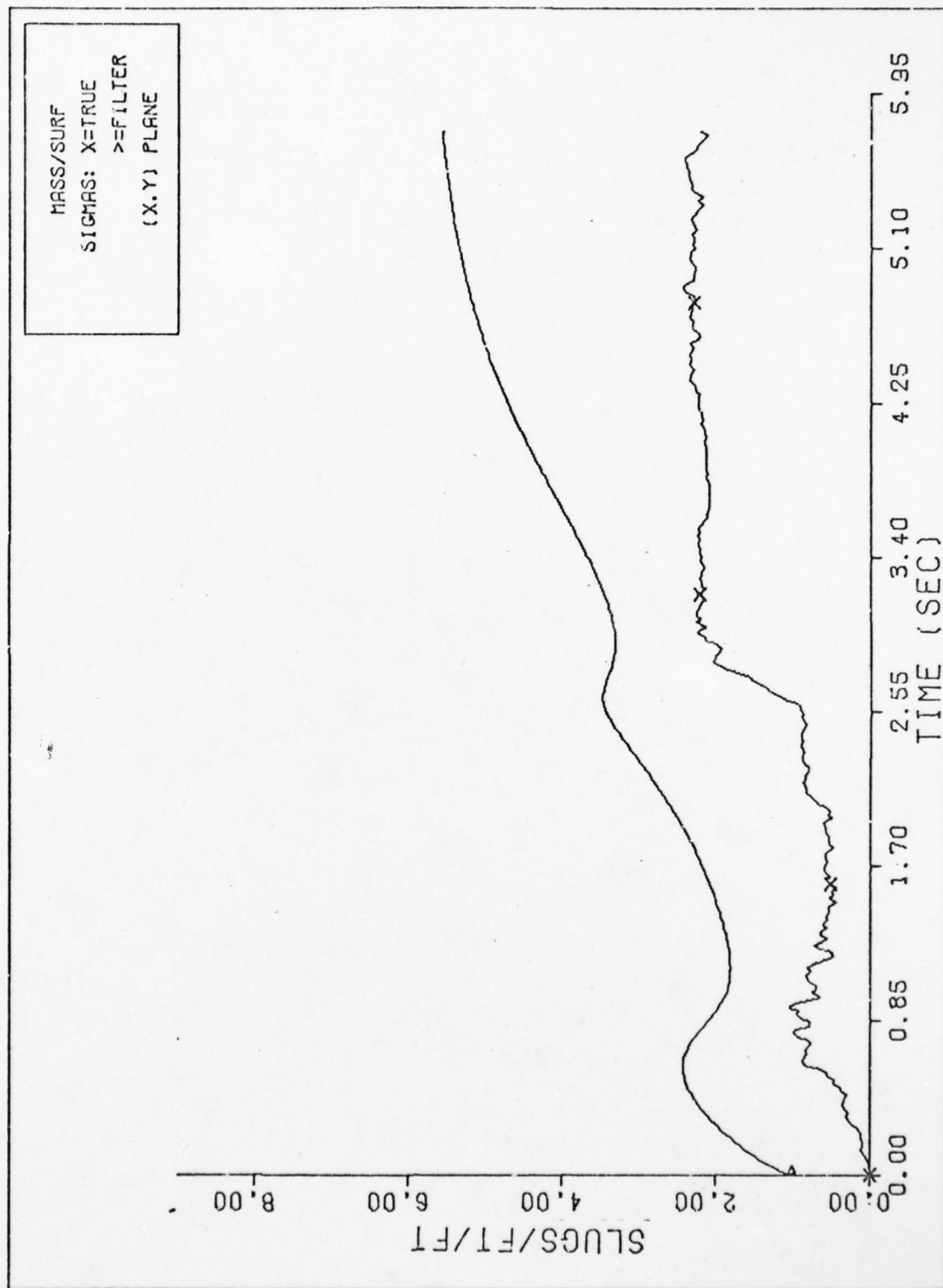


Fig. C-34

MASS/SURF SIGMAS DOUBLE FILTER

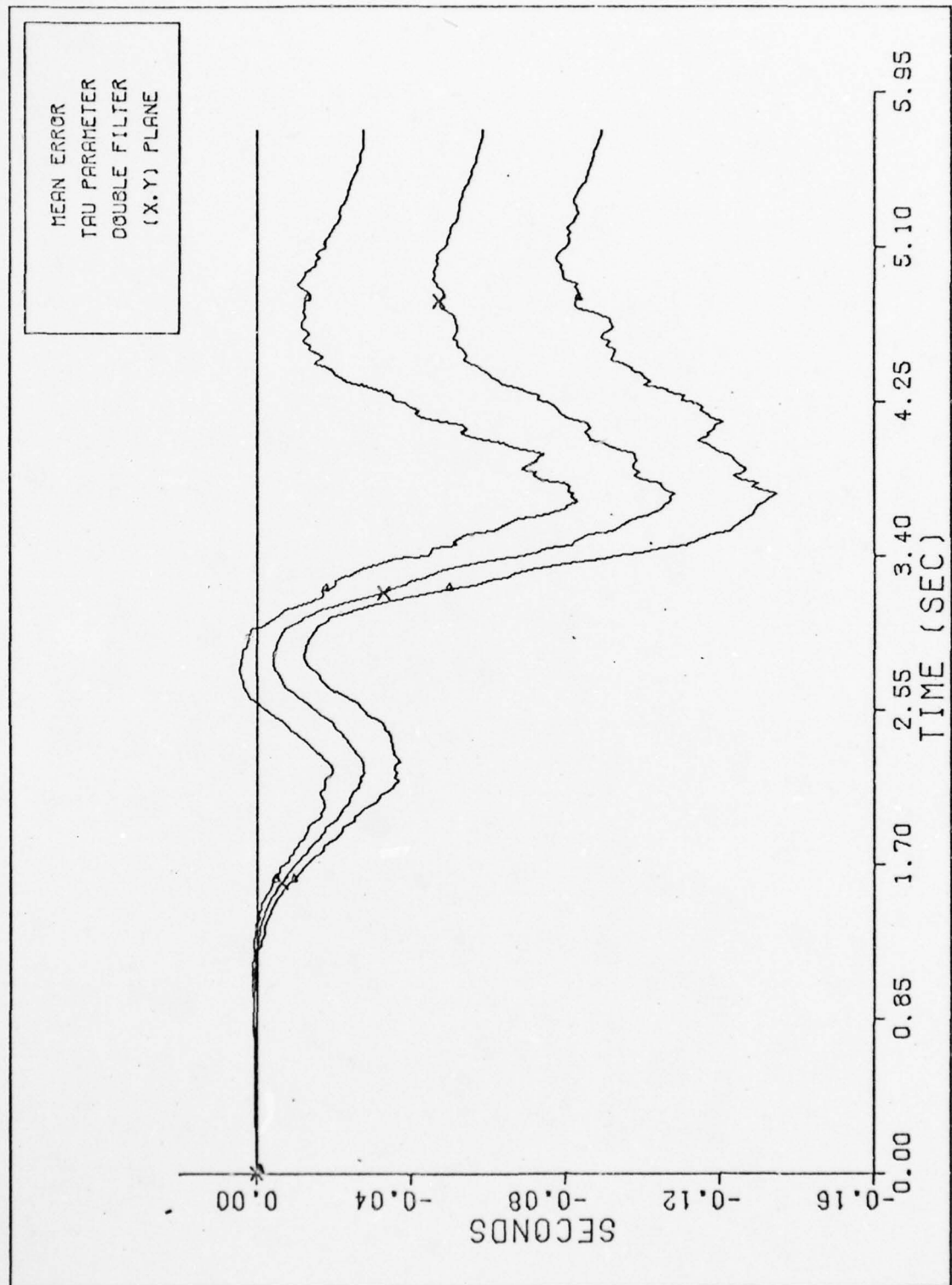


Fig. C-35

TAU PARAMETER

DOUBLE FILTER

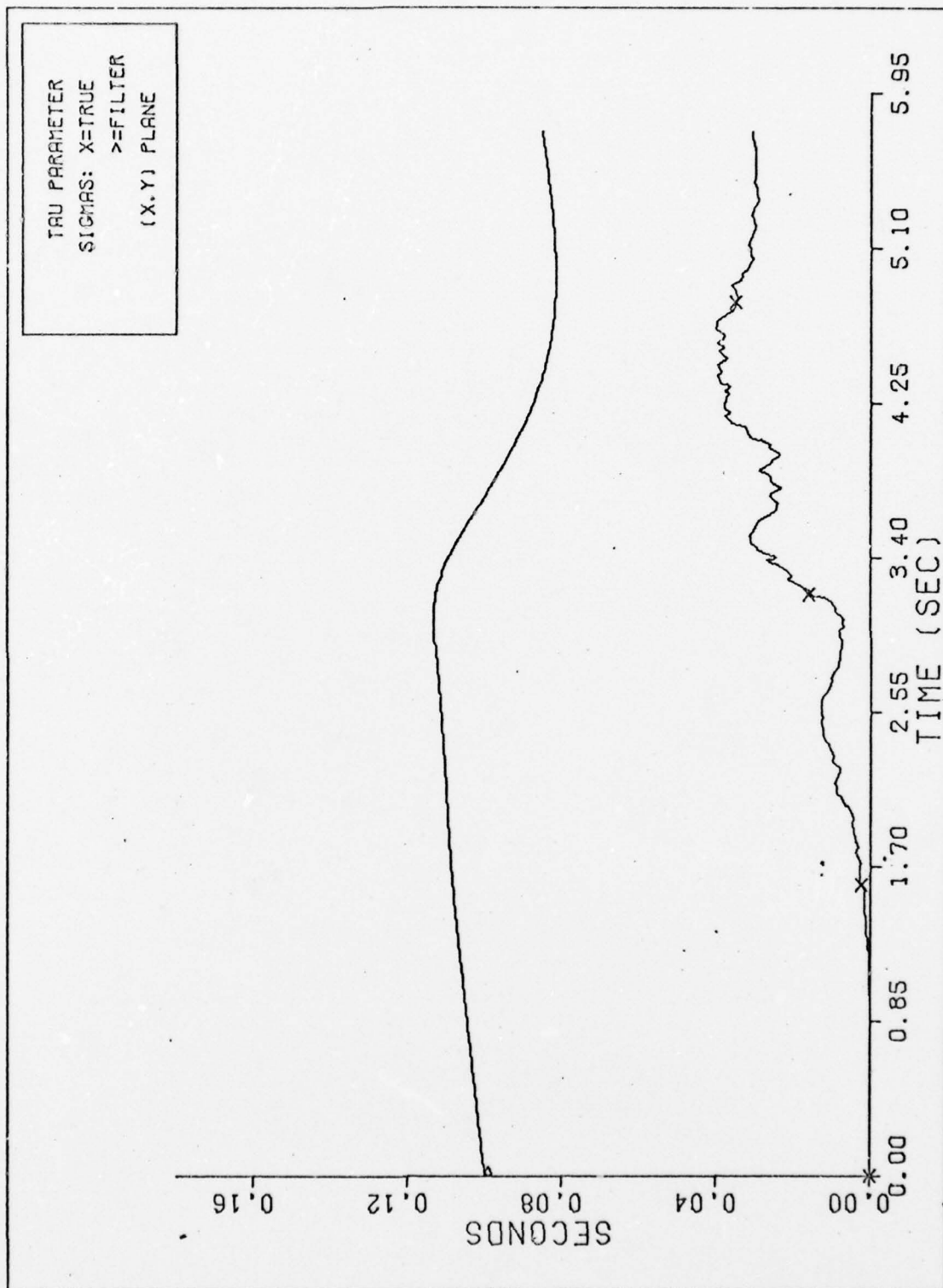


Fig. C-36

TAU PARAMETER SIGMAS DOUBLE FILTER

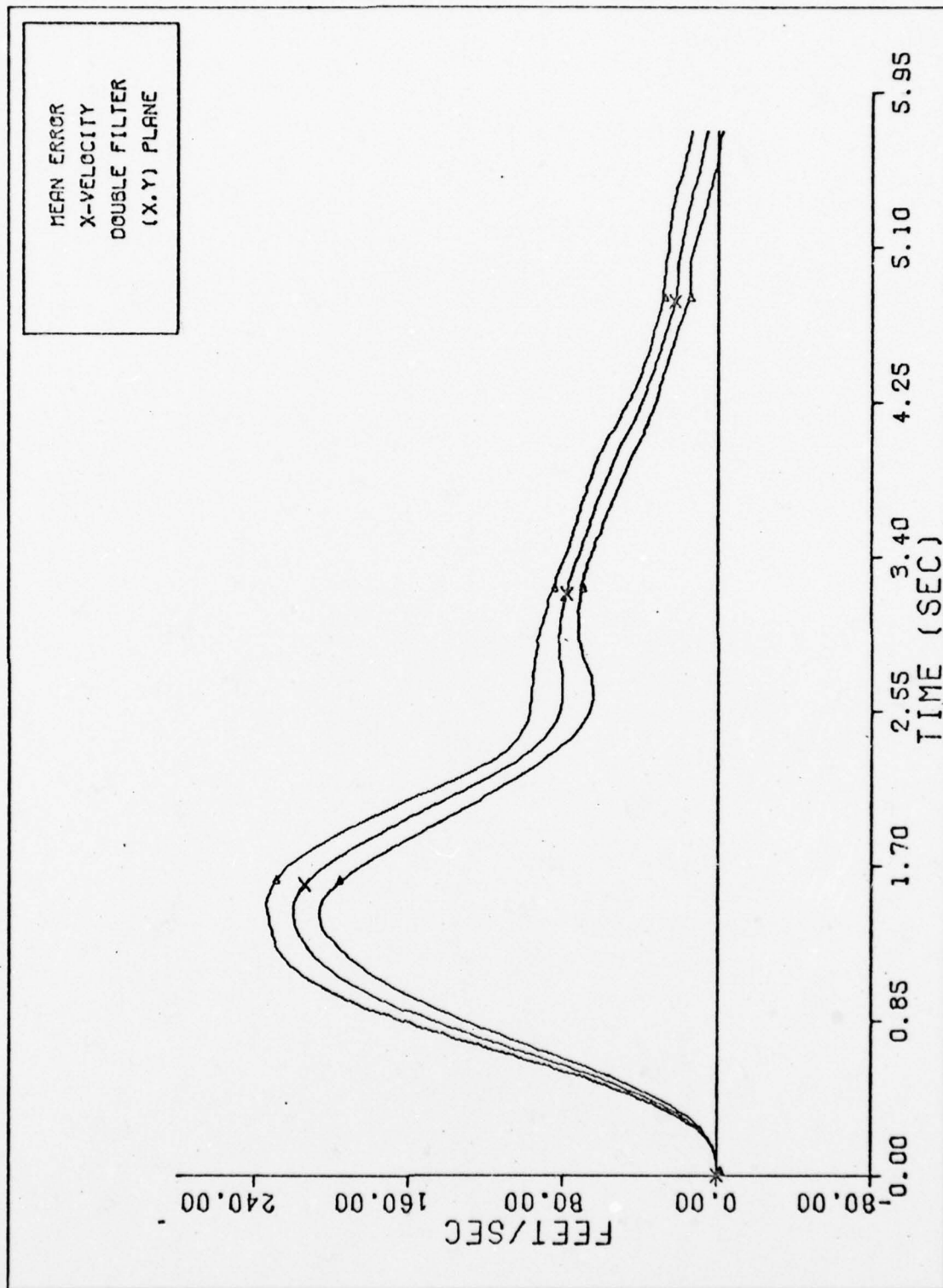


Fig. C-37

X-VELOCITY DOUBLE FILTER

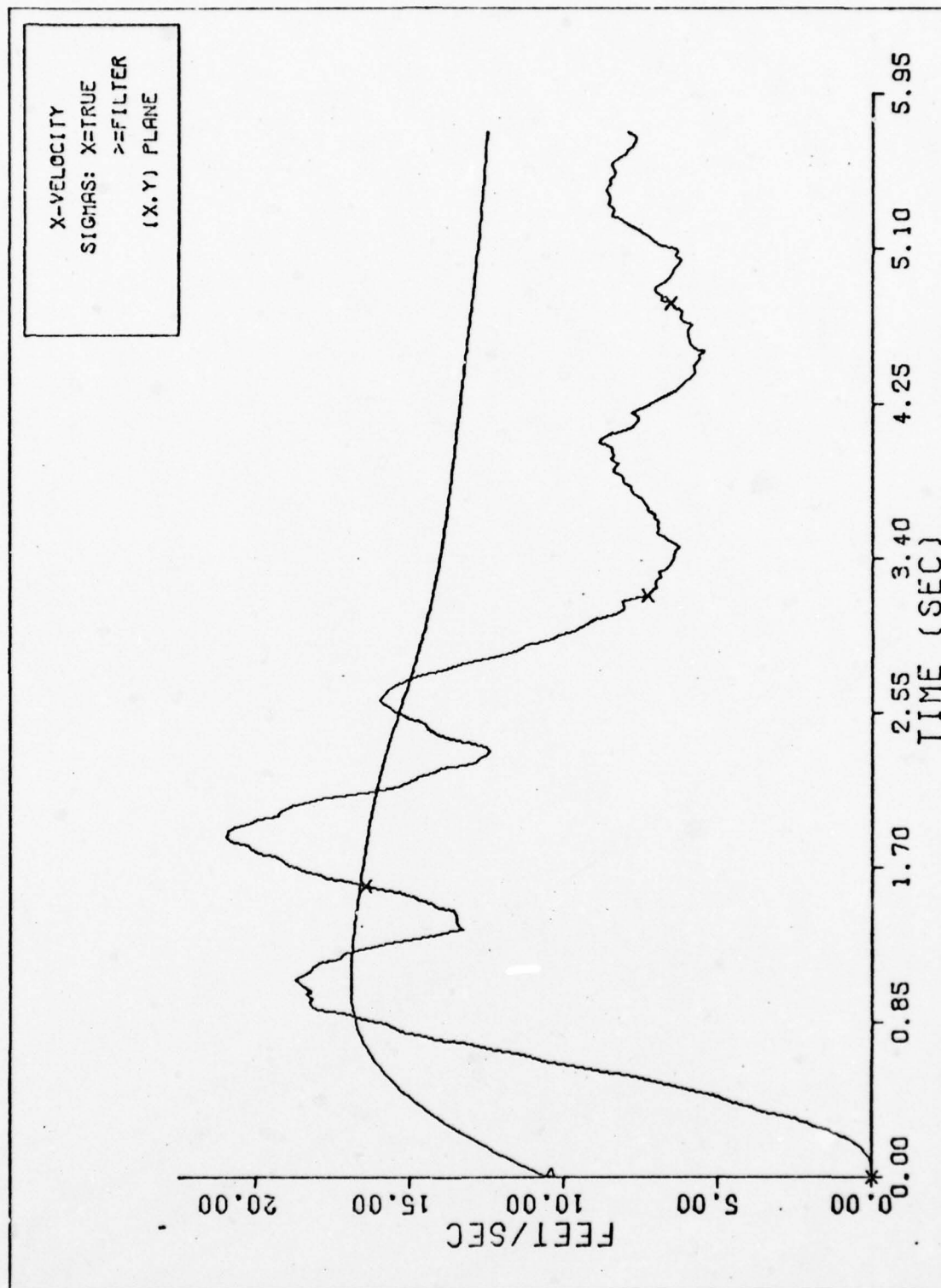


Fig. C-38

X-VELOCITY SIGMAS DOUBLE FILTER

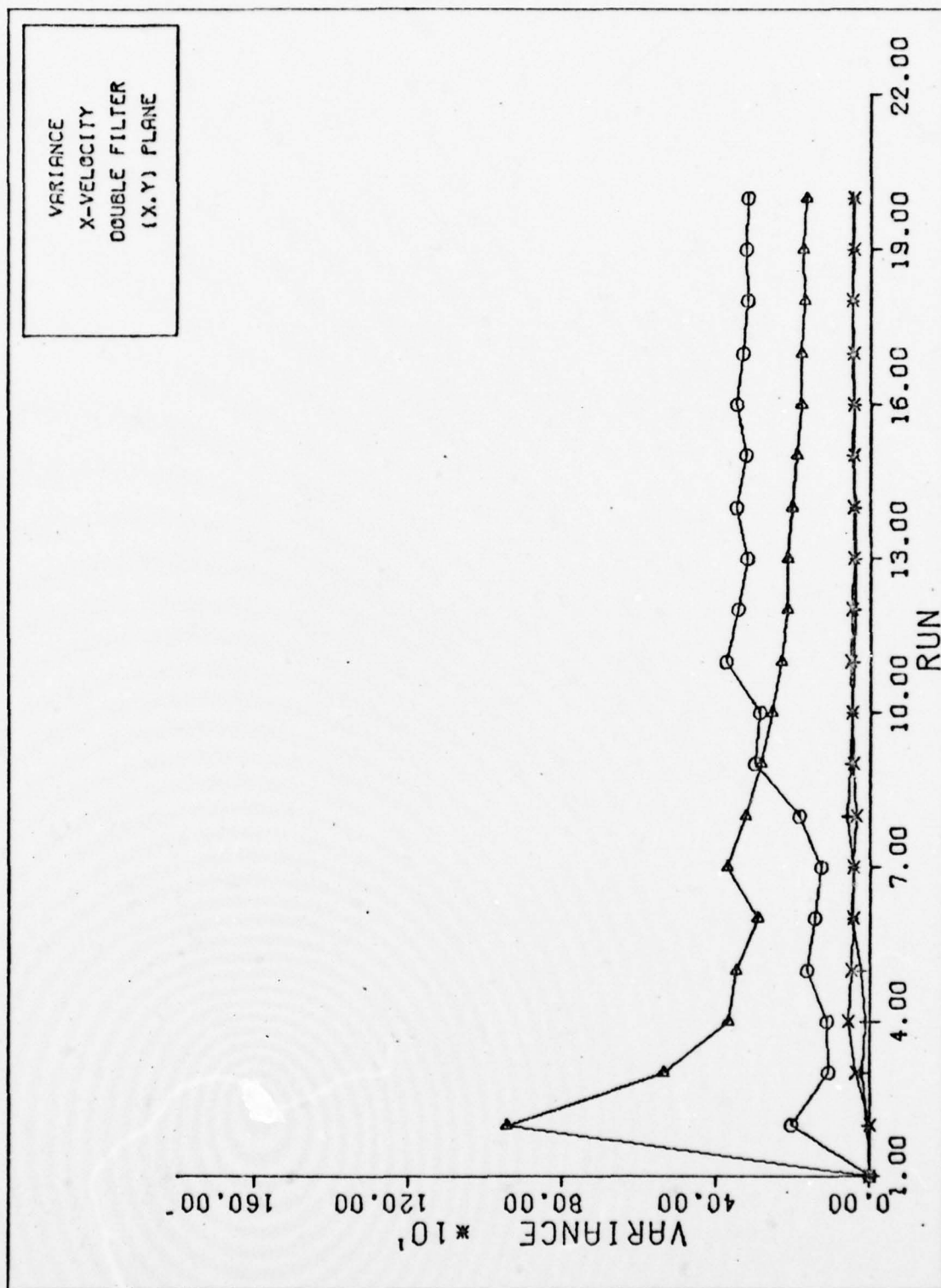


Fig. C-39

VARIANCE CONVERGENCE

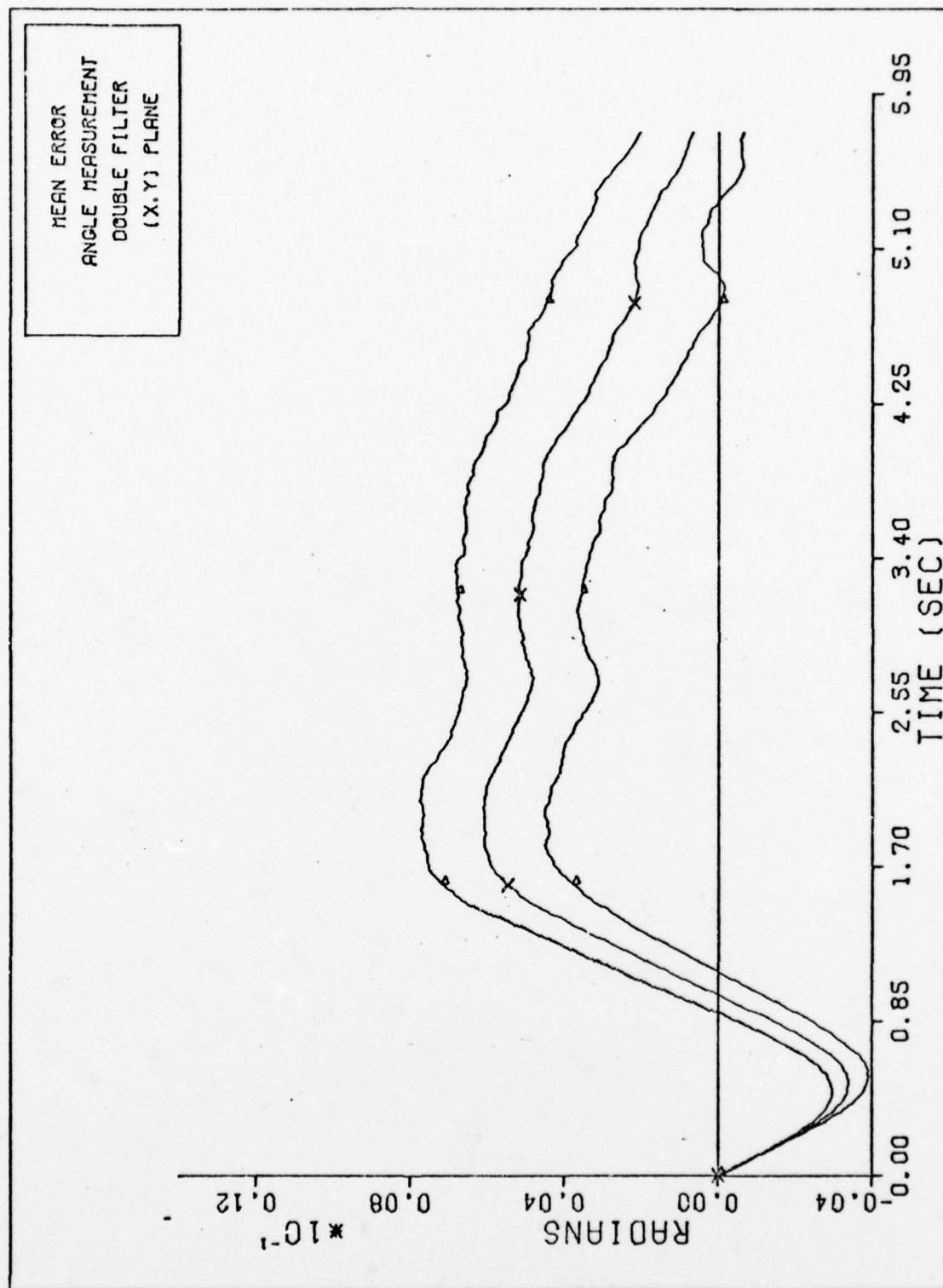


Fig. C-40

ANGLE MEASUREMENT DOUBLE FILTER

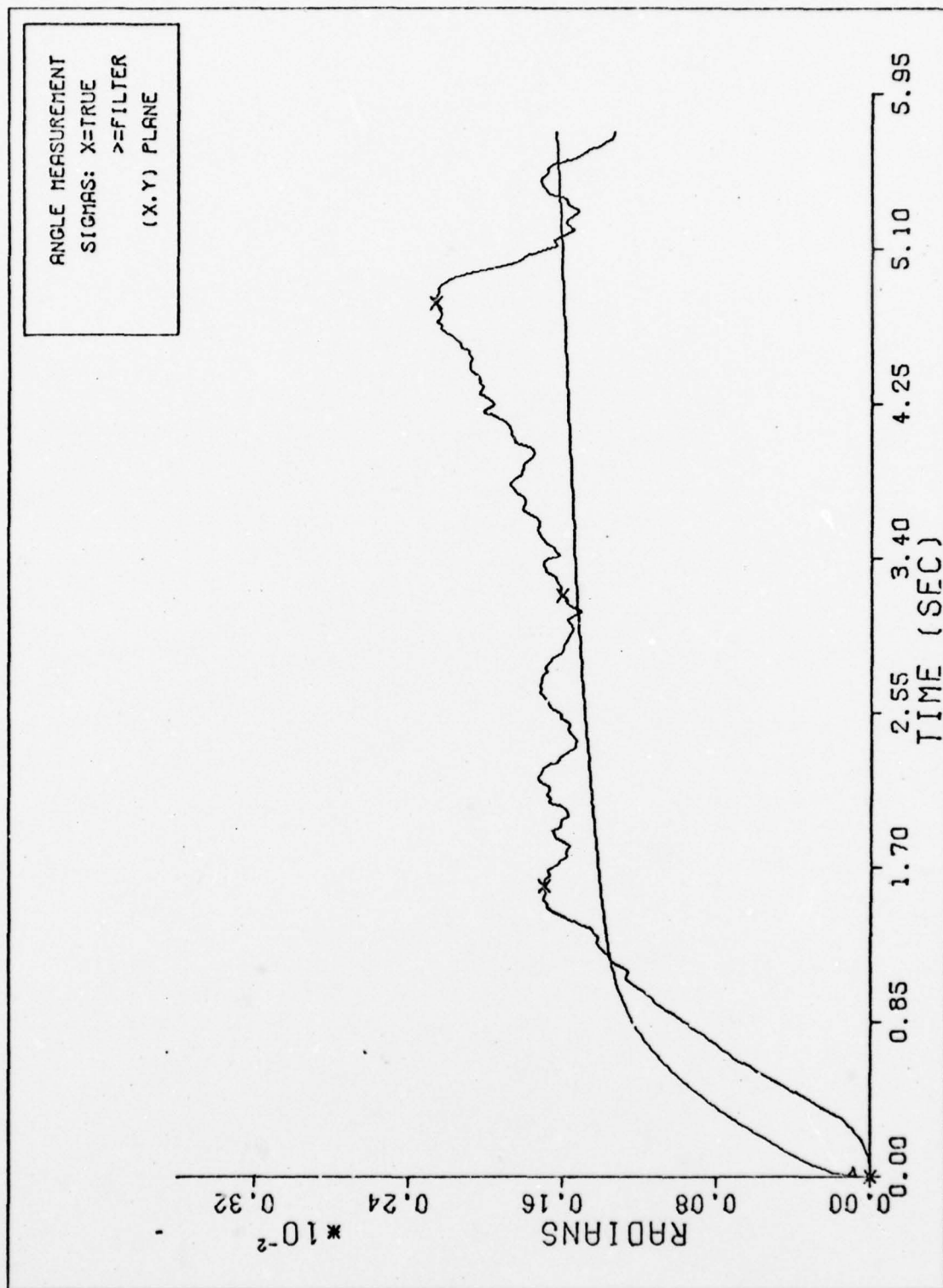


Fig. C-41 ANGLE MEASUREMENT SIGMAS DOUBLE FILTER

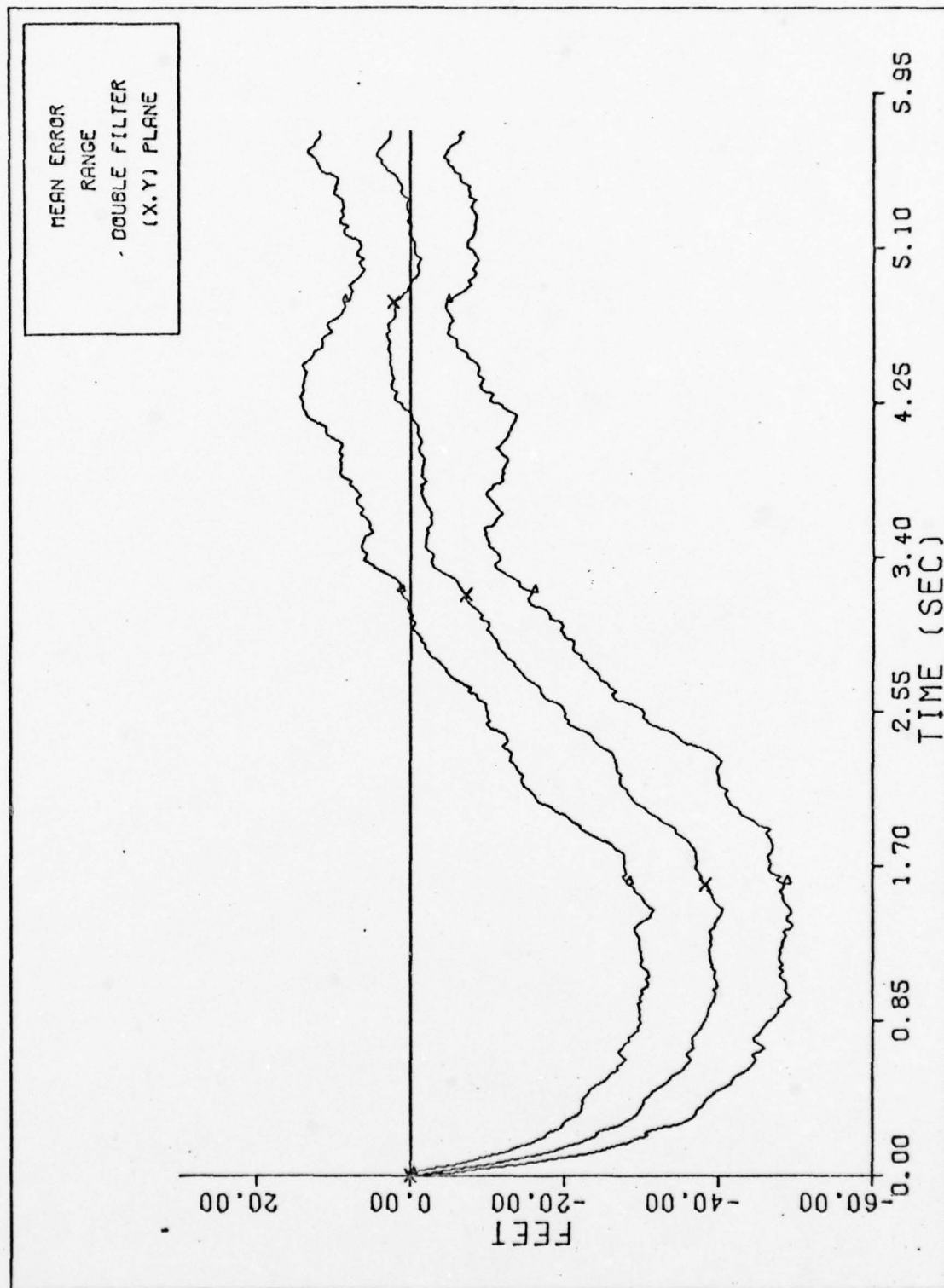


Fig. C-42

RANGE DOUBLE FILTER

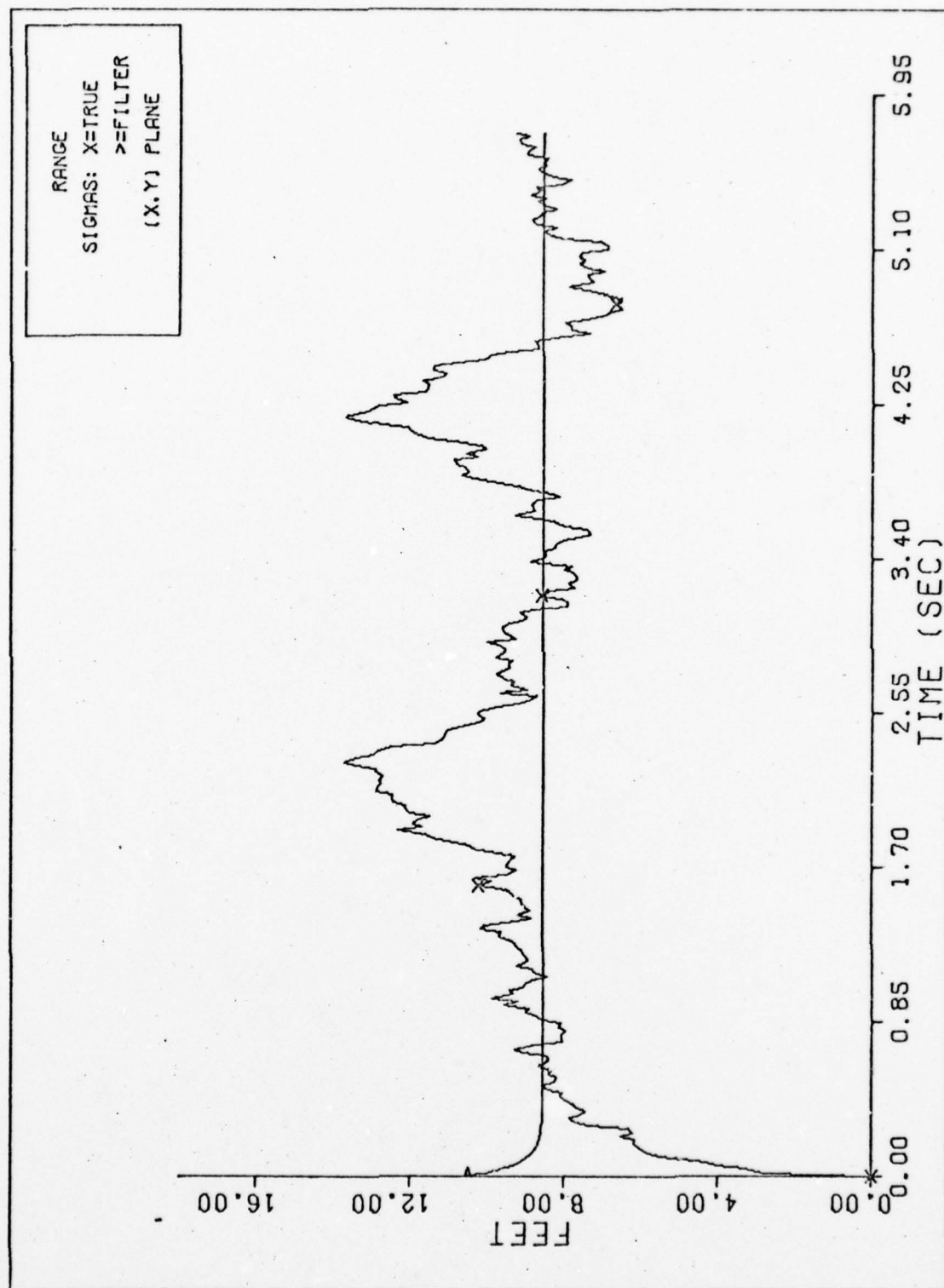


Fig. C-43

RANGE SIGMAS DOUBLE FILTER

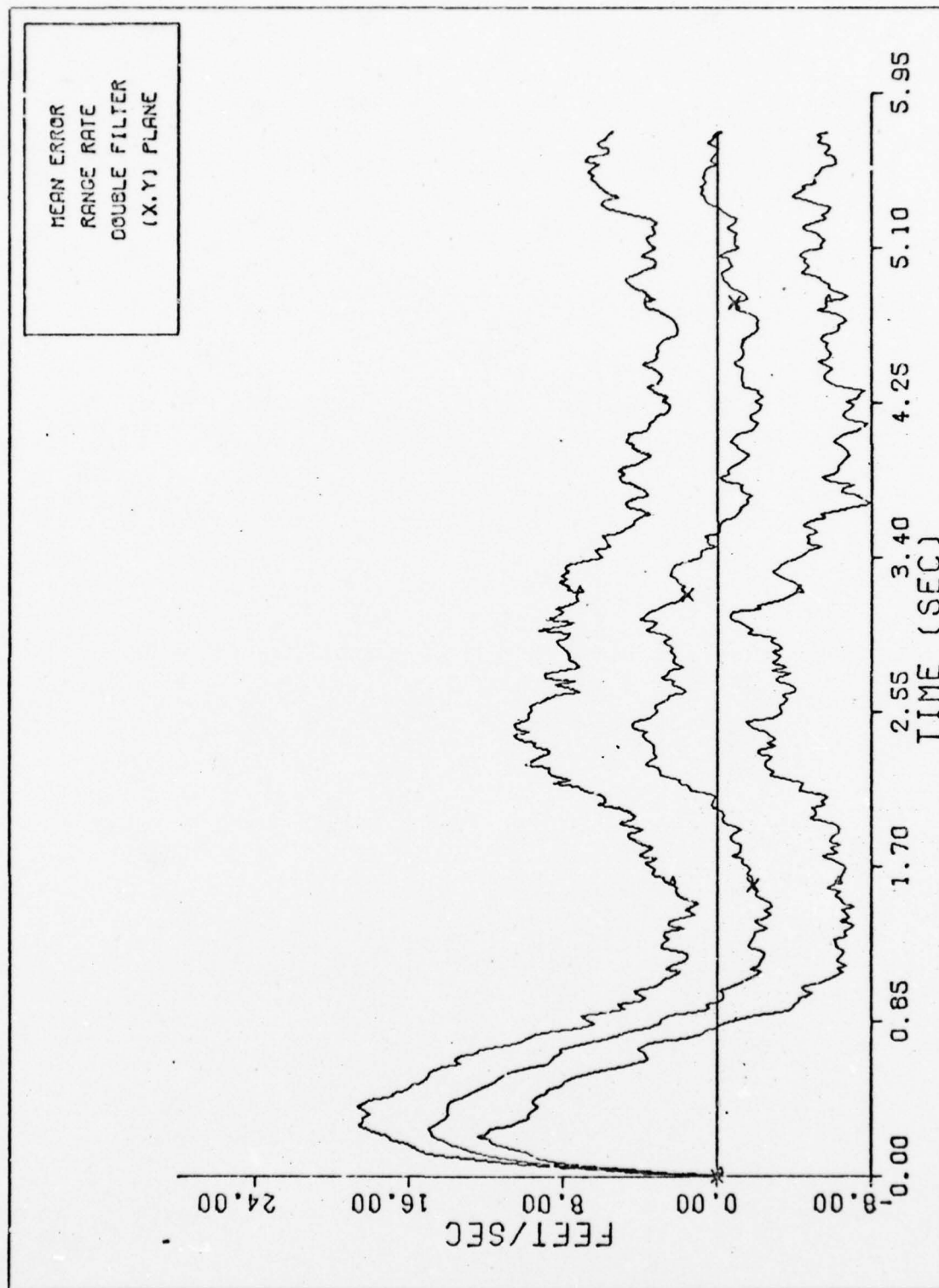


Fig. C-44

RANGE RATE DOUBLE FILTER

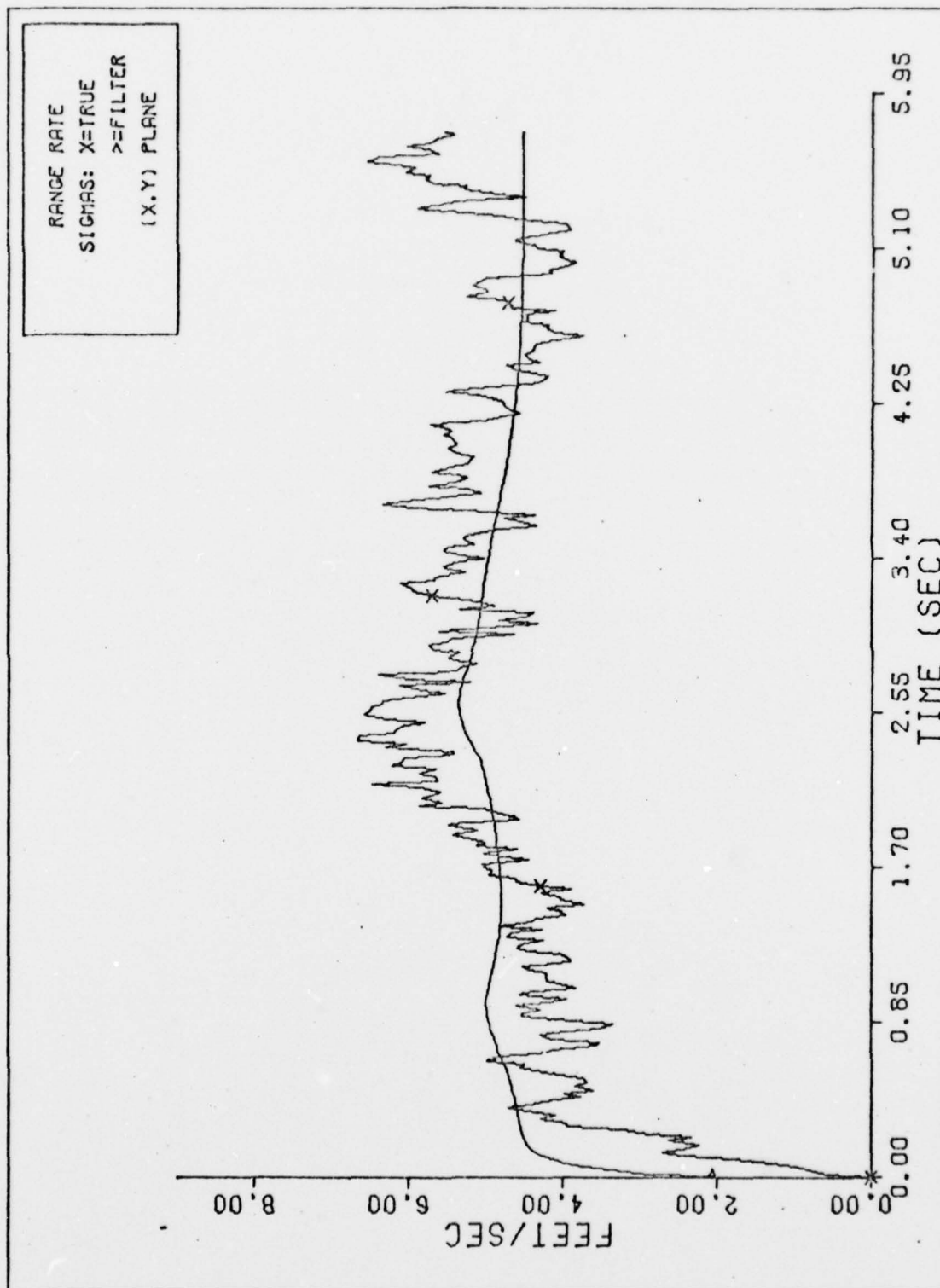


Fig. C-45

RANGE RATE SIGMAS DOUBLE FILTER

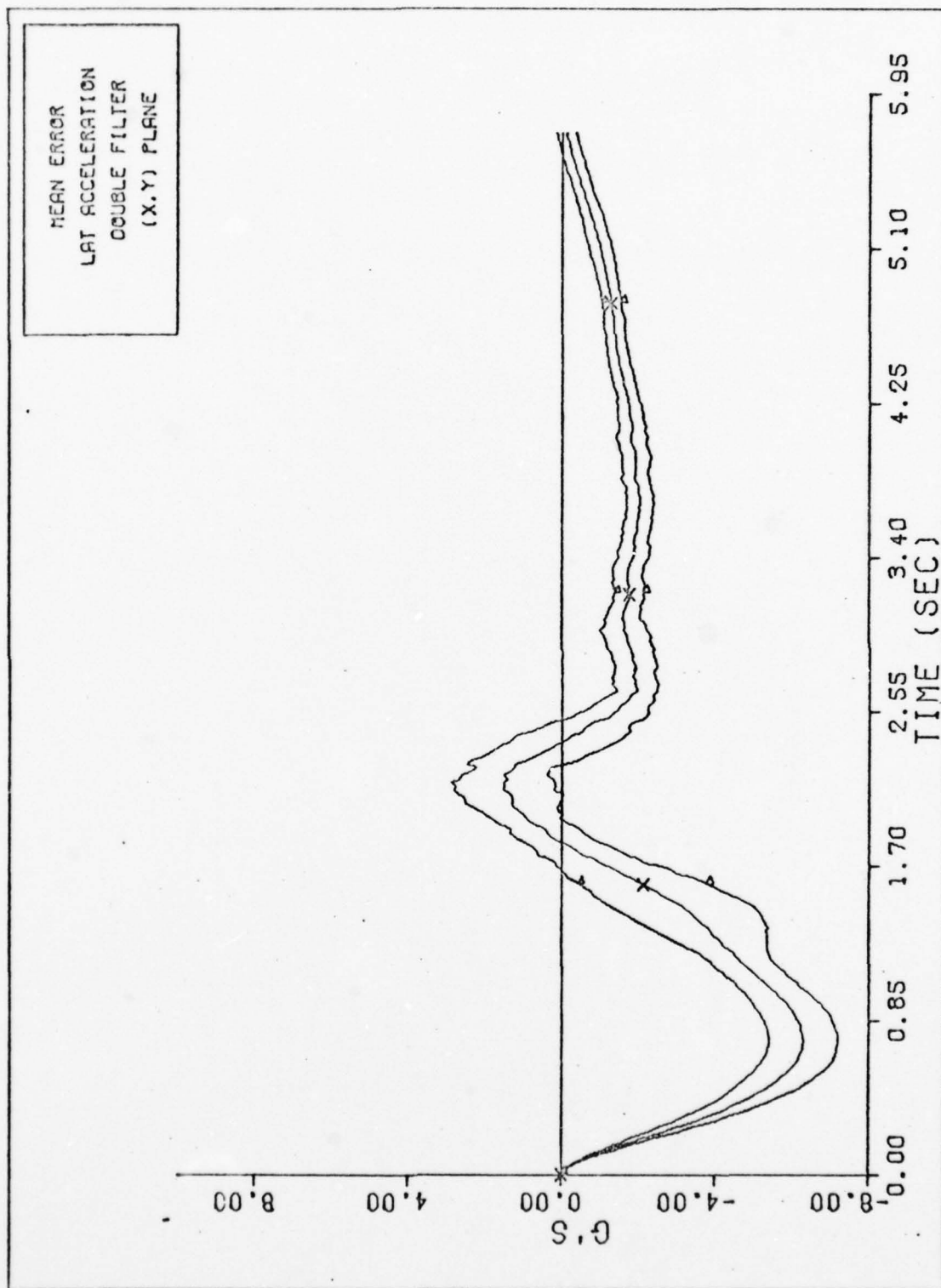


Fig. C-46 LAT ACCELERATION DOUBLE FILTER

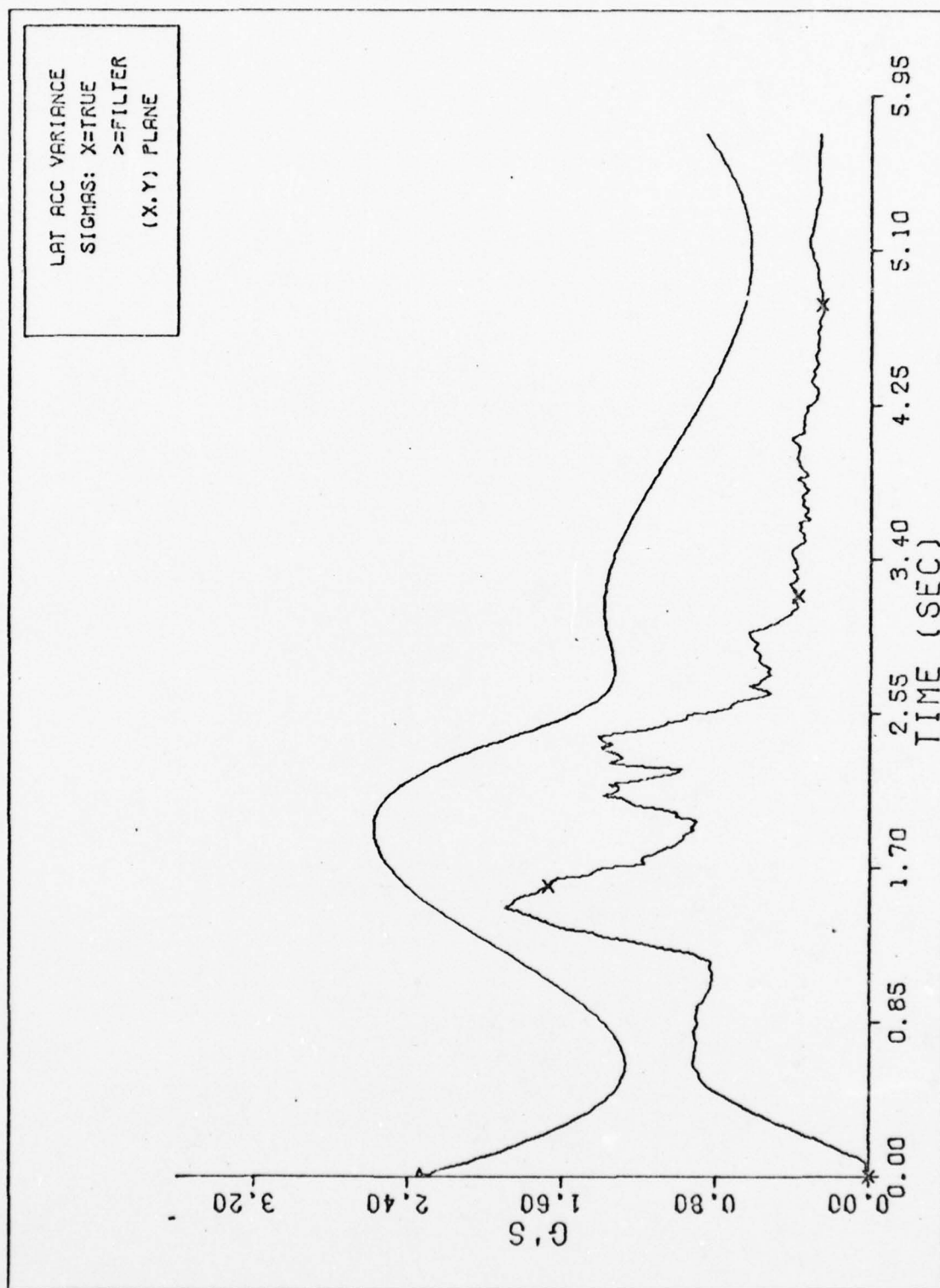


Fig. C-47 LAT ACCELERATION SIGMAS DOUBLE FILTER

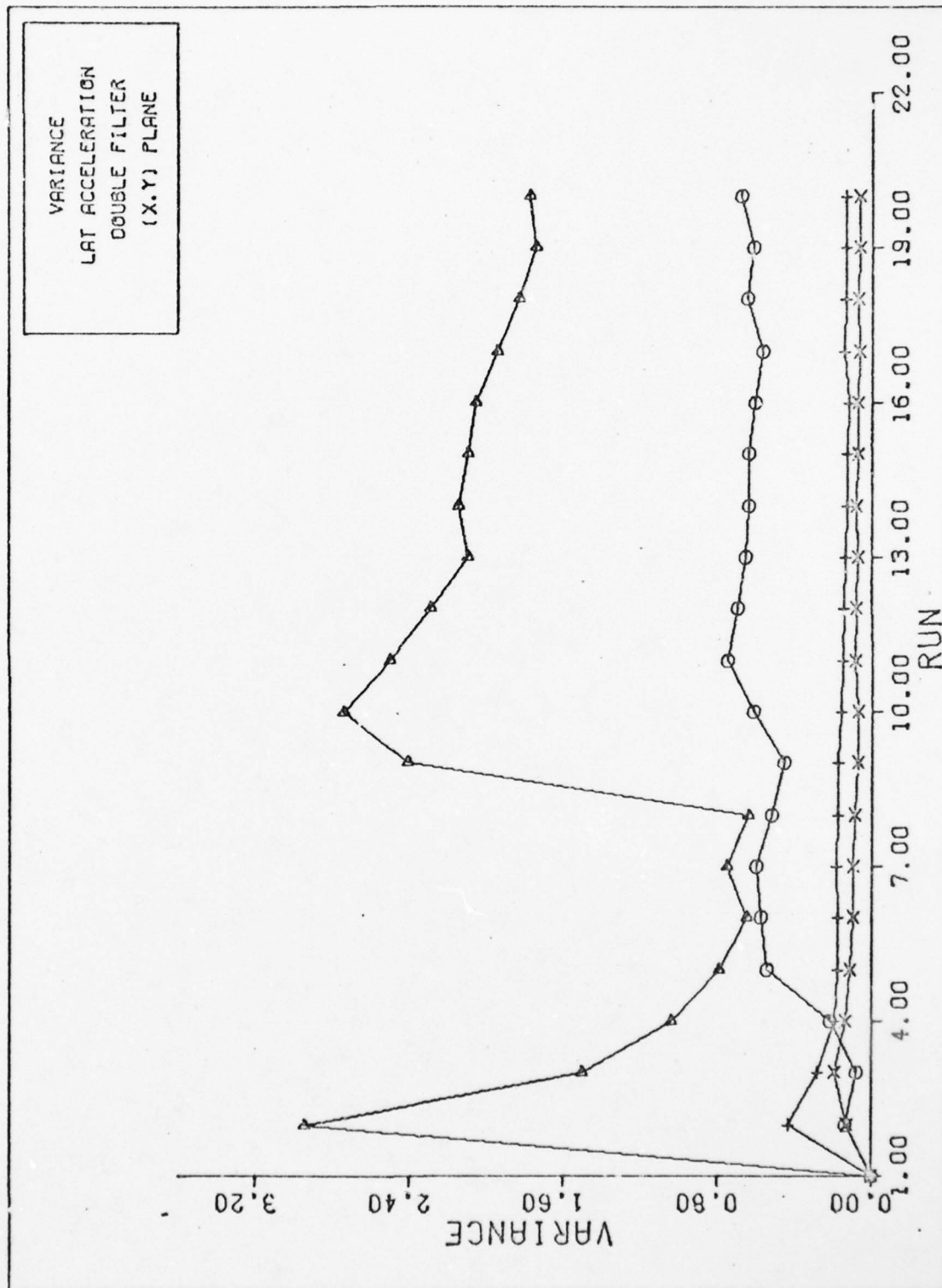


Fig. C-48

VARIANCE CONVERGENCE

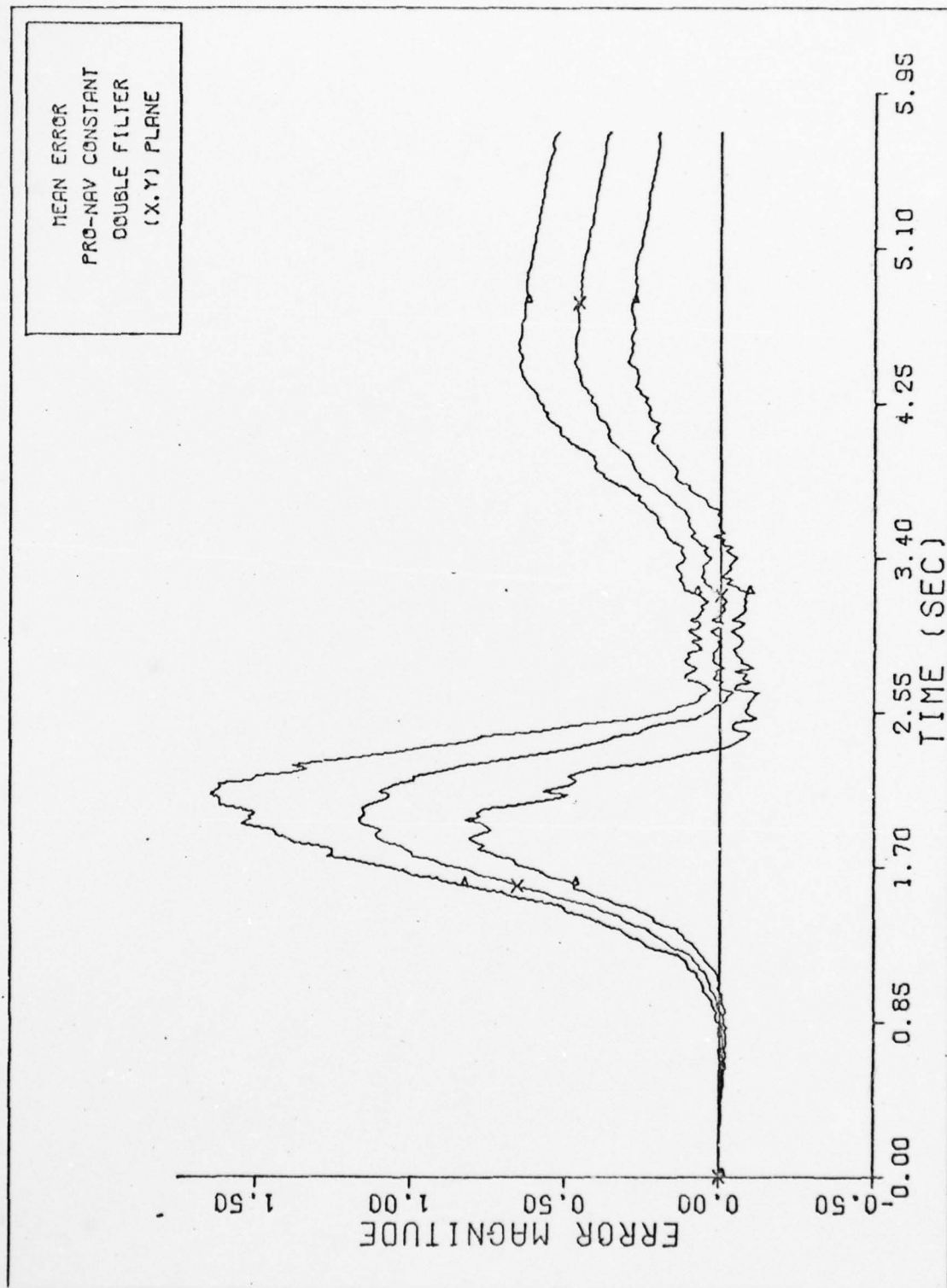


Fig. C-49

PRO-NAV CONSTANT DOUBLE FILTER

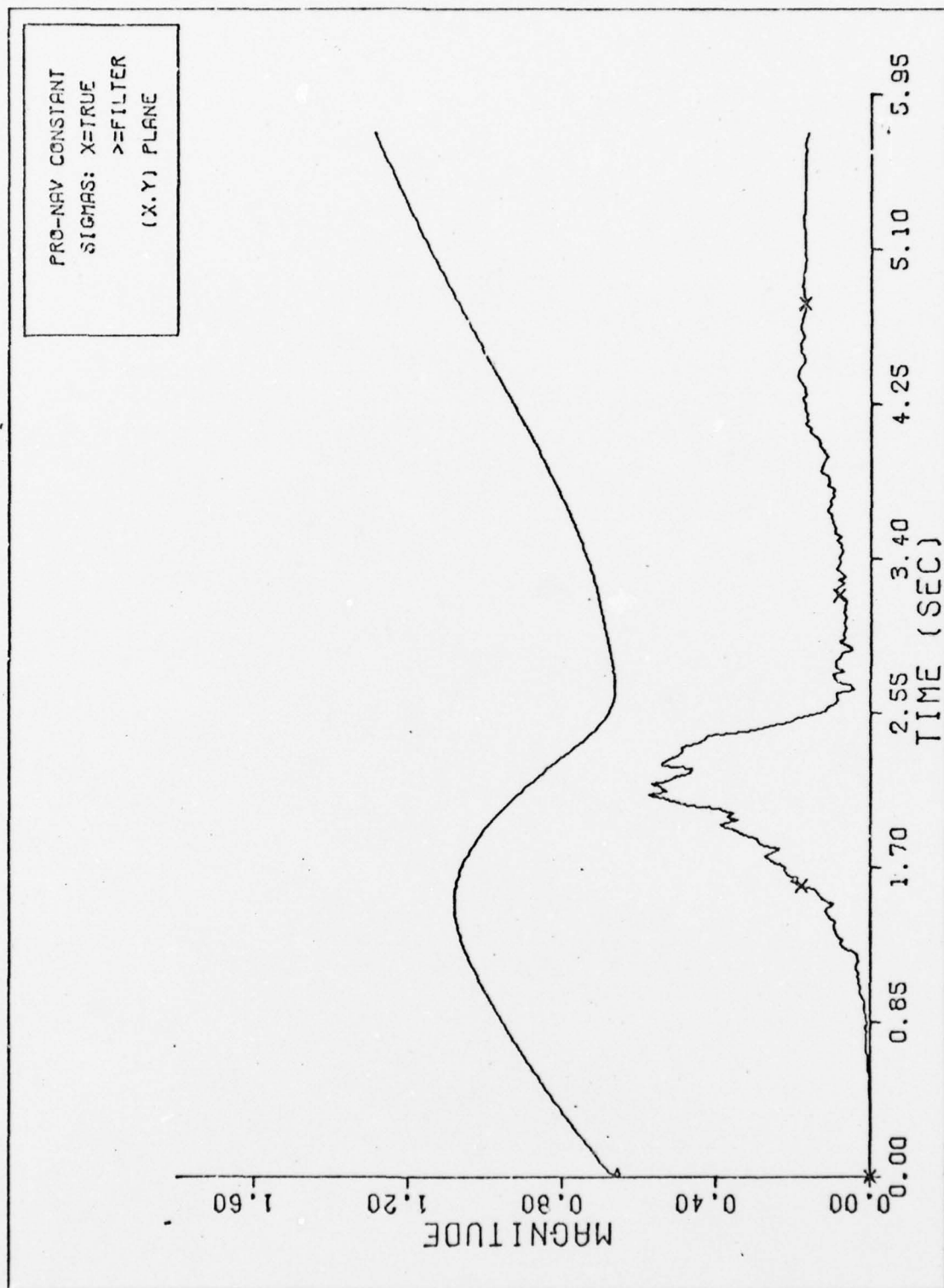


Fig. C-50 PRO-NAV CONSTANT SIGMAS DOUBLE FILTER

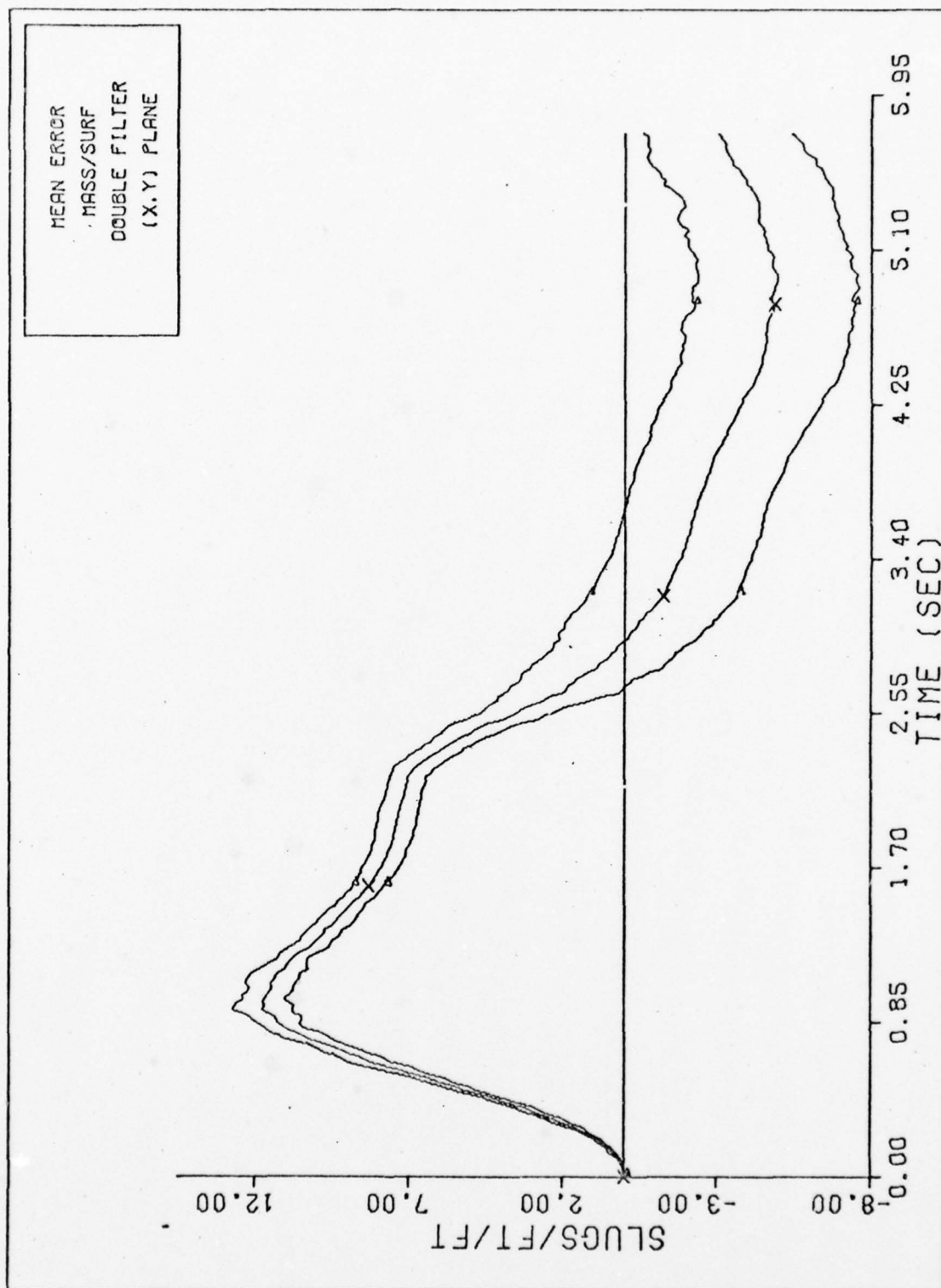


Fig. C-51

MASS/SURF DOUBLE FILTER

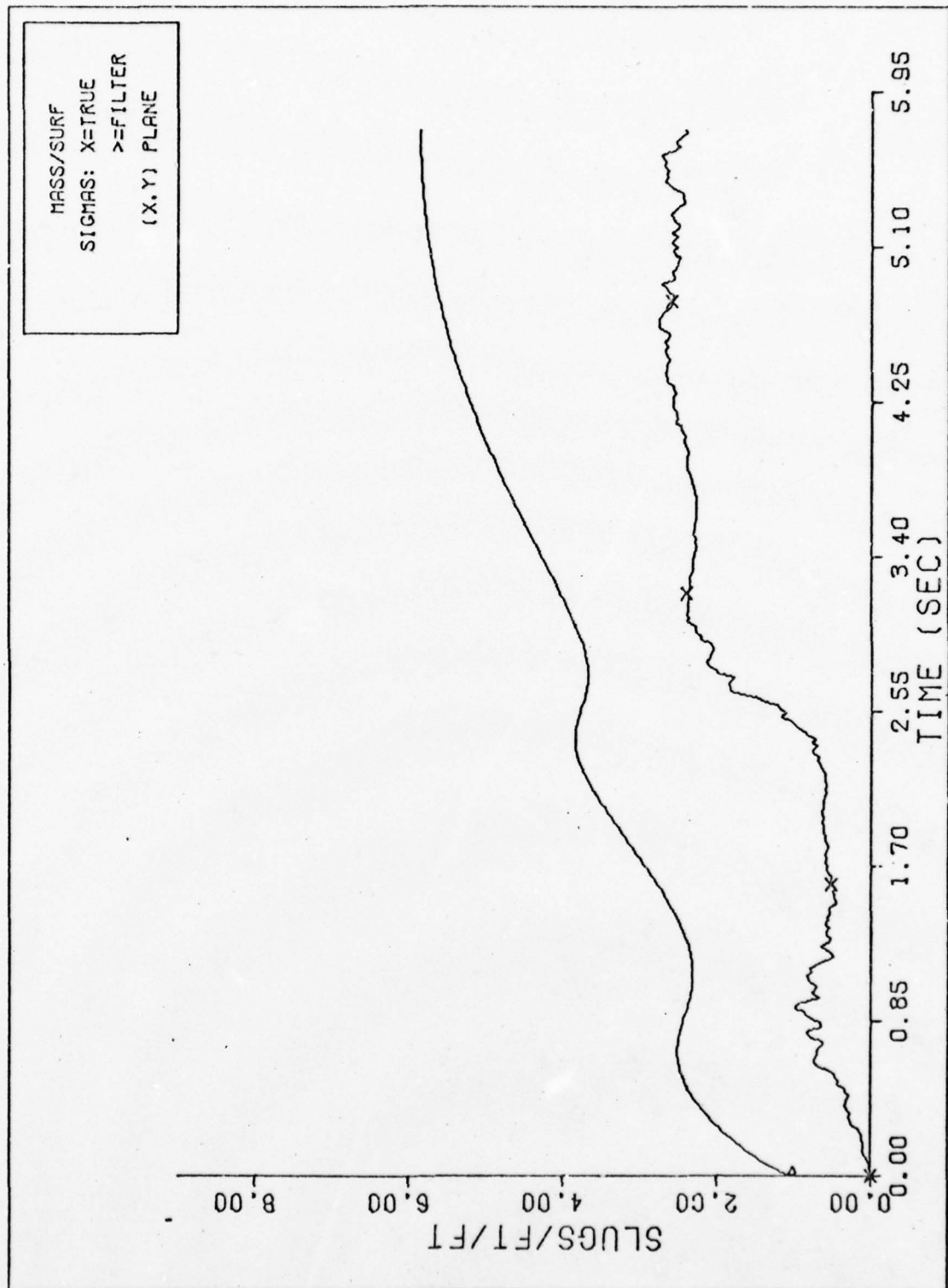


Fig. C-52

MASS/SURF SIGMAS DOUBLE FILTER

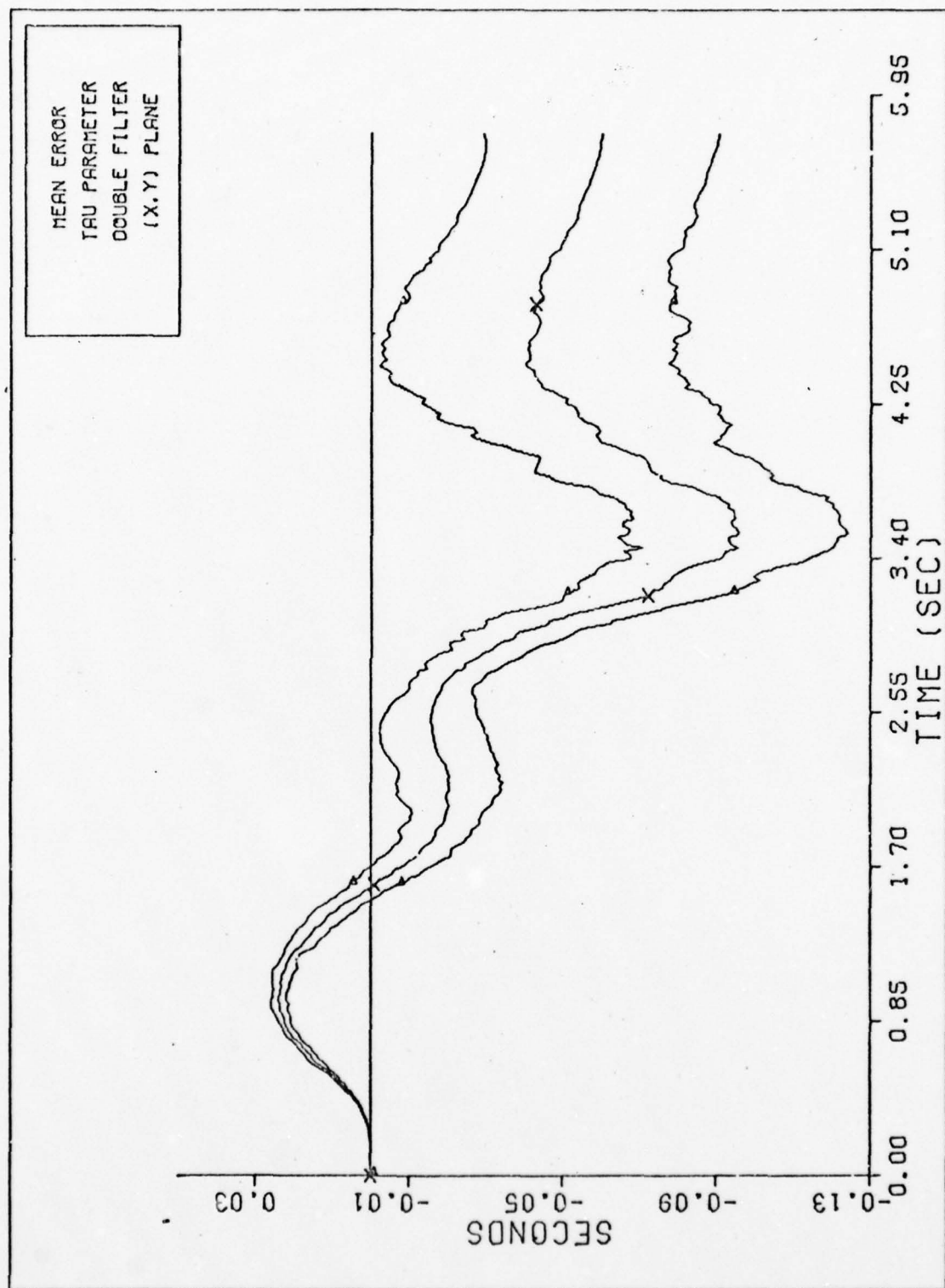


Fig. C-53

TAU PARAMETER DOUBLE FILTER

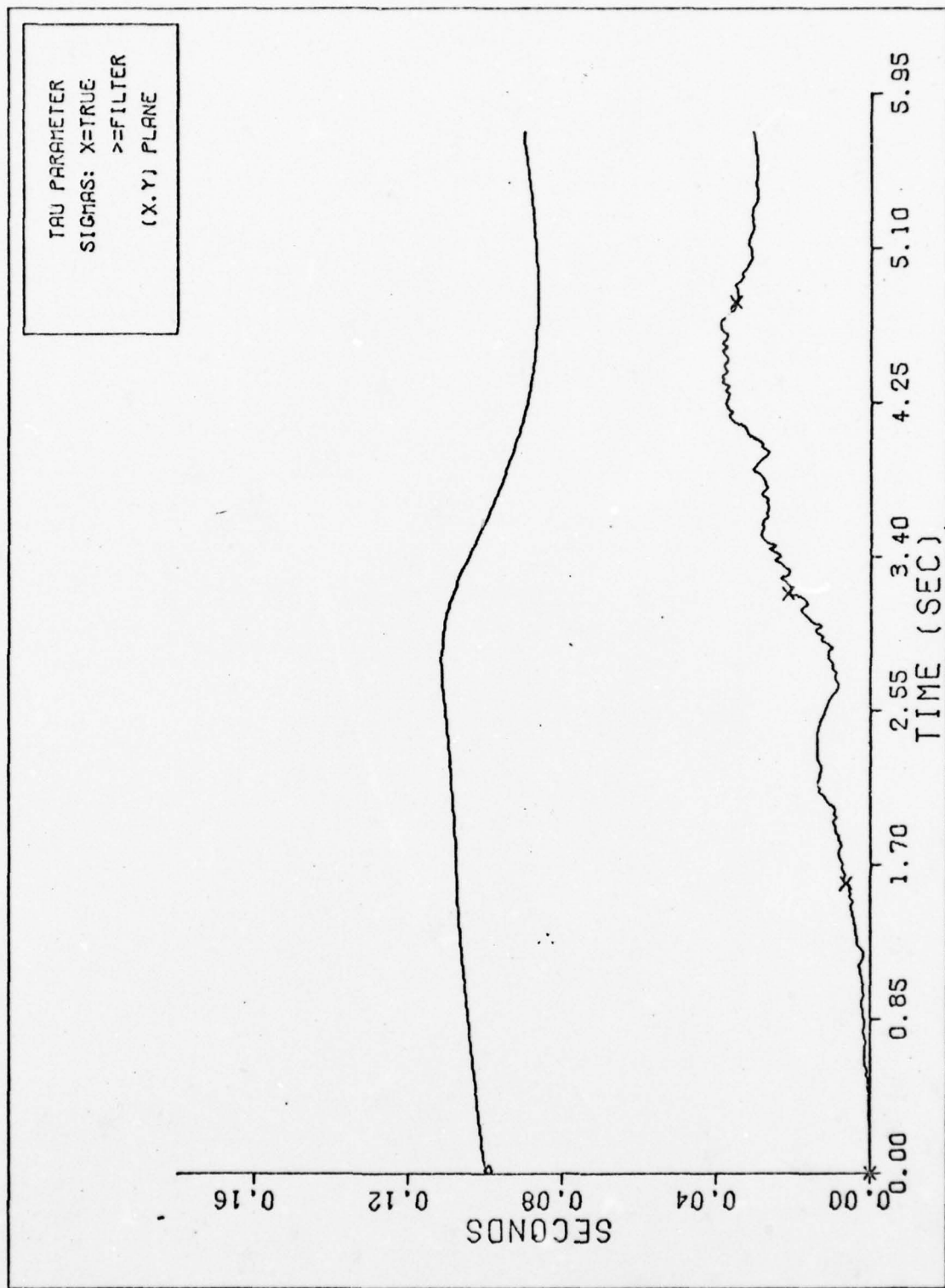


Fig. C-54

TAU PARAMETER SIGMAS DOUBLE FILTER

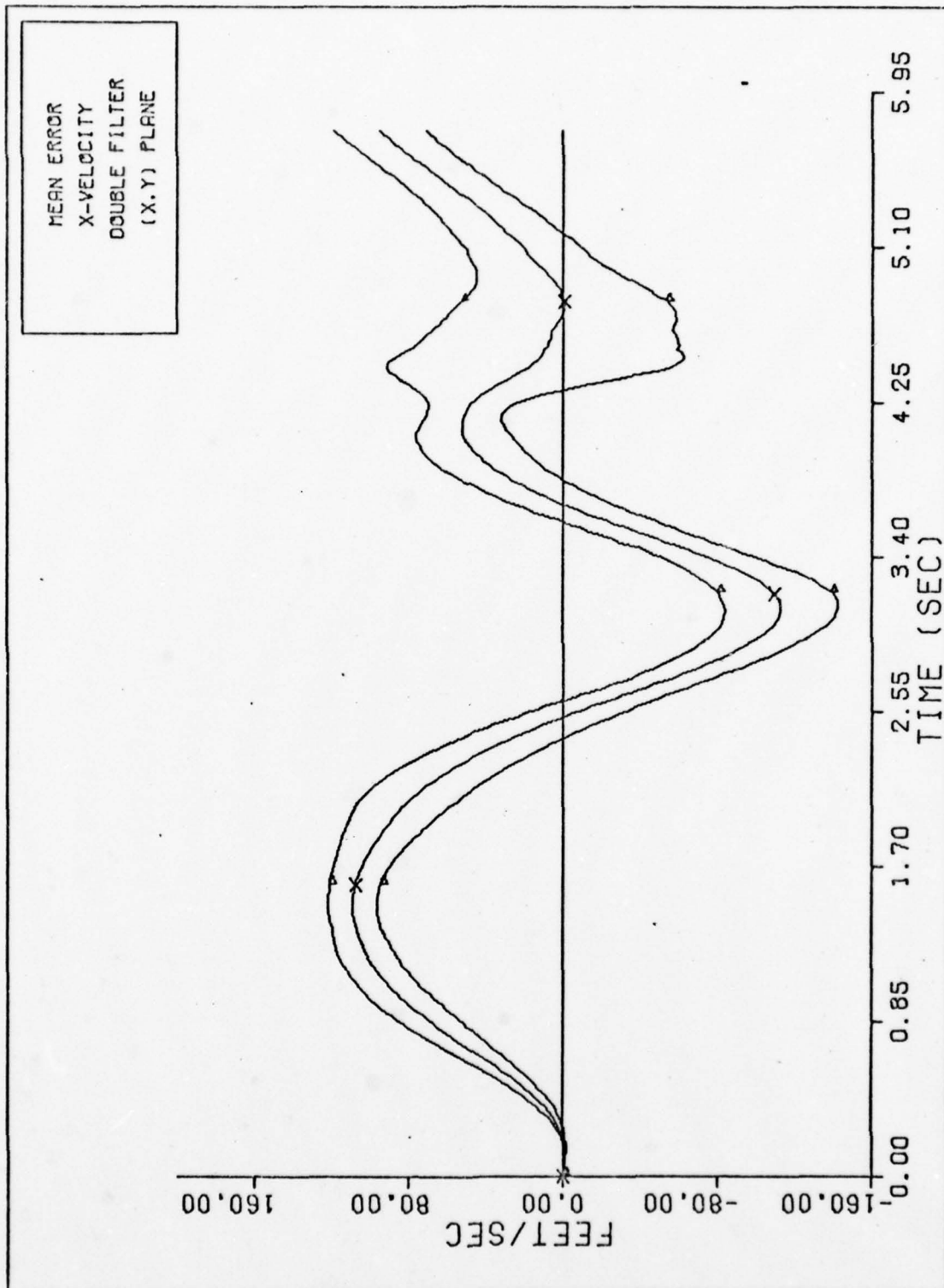


Fig. C-55

X-VELOCITY DOUBLE FILTER

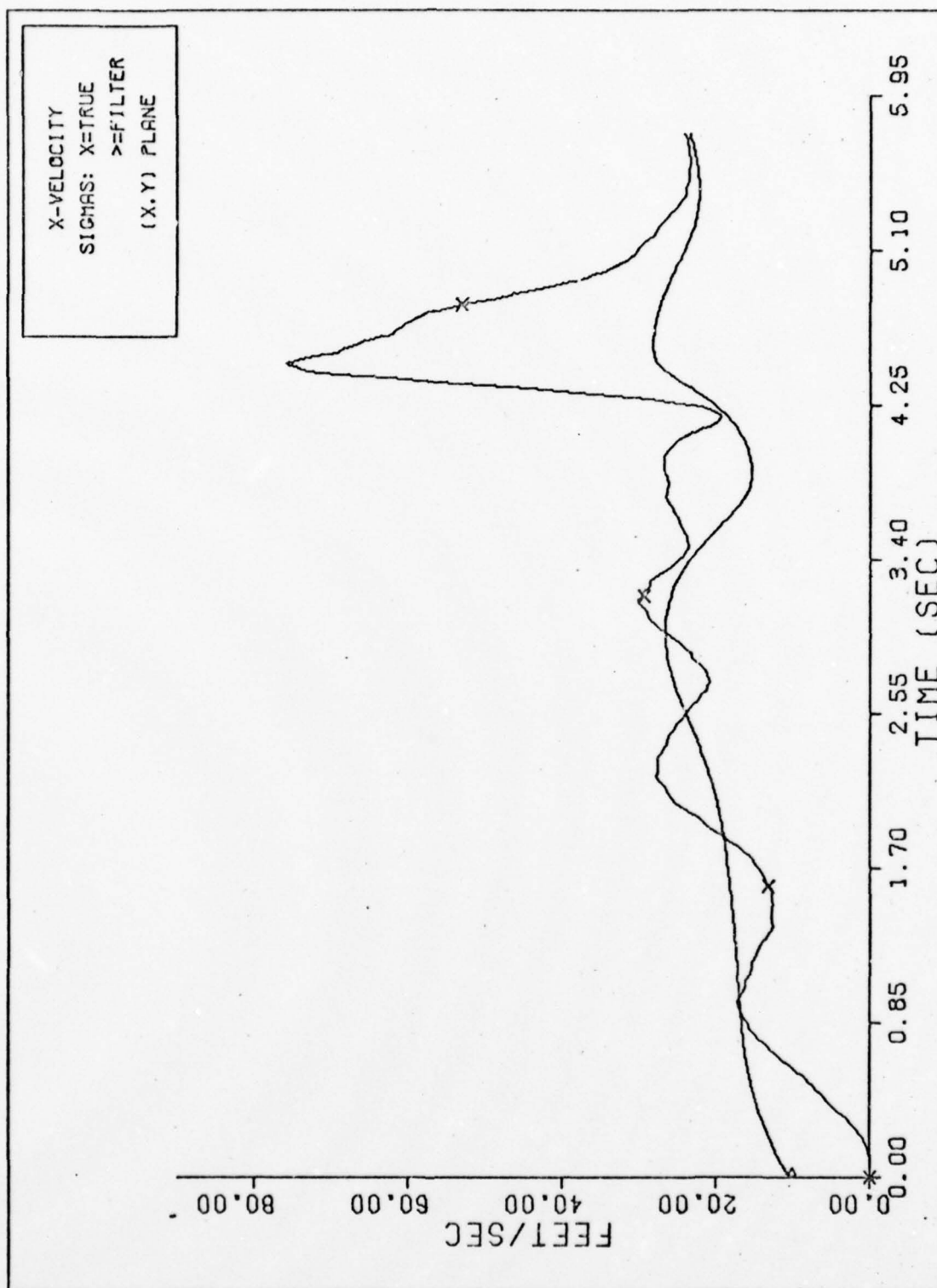


Fig. C-56

X-VELOCITY SIGMAS DOUBLE FILTER

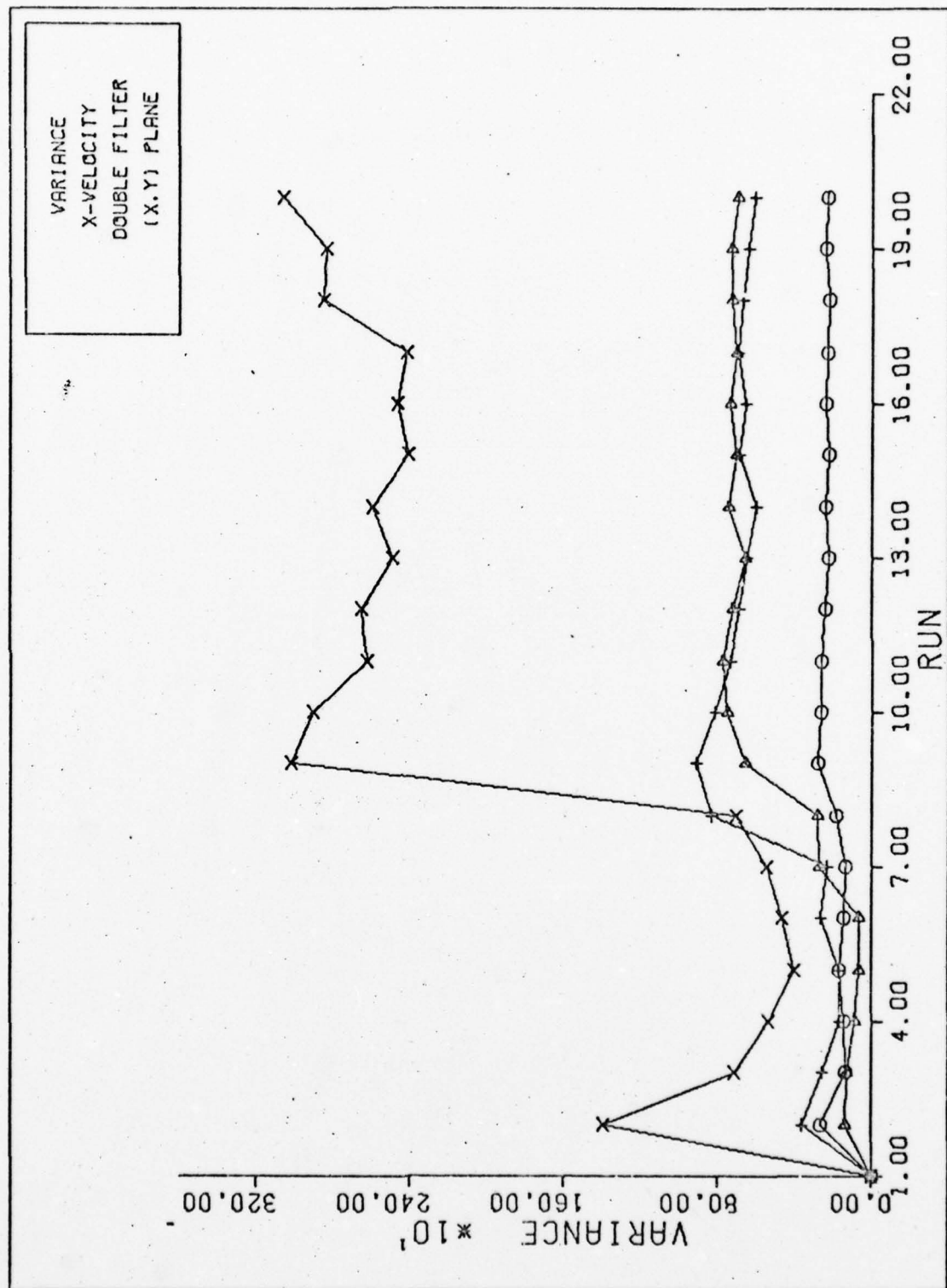


Fig. C-57

VARIANCE CONVERGENCE

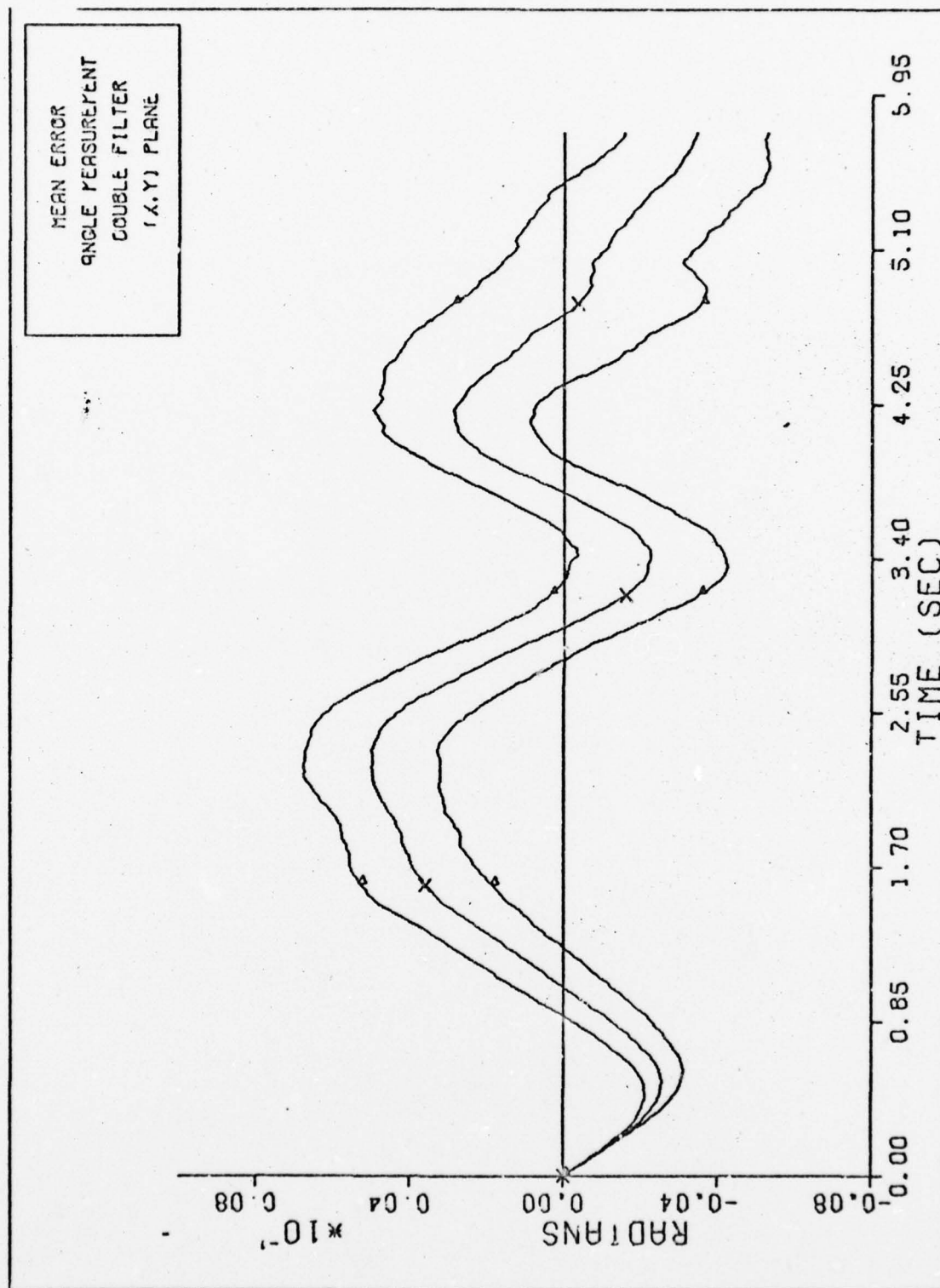


Fig. C-58

ANGLE MEASUREMENT DOUBLE FILTER

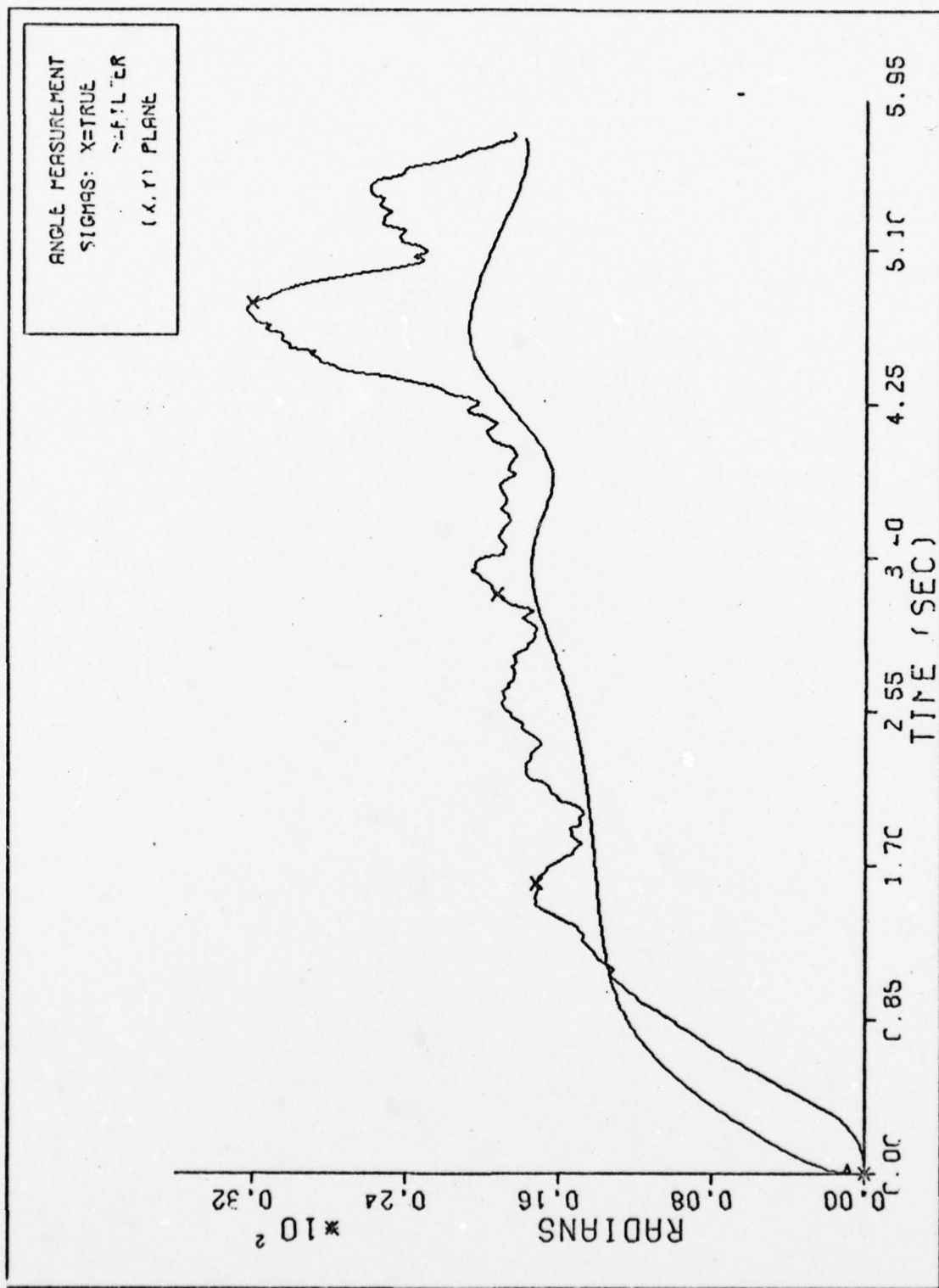


Fig. C-59 ANGLE MEASUREMENT SIGMAS DOUBLE FILTER

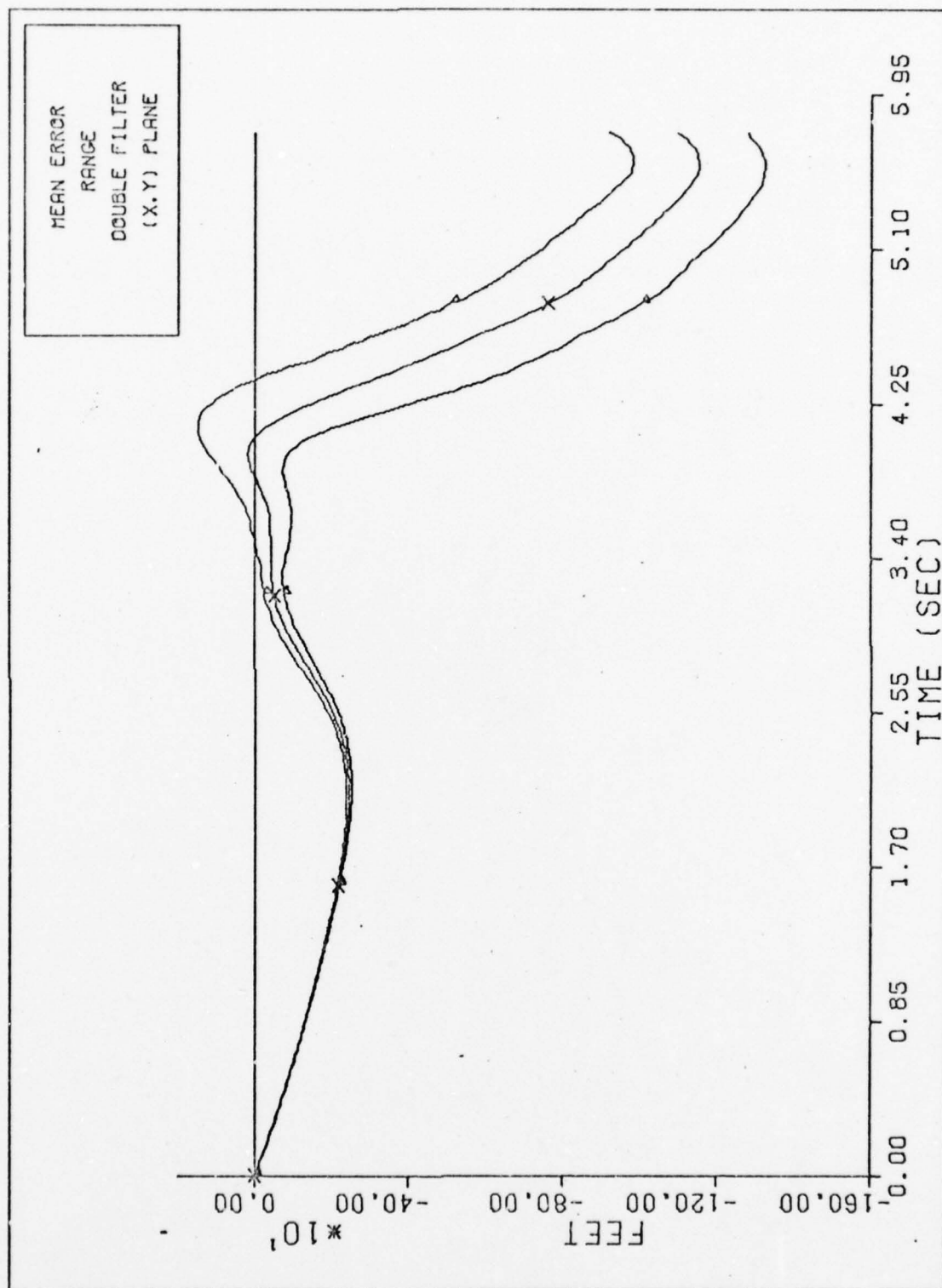


Fig. C-60

RANGE DOUBLE FILTER

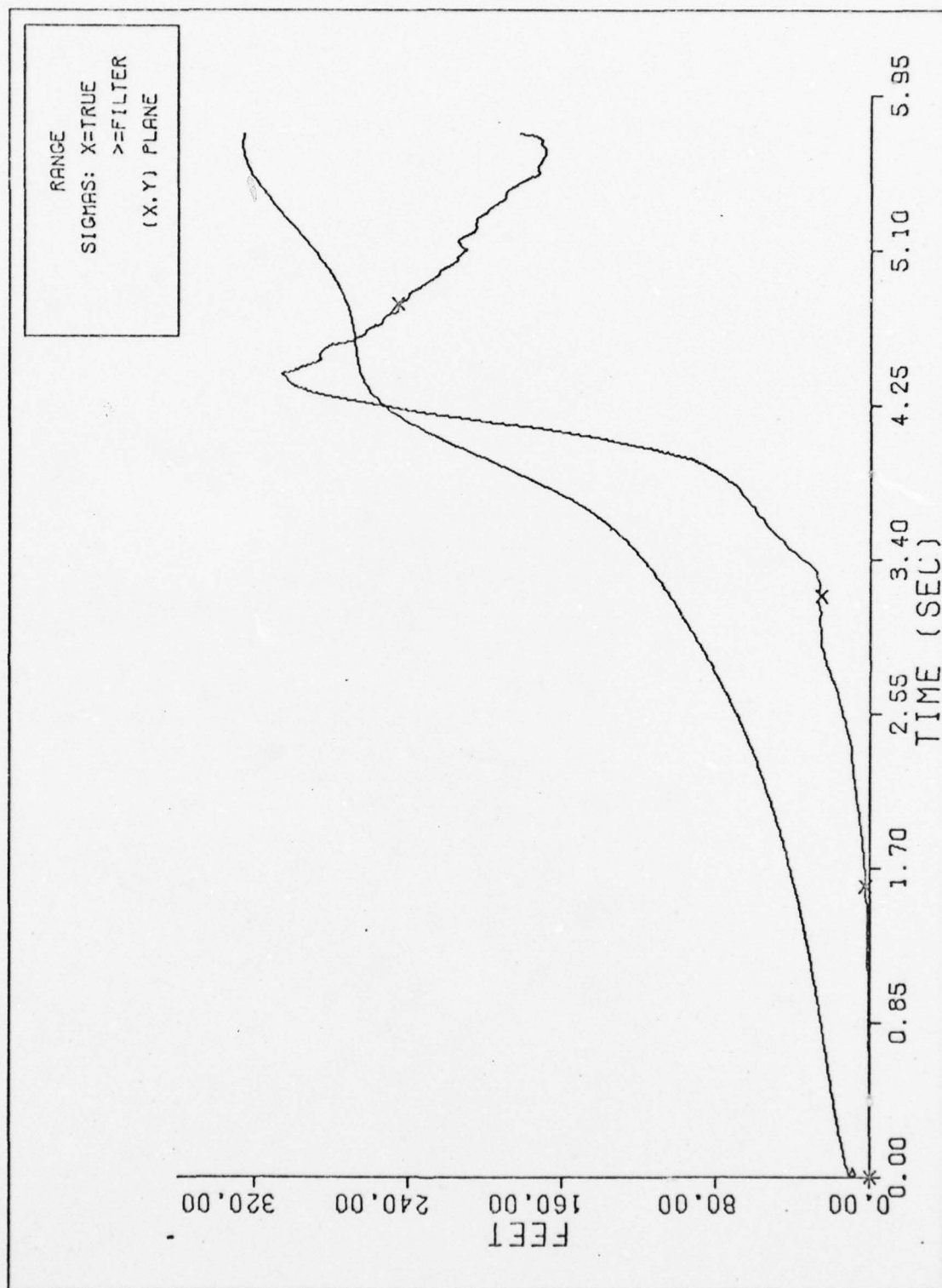


Fig. C-61

RANGE SIGMAS DOUBLE FILTER

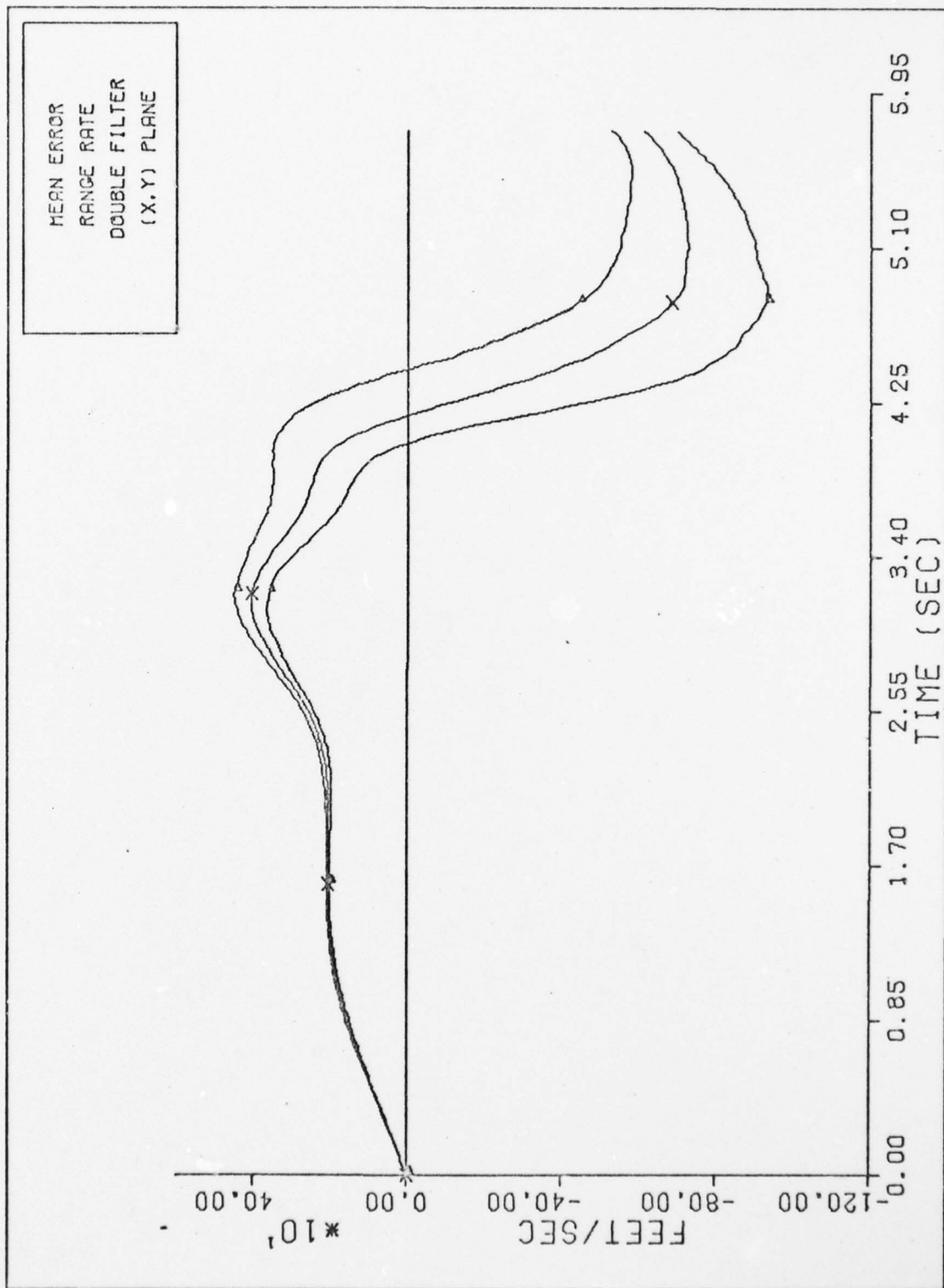


Fig. C-62

RANGE RATE DOUBLE FILTER

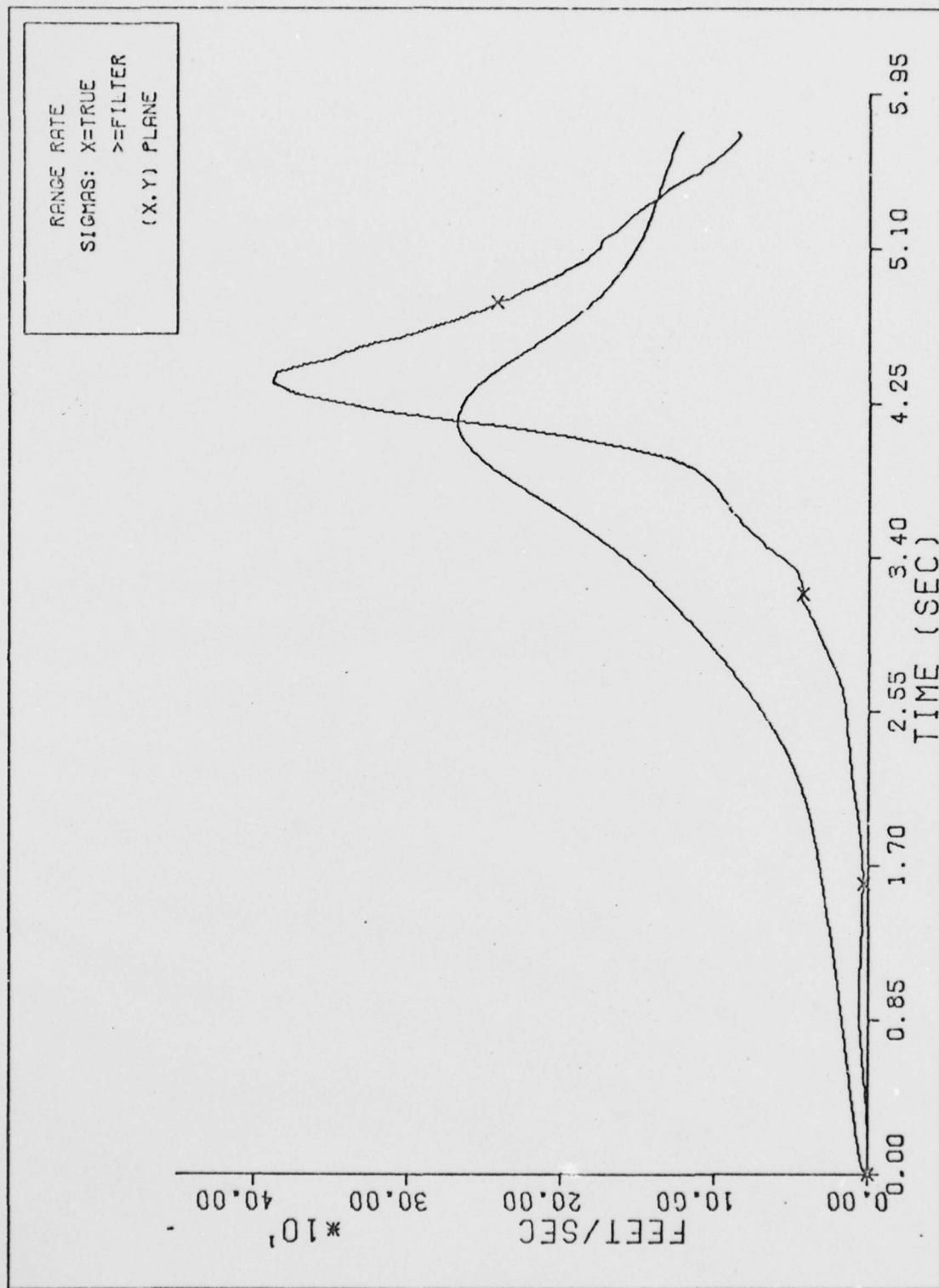


Fig. C-63

RANGE RATE SIGMAS DOUBLE FILTER

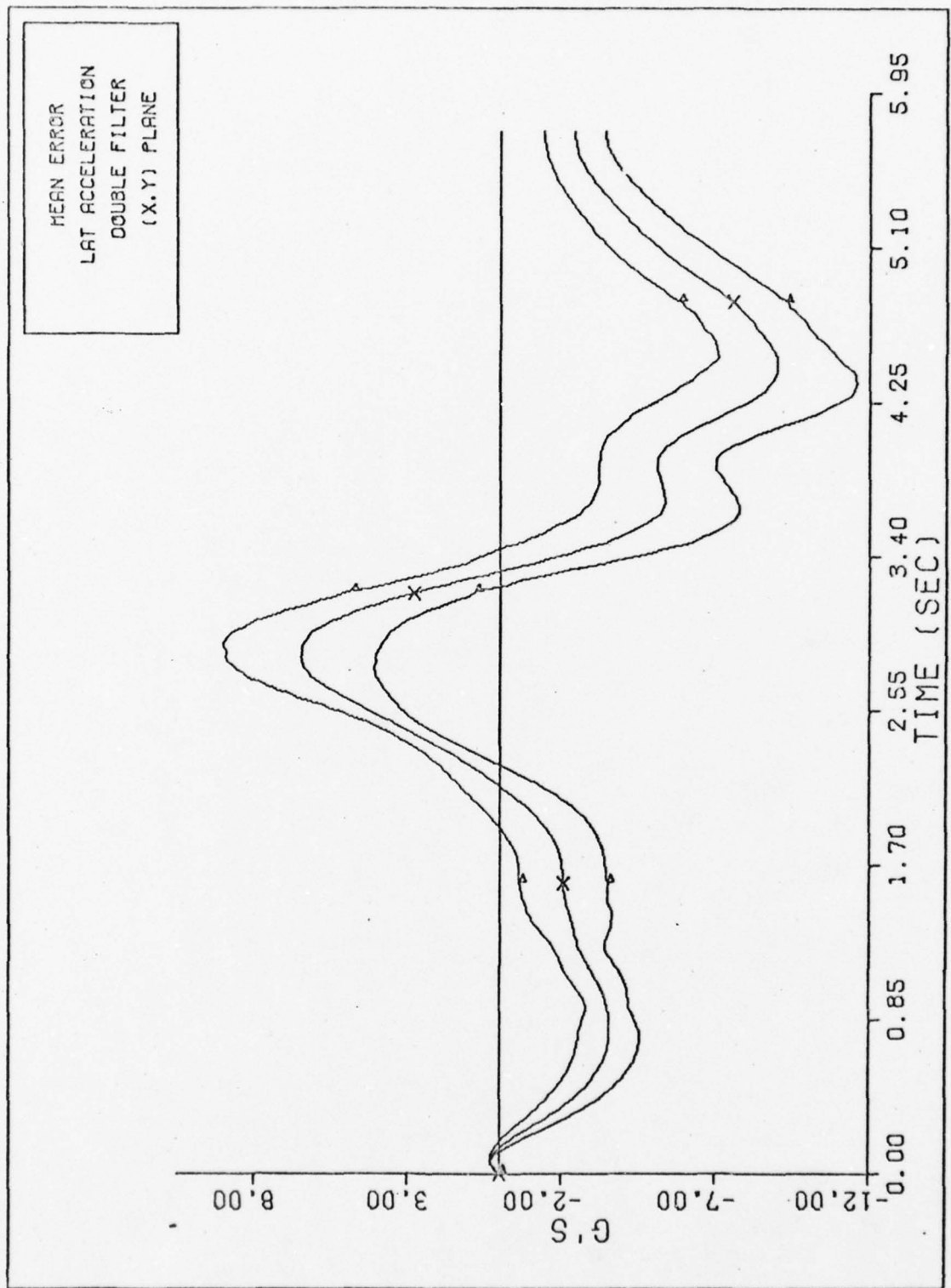


Fig. C-64 LAT ACCELERATION DOUBLE FILTER

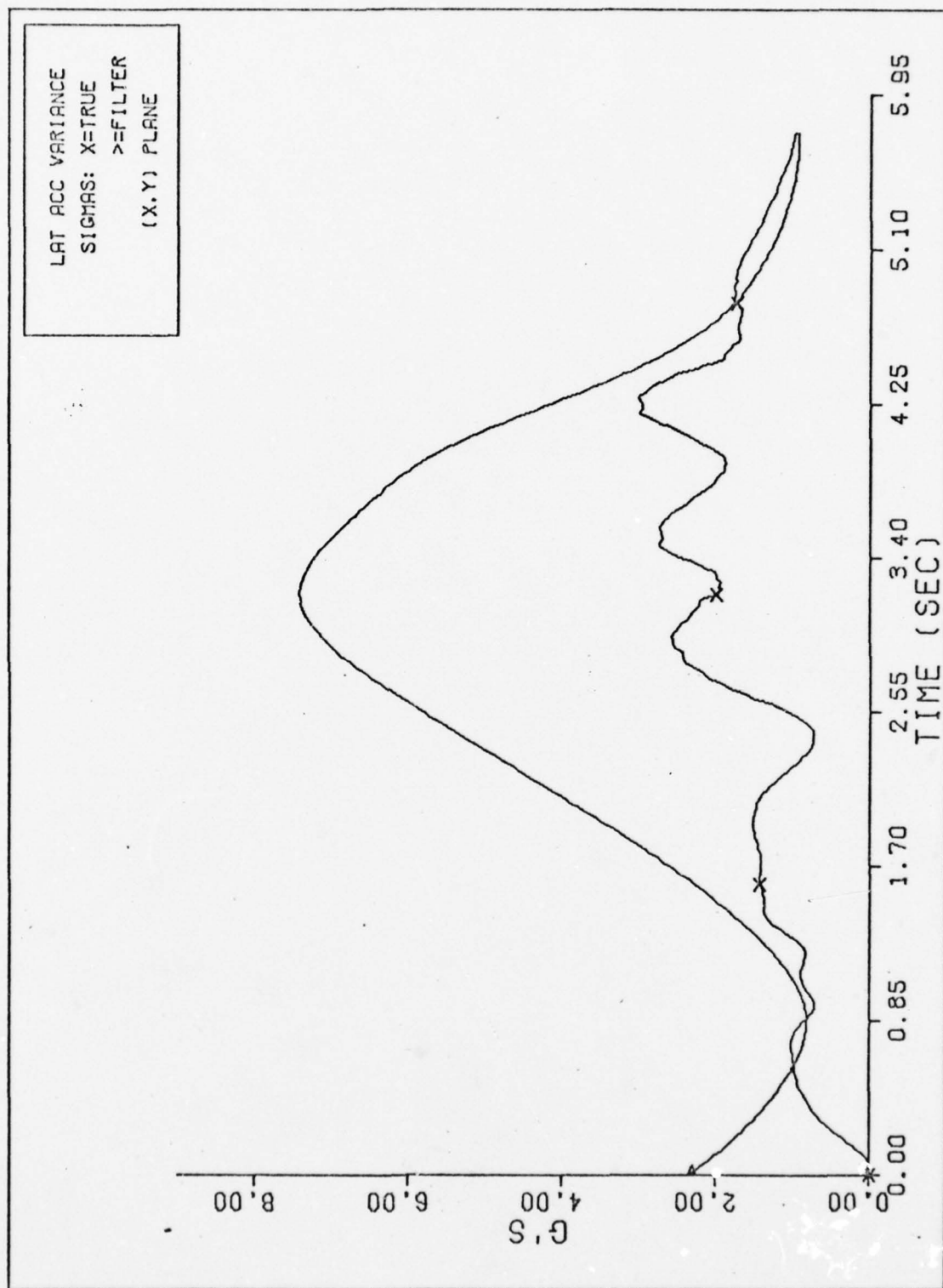


Fig. C-65 LAT ACCELERATION SIGMAS DOUBLE FILTER

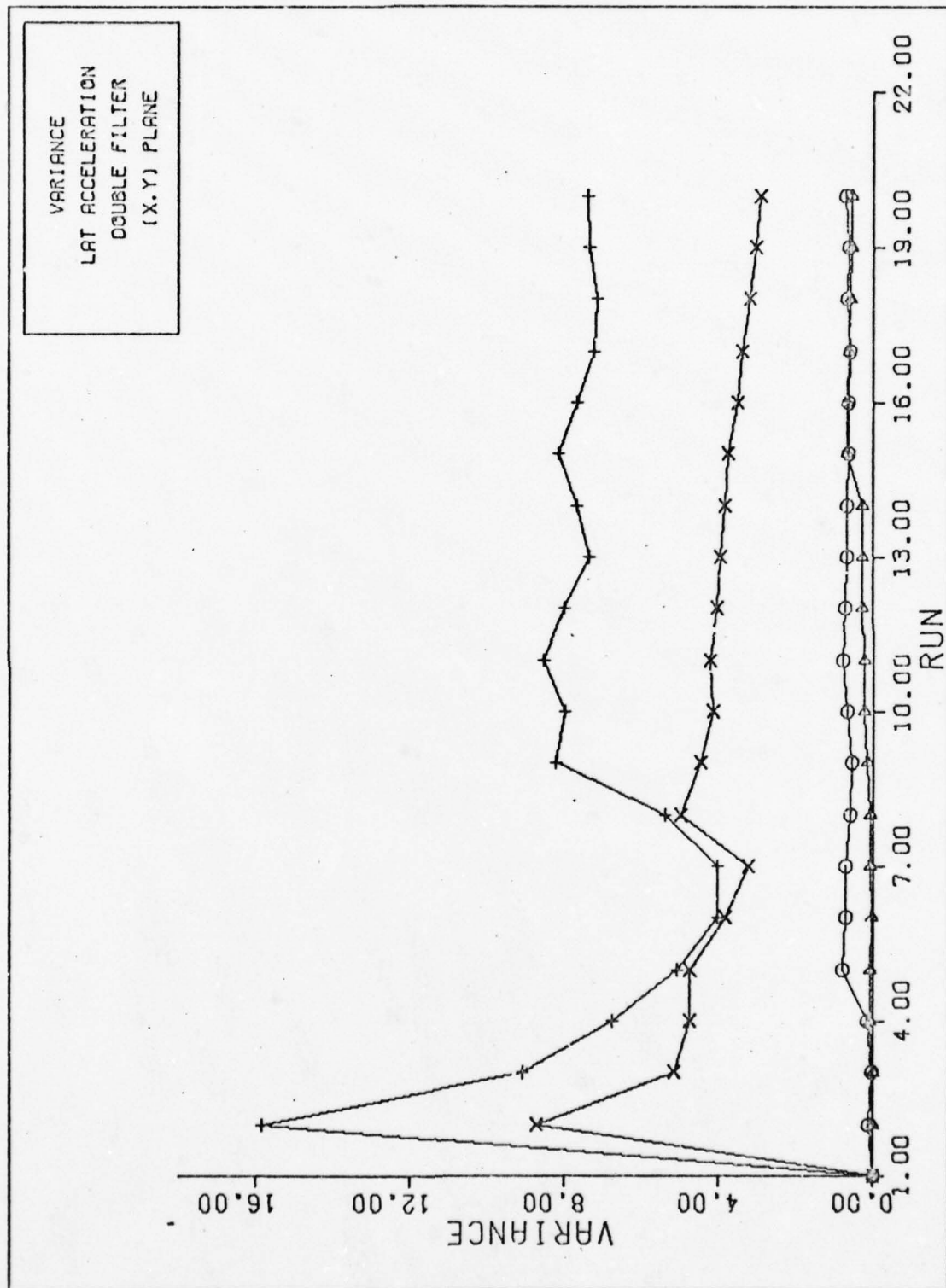


Fig. C-66

VARIANCE CONVERGENCE

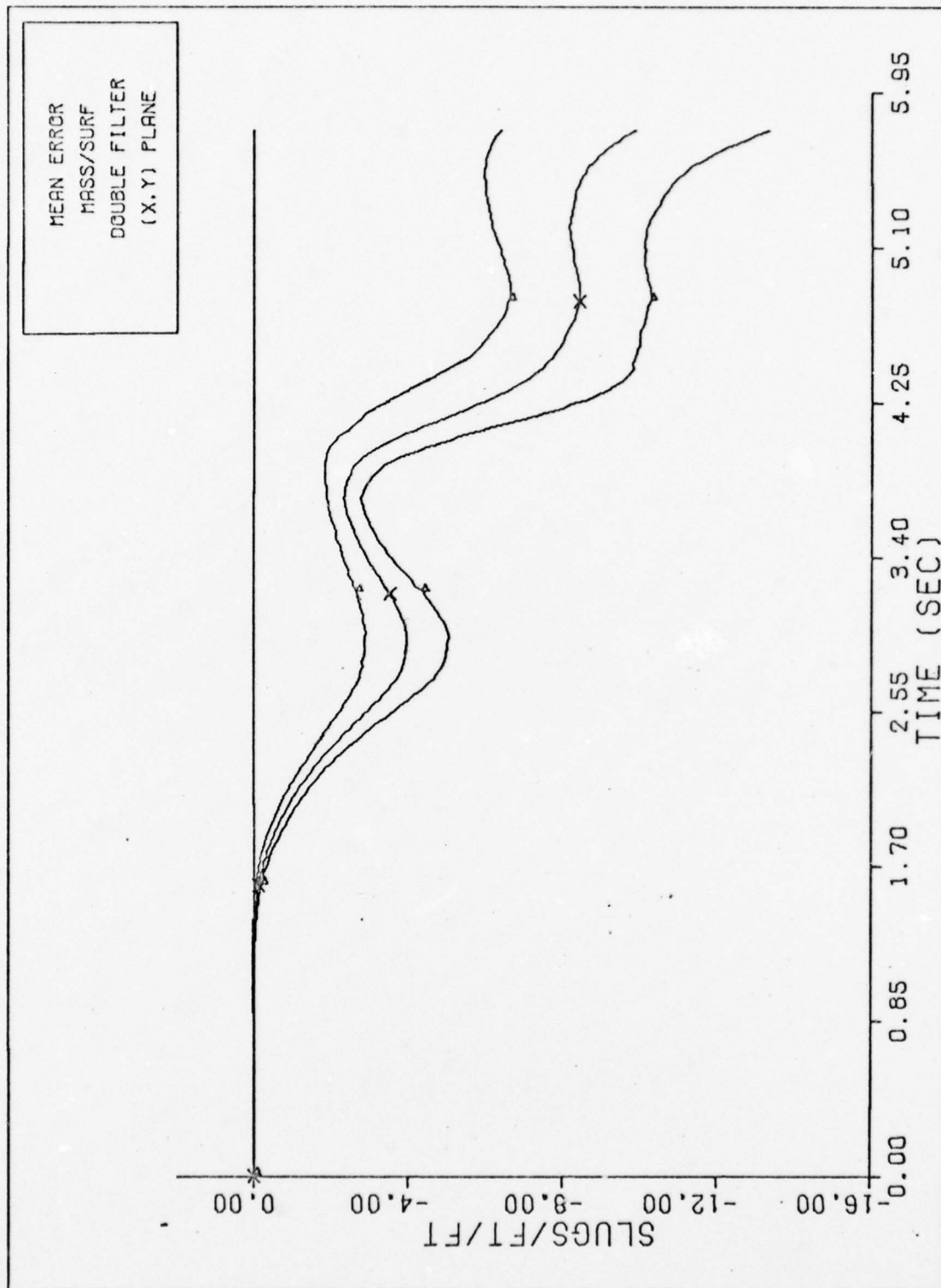


Fig. C-67

MASS/SURF DOUBLE FILTER

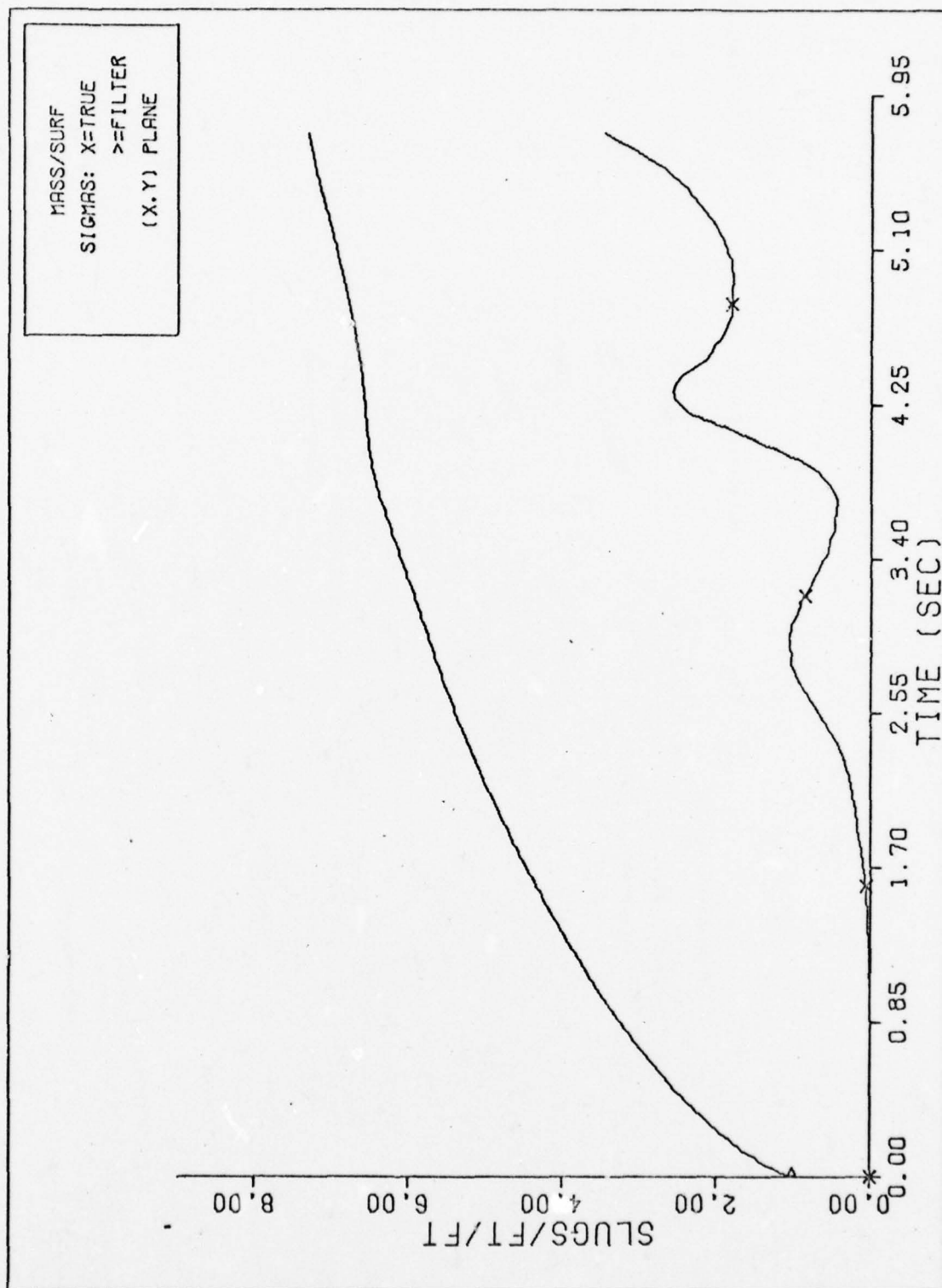


Fig. C-68

MASS/SURF SIGMAS DOUBLE FILTER

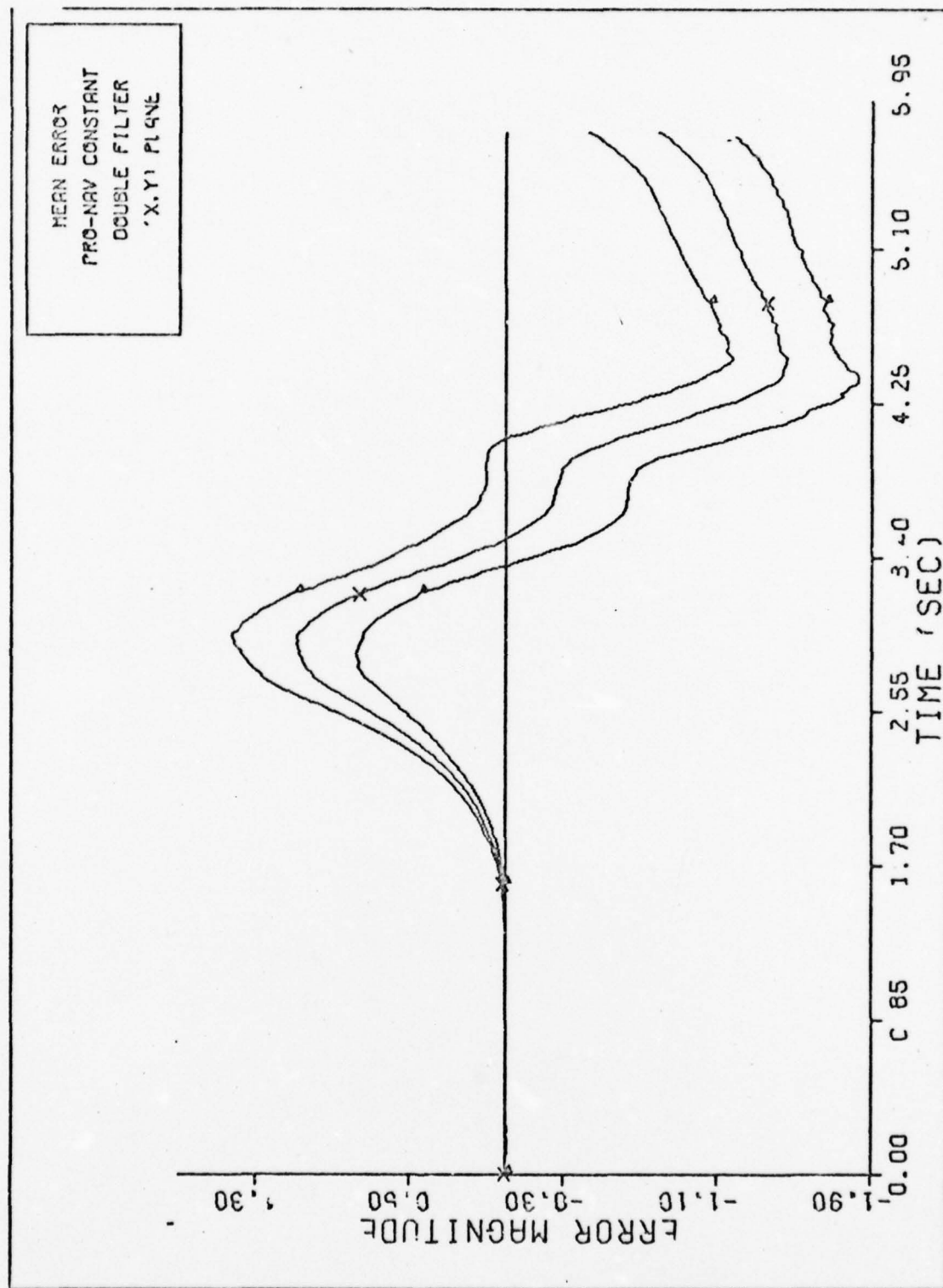


Fig. C-69

PRG NAV CONSTANT DOUBLE FILTER

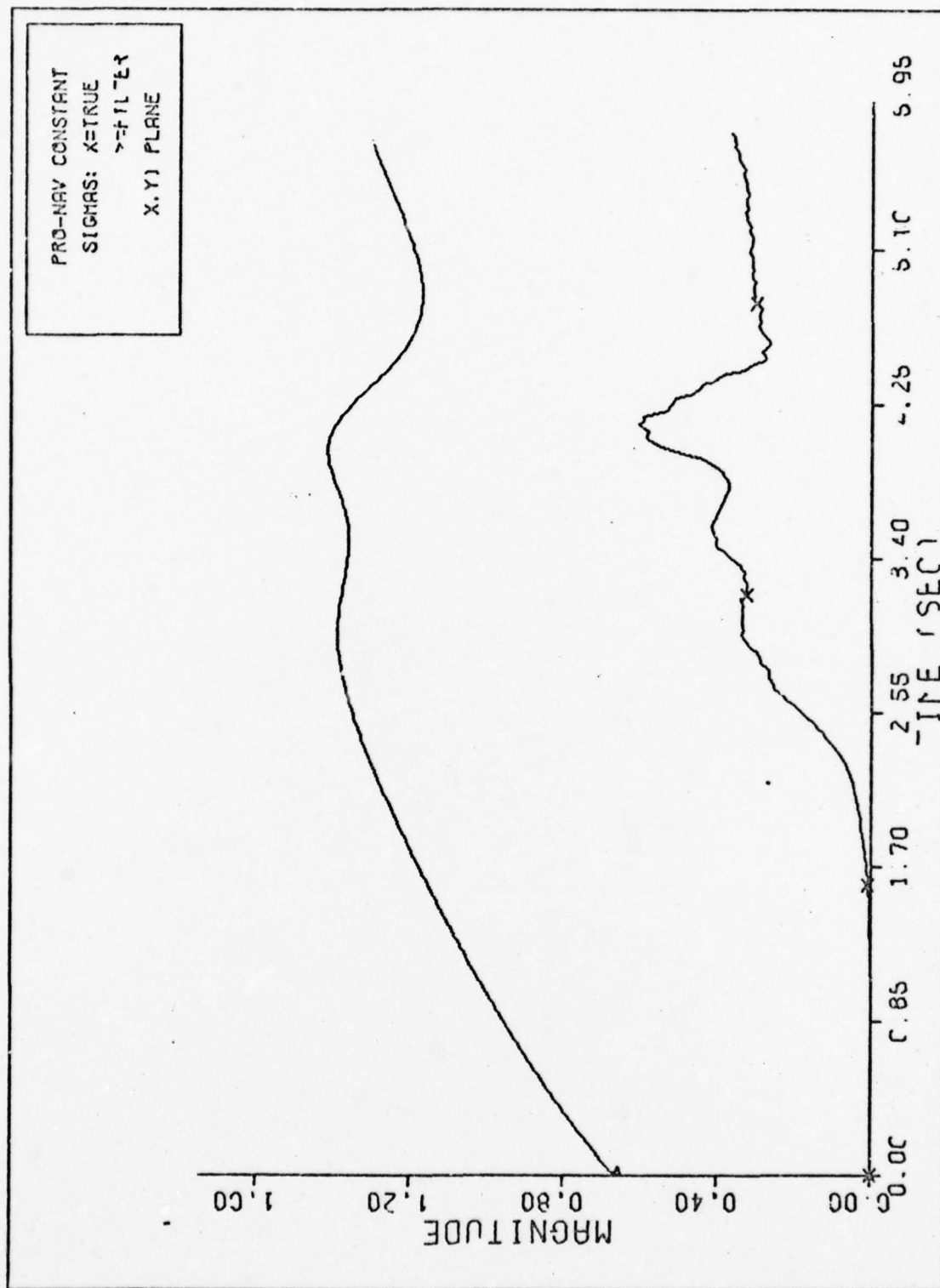


Fig. C-70

PRO NAV CONSTANT SIGMAS DOUBLE FILTER

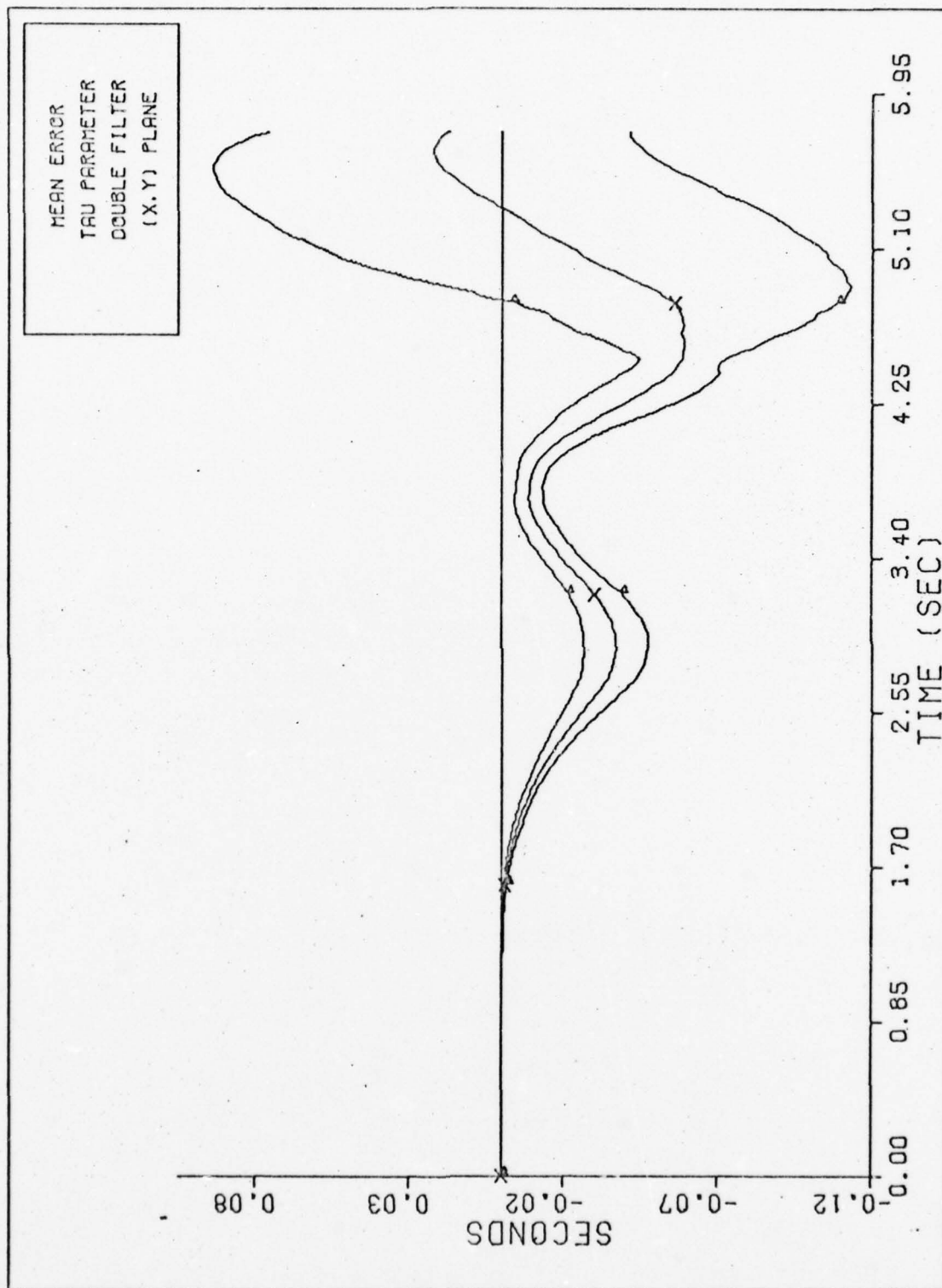


Fig. C-71

TAU PARAMETER DOUBLE FILTER

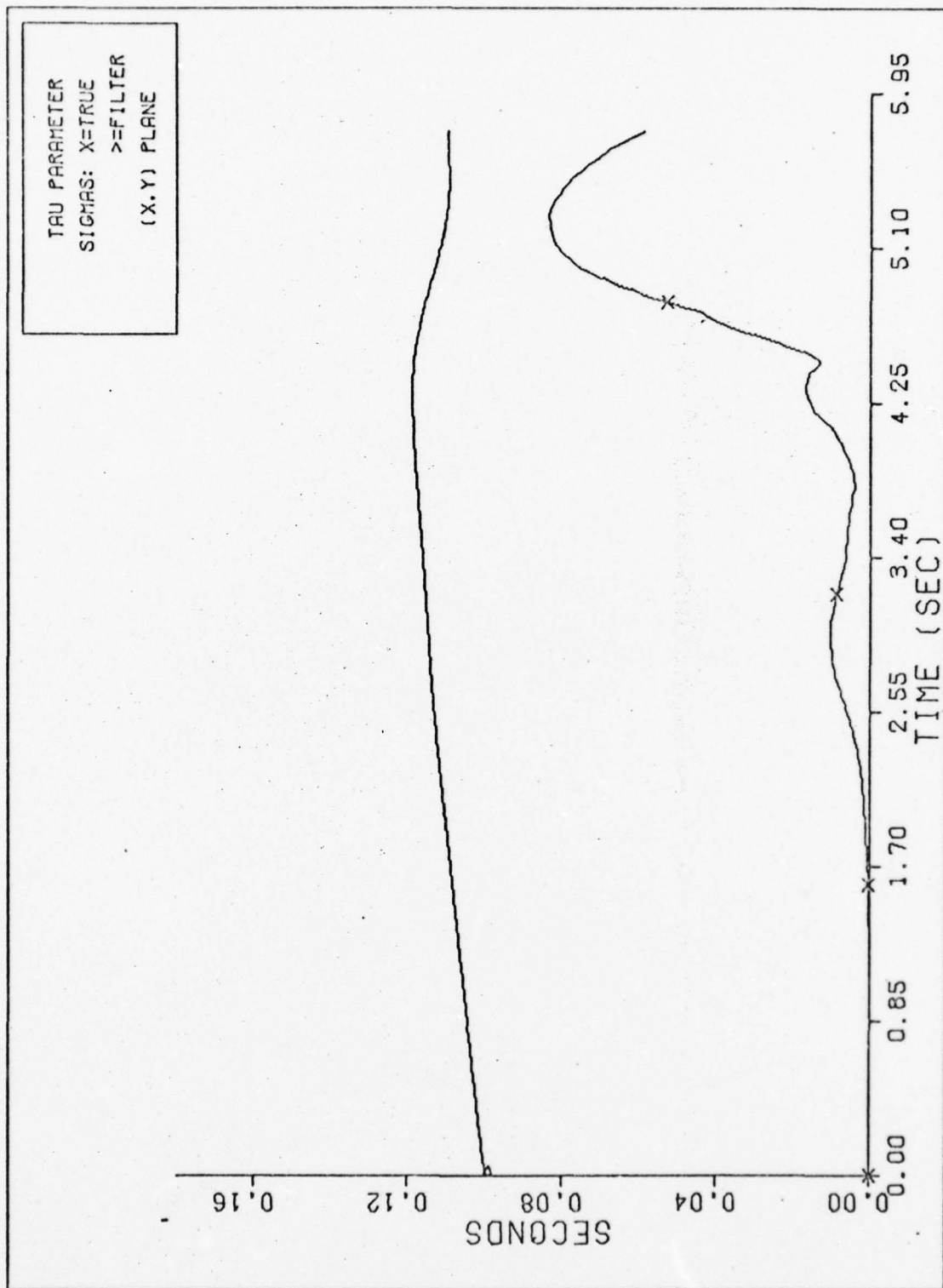


Fig. C-72

TAU PARAMETER SIGMAS DOUBLE FILTER

Appendix D

Appendix D contains the computer software used to evaluate the 11 state filter. The only subroutine that is not contained in this appendix is Subroutine MINV - a matrix inversion subroutine. The software is organized as follows:

<u>Unit</u>	<u>Page</u>
Program Eigen.....	77
(Executive program)	
Subroutine Traj.....	84
(Truth models)	
Subroutine Noise.....	97
(Generates noise values)	
Subroutine TIN.....	99
(Rotates vector as per Appendix A)	
Subroutine Cross.....	100
(Crosses two vectors)	
Subroutine DxCovar.....	101
(Propagates the filter)	
Subroutine Fmat.....	103
(Evaluates filter's partial derivative equations)	
Subroutine DxGain.....	105
(Computes Kalman filter gain)	

Subroutine DxPPlus.....	106
(Computes the covariance update)	
Subroutine DxSPlus.....	107
(Computes the state update)	
Subroutine Reed.....	108
(Reads filter initialization values)	
Subroutine MMPY.....	109
(Multiplies two matrices)	
Subroutine MTRAN.....	110
(Transposes a matrix)	
Subroutine MSUB.....	111
(Subtracts two matrices)	
Subroutine MADD.....	112
(Adds two matrices)	

```

PROGRAM EISEN(INPUT,OUTPUT,TAPE4,TAPE5,TAPE6,TAPE8,TAPE9,DEBUG=OUT
      PUT,TAPE2)
      COMMON/SIFE/A1(11,11),A2(11,11),A3(11,6),A5(6,6),A7(11)
      COMMON/SIFE1/V(3),A(3)
      COMMON/SIFE1/K1,K2,K3,K4,K5,K6,W,TS(11),TYME,DT,TRJONT,PNK,MODE1,
      TAP3
      COMMON/SIFE2/COT2,SIT2,COA2,SIA2,COA1,SIA1,VM,Z,B,G,AD,COT1,SIT1
      COMMON/SIFE3/Q(11,11),F(11,11),FS(11),FP(11,11)
      COMMON/SIFE4/MEAS(6)
      COMMON/SIFE5/EK(11,6)
      COMMON/SIFE5/H(6,11),K(6,5)
      DIMENSION FVAR(11,268),VAR(11,268)
      DIMENSION FSDUM(11),FPOUM(11,11),RDUM(6,6),ODUM(11,11)
      DIMENSION OUT(23),VPT(20,4),VP2(20,5)
      DIMENSION XSM(11,268),XSOS(11,268),FVARS(11,268),XM(11,268)
      INTEGER TRJONT,ON
      LOGICAL TAP,TAPE,MODE1
      REAL MEAS,K1,K2,K3,K4,K5,K6
      *****
      PROGRAM AND INTEGRATION PARAMETERS
      DT = PROGRAM INTEGRATION STEP SIZE
      JJ = CONTROLS NUMBER OF SIMULATION RUNS BY # RUNS = 10 - JJ
      MODE1 FALSE = INITIALIZES TRAJ
      N = DIMENSION OF FSDUM, FPOUM, ODUM, AND RDUM
      PNK = PRO NAI CONSTANT
      TAP FALSE PRINTS STATE ERRORS ON TAPE 9
      TAP3 TRUE = PRINTS MISSILE DATA ON TAPE4, TAPE5, AND TAPE6
      TRJONT CONTROLS INTEGRATION STEP SIZE OF TRAJ BY DX = DT/TRJONT
      *****
      *****
      DT=.02
      G=.707*32.17**1.E-3
      B=1.017
      Z=1.000E5
      N=11
      CALL REED(FSDUM,FPOUM,RDUM,ODUM,N,RN)

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```

C      CALL FANSET(121412024)
C      IF(RN.EQ.2) CALL RANSET(.27327523703+-)
C      *****
C      INITIALIZATION FOR 20 RUNS
C      *****
      TAP=.TRUE.
      TAPJ=.FALSE.
      IF(TAP)GO TO 332
      PRINT(3,358)
      PRINT(3,357)
317  FORMAT(T3,"TIME",T14,"THEIA 1",T25,"THEIA 2",T36,"W 1",T47,"W 2",
      .T58,"RANGE",T69,"R-OUT",T80,"AL-1",T91,"AL-2",T102,"PRO NAV",T113,
      .T124,"4/S",//)
318  FORMAT(T60,"STATE ERRORS",//)
332  CONTINUE
      DO 340 I=1,238
      DO 345 J=1,11
      XSUM(J,I)=0
      FVARS(J,I)=0
318  XSQS(J,I)=0
      JJ=1
      *****
      TRACKER AND MISSILE INITIALIZATION PARAMETERS
      *****
      TRJUNT=>
      RNK=6.5
      *****
      INITIALIZATION VALUES FOR TRACKER MEASUREMENT NOISES
      *****
      CORR0 (ANGLE MEAS. SCINTILLATION NOISE)
      CORR1 (ANGLE MEAS. THERMA- NOISE)
      CORR2 (RANGE MEAS. SCINTILLATION NOISE)
      CORR3 (RANGE MEAS. THERMAL NOISE)
      CORR4 (RANGE RATE MEAS. SCINTILLATION NOISE)
      CORR5 (RANGE RATE THERMAL NOISE)
      CORR6 (ANGLE RATE SCINTILLATION NOISE)

```

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```

C      CORR (ANGLE RATE THERMAL NOISE)
C      *****
CORR0=0.000475175
CORR1=0.00125
CORR2=2.82343
CORR3=11.7
CORR4=0.5454
CORR5=7.
CORR6=.000045
CORR7=.001745
000790
000800
000810
000820
000830
000840
000850

```

```

C      *****
C      INITIALIZATION FOR EACH RJN
C      *****

```

```

999  CONTINUE
      MODE1=.FALSE.
      LTIME=0
      TYME=0
      X0=X1=X2=X3=X4=X5=0.0
      *****
C      TRAJECTORY INITIALIZATION
C      *****
C      CALL TRAJ
C      MODE1=.TRUE.
      *****
000850
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000950

```

```

C      *****
C      INITIALIZATION OF FILTER STATE, COVARIANCE, Q, R, AND H MATRIX
C      *****

```

```

DO 3 J=1,11
DO 5 I=1,5
H(I,J)=0
CONTINUE
CONTINUE
H(1,1)=H(2,2)=H(3,3)=H(4,4)=H(5,5)=H(6,6)=1
DO 11 J=1,11
DO 10 I=1,11
F(I,J)=0
CONTINUE
      *****
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```

18  CONTINUE
    ITIME=ITIME+1
    IF(JJ.EQ.1)WRITE(8)OUT(1)
    IF(IAP)GO TO 333
    WRITE(9,370)(OUT(I),I=1,12)
    WRITE(9,371)(OUT(I),I=13,23)
370  FORMAT(T3,12(G9.3,2X))
371  FORMAT(T12,11(G9.3,2X),/)
333  CONTINUE

    *****
    COMPUTATION OF RUN STATISTICS
    *****
    DO 310 J=1,11
        XSUM(J,ITIME)=XSUM(J,ITIME)+OUT(J+1)
        XSQS(J,ITIME)=XSQS(J,ITIME)+OUT(J+1)**2
        FVARS(J,ITIME)=FVARS(J,ITIME)+OUT(J+12)
        XY(J,ITIME)=XSUM(J,ITIME)/FLOAT(JJ)
        IF(JJ.EQ.1)GO TO 310
        FVAR(J,ITIME)=FVARS(J,ITIME)/JJ
        VAR(J,ITIME)=XSQS(J,ITIME)/FLOAT(JJ-1)-FLOAT(JJ)*XM(J,ITIME)**2/
        .FLOAT(JJ-1)
    IF(VAR(J,ITIME).LT.0.)VAR(J,ITIME)=0.
310  CONTINUE
    IF(IYME.GT.5.73)GO TO 501
    *****
    PROPAGATION OF TRUTH MODE_
    *****
    CALL TRAJ
    *****
    PROPAGATION OF FILTER STATES AND FILTER COVARIANCE
    *****
    CALL DXCOVAR(2,DT)
    *****
    COMPUTATION OF MEASUREMENT NOISE
    *****
    CALL NOISE(CORR0,0.,CORRUP)

```

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```

XU=X0-2*X0*DT+CORRUP
CALL NOISE(CORR1,0.,CORRUP)
MEAS(1)=TS(1)+X0+CORRUP
CALL NOISE(CORR0,0.,CORRUP)
X1=X1-2*X1*DT+CORRUP
CALL NOISE(CORR1,0.,CORRUP)
MEAS(2)=TS(2)+X1+CORRUP
CALL NOISE(CORR0,0.,CORRUP)
X2=X2-.057*X2*DT+CORRUP
CALL NOISE(CORR1,0.,CORRUP)
MEAS(3)=TS(3)+X2+CORRUP
CALL NOISE(CORR0,0.,CORRUP)
X3=X3-.007*X3*DT+CORRUP
CALL NOISE(CORR1,0.,CORRUP)
MEAS(4)=TS(4)+X3+CORRUP
CALL NOISE(CORR0,0.,CORRUP)
X4=X4-2*X4*DT+CORRUP
CALL NOISE(CORR3,0.,CORRUP)
MEAS(5)=TS(5)+(X4+CORRUP)/1000
CALL NOISE(CORR1,0.,CORRUP)
X5=X5-1*X5*DT+CORRUP
CALL NOISE(CORR5,0.,CORRUP)
MEAS(6)=TS(6)+(X5+CORRUP)/1000

```

```

C
C
C
UPDATE OF FILTER STATES AND FILTER COVARIANCE WITH MEASUREMENTS
*****

```

```

CALL EXGAIN
CALL OXPPLUS
CALL OXSPLUS
GO TO 500

```

```

C
C
*****
END OF RUN

```

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C C C C C C
SUBROUTINE TRAJ
*****
SUBROUTINE TRAJ GENERATES THE NOMINAL TRAJECTORIES FOR THE
MONTE CARLO ANALYSIS
*****
IMPLICIT REAL(J-N)
VVIS(3), AMIS(3), ANCL(3), MCL(3), MISZ(3), RANG(3)
DIMENSION LOR(3), DA(3), ALDS(3), ALPCH(3), ALYAW(3), WIN(3), WMIS(3)
DIMENSION VOWN(3), AOWN(3), P(8), Y(13), NORH(3), ALM(3)
DIMENSION XOWN(3), XMIS(3)
COMMON/SIIE1A/V(3), R(3)
COMMON/SIIE1/K1, K2, K3, K4, K5, K6, W, TS(11), X, DY, TRJCNT, PNK, MODE1, TAP5
LOGICAL MODF1, TAP8
INTEGER TRJCNT
DOUBLE PRECISION RANGE, MYORM
IF (MODE1) GO TO 77
*****
INITIALIZATION OF SYSTEM PARAMETERS
*****
DEFINITIONS
M4SS= MISSILE MASS
IYY = MOMENT OF INERTIA, MISSILE YY AXIS, WHICH EQUALS
THE MOMENT OF INERTIA OF THE MISSILE 77 AXIS
OMEGA= AUTOPILOT 2ND ORDER NAT. FREQ COEFF.
ZETA= AUTOPILOT 2ND ORDER DAMPING COEFFICIENT
A= HACH CONVERSION AT 10,000 FEET STANDARD DAY
D= CHARACTERISTIC LENGTH OF MISSILE
RHO= AIR DENSITY
XKR= ABERATION SLOPE FOR THE NOSE CONE
TAU1= SEEKER TIME CONSTANT
TAU2= PROPORTIONAL NAV LAW TIME CONSTANT
LAY= ACTUATOR TIME CONSTANT
G= ACCELERATION OF GRAVITY
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002390
002390
002400

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RANGE=DSORT (ABS (RANG (1)) * * 2.00 + ABS (RANG (2)) * * 2.00 + ABS (RANG (3))
* * 2.00)
DO 753 I=1,3
  LOS(I)=RANG(I)/RANGE
753 ANCL(I)=LOS(I)
  Y(1)=SQRT (VM**2-VMIS(3)**2)
  VMIS(1)=Y(1)*LOS(1)
  VMIS(2)=Y(1)*LOS(2)
DO 200 I=1,3
  MCL(I)=VMIS(I)/VM
200 AMIS(I)=-ADRAS*MCL(I)
  MIS7(1)=MCL(1)*MCL(2)
  MIS7(2)=MCL(3)*2-MCL(1)*I2
  MIS7(3)=-MCL(2)*MCL(3)
  MNORM=DSORT (ABS (MIS7(1)) * * 2.00 + ABS (MIS7(2)) * * 2.00 + ABS (MIS7(3))
* * 2.00)
DO 210 I=1,3
210 MISZ(I)=MIS7(I)/MNORM
  VC=SQRT ((VMIS(1)-VOWN(1)) * LOS(1)) * * 2 + ((VMIS(2)-VOWN(2)) * LOS(2))
* * 2 + ((VMIS(3)-VOWN(3)) * LOS(3)) * * 2)

```

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STATE INITIALIZATION FOR INTERFACE
NOTE: AL- STATES ARE OUTPUTTED IN KILOFEET UNITS RATHER
THAN FEET

```

THETAY=C.
THETAP=0.
TS(1)=ATAN (-LOS(3)/LOS(1))
TS(2)=ASIN (LOS(2))
SI=SIGN (TS(1))
CO=COS (TS(1))
SIF=SIGN (TS(2))
COT=COS (TS(2))
B(1)=COT * AOWN(2) - SIF * (CO * AOWN(1) - SI * AOWN(3))
B(3)=SIF * AOWN(2) + COT * (CO * AOWN(1) - SI * AOWN(3))

```

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000213

```

LD=(DP*SURF*CHD)/(MASS*VM)
LA=(DP*SURF*CHNA)/(MASS*VM)
*****
INITIALIZATION OF AUTOPILOT FEEDBACK COEFFICIENTS AND GAIN
*****
H1=-LA*(MA-(MD/LD)*LA+OMEGA**2+(2*ZETA*OMEGA+MQ)*(MD/LD+MQ))/(MD*
X(MA-MD*LA/LD+OMEGA**2)+(MD+2*ZETA*OMEGA)*(LD*MA-MD*LA))
H2=(LD*MA*(LA-2*ZETA*OMEGA-MQ)+MD*(-A*(2*ZETA*OMEGA-LA)-OMEGA**2
X-MA))/(VM*LD*(MD*(MA-MD*LA/LD+OMEGA**2)+(MQ+2*ZETA*OMEGA)*(LD*
XMA-MD*LA)))
KD=41/VM+H2-(1/VM)*((MA+LA*MQ)/(LA*MD-MA*LD))
DX=DY/FLOAT(ERJUNT)
CORR=CORR*SORT(CX)
CURR1=CORR1*SORT(CX)
CURR2=CORR2*SORT(CX)
CURR3=CORR3*SORT(CX)
IF(.NOT.TAP8)GO TO 505
PRINT(4,20)
20 FORMAT(5X,"TIME",T15,"THETA1",T25,"THETA2",T35,"RANGE",
.T45,"VCM",T55,"AL PITCH",T65,"AC PITCH",T75,"AL YAW",T85,"AC YAW")
PRINT(4,15)X,TS(1),TS(2),TS(3),TS(5),TS(7),Y(8),TS(8),Y(4)
15 FORMAT(7,1X,10(66.2,2X))
PRINT(5,501)
PRINT(5,455)
PRINT(5,450)X,XOWN(1),XOWN(1),AOWN(1),XVIS(1),VMIS(1),AMIS(1),
.ALPH(1),ALYAW(1)
PRINT(5,51)XOWN(2),XOWN(2),AOWN(2),XVIS(2),VMIS(2),AMIS(2),
.ALPH(2),ALYAW(2)
PRINT(5,451)XOWN(3),XOWN(3),AOWN(3),XVIS(3),VMIS(3),AMIS(3),
.ALPH(3),ALYAW(3)
PRINT(5,453)
PRINT(5,502)
PRINT(5,453)
PRINT(5,453)
PRINT(5,550)X,MCL(1),MIS7(1),LOS(1),ALOS(1),ANCL(1),WIN(1)
PRINT(5,551)MCL(2),MIS7(2),LOS(2),ALOS(2),ANCL(2),WIN(2)
PRINT(5,551)MCL(3),MIS7(3),LOS(3),ALOS(3),ANCL(3),WIN(3)

```

```

PRINT (5,455)
501 FORMAT(5X,"X",I15,"XOWN",I25,"VOWN",I35,"AOWN",I45,"XMIS",I55,"VMI
.S",I65,"AMIS",I75,"ALPCH",I85,"ALYAW")
502 FORMAT(5X,"Y",I15,"MCL",I25,"MISZ",I35,"LOS",I45,"ALOS",I55,"ANC-
",I65,"WIN")
503 CONTINUE
RETURN
*****
INITIALIZATION COMPLETE. THE FOLLOWING IS THE RUN PORTION
*****
CONTINUE
DO 78 IT=1,ITJONT
*****
NOISE UPDATE
*****
CALL NOISE(CORR,0.,CORRUP)
Y(9)=Y(9)-.1*Y(9)*DX+CORRJP
CALL NOISE(CORR1,0.,CORRUP)
NOISE1=Y(9)+CORRUP
CALL NOISE(CORR,0.,CORRUP)
Y(10)=Y(10)-.1*Y(10)*DX+CORRJP
CALL NOISE(CORR1,0.,CORRUP)
NOISE2=Y(10)+CORRUP
CALL NCISE(CORR2,0.,CORRUP)
Y(11)=Y(11)-Y(11)*DX+CORRJP
CALL NOISE(CORR3,0.,CORRUP)
NOISE3=Y(11)+CORRUP
*****
DETERMINATION OF ABERATION ERROR
*****
THEIA=ACOS(MCL(1)*LOS(1)+MCL(2)*LOS(2)+MCL(3)*LOS(3))
IF(THETA.LI.1.5)GO TO 773
PRINT *,"MISSILE HAS LOST LOCK"
STOP
*****

```

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```

IF(E.E0.0.0.0) 3 TO 120
DO 32 I=1,3
32 NORM(I)=A-OS(I)-ANCL(I)
NNORM=DSORT(ABS(NORM(1))*2.00+ABS(NORM(2))*2.00+ABS(NORM(3))*2.
.00)
DO 57 I=1,3
67 NORM(I)=NORM(I)/NNORM
WIN(1)=WIN(3)=0
WIN(2)=1.
THETA=ACOS(ANCL(2))
PHEE=1.5707953267948966+.423-THETA
CALL TIN(ANCL,WIN,THETA,PHEE,WIN)
CALL CROSS(ANCL,WIN,DA,DX,0)
120 Y(12)=THETAY
Y(13)=THETAP
THETAY=(NORM(1)*DA(1)+NORM(2)*DA(2)+NORM(3)*DA(3))*E
THETAP=(NORM(1)*WIN(1)+NORM(2)*WIN(2)+NORM(3)*WIN(3))*E
Y(12)=THETAY-Y(12)
Y(13)=THETAP-Y(13)
WPITCH=WPITCH+Y(13)/TAU1
WYAW=WYAW+Y(12)/TAU1
WIN IS NOW THE ANGULAR RATE USED TO UPDATE SEEKER POSITION
DO 33 I=1,3
73 WIN(I)=-WYAW-WIN(I)+WPITCH*DA(I)
CALL CROSS(WIN,ANCL,ANCL,DX,2)
71 CONTINUE

```

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000870
000890
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000900

STATE EQUATIONS FOR MISSILE FLIGHT DYNAMICS

EQUATIONS 1-110 & COMPOSE THE GUIDANCE PACKAGE OF THE MISSILE
STATES 1 THROUGH 4 ARE YAW
5 THROUGH 8 ARE PITCH
9 MISSILE PITCH RATE

AD-A064 760

AIR FORCE INST OF TECH WRIGHT-PATTERSON AFB OHIO SCH--ETC F/G 15/3.1
A PRACTICAL THREE DIMENSIONAL, 11 STATE EXTENDED KALMAN FILTER --ETC(U)
DEC 78 C W HLAVATY

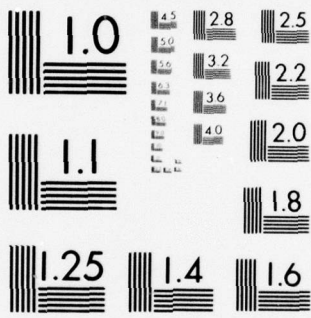
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NL

2 OF 3
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MICROCOPY RESOLUTION TEST CHART
NATIONAL BUREAU OF STANDARDS-1963-A

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003590
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255 MISSILE LATERAL ACCELERATION IN G'S
357 ELEVATION DEFLECTION IN RAD
455 COMMAND ACCELERATION IN G'S

P(1)=M0*Y(1)+(G*MA)/(VM*LA)+Y(2)+(MD-LD*MA/LA)*Y(3)
P(2)=1/G*(Y*LA-H1*LAM*VM*LD)+Y(1)-(LA+H2*LAM*VM*LD)*Y(2)-1/G*
XLAM*VM*LD*Y(3)+LAM*VM*LD*Y(4)
P(3)=-H1*LAM*Y(1)-G*H2*LAM*Y(2)-LAM*Y(3)+G*LAM*KD*Y(4)
P(4)=+PNK*VC/(G*TAU2)*WYAW-1/TAU2*Y(4)
P(5)=M0*Y(5)+(G*MA)/(VM*LA)+Y(6)+(MD-LD*MA/LA)*Y(7)
P(6)=1/G*(Y*LA-H1*LAM*VM*LD)+Y(5)-(LA+H2*LAM*VM*LD)*Y(6)-1/G*
XLAM*VM*LD*Y(7)+LAM*VM*LD*Y(8)
P(7)=-H1*LAM*Y(5)-G*H2*LAM*Y(6)-LAM*Y(7)+G*LAM*KD*Y(8)
P(8)=+PNK*VC/(G*TAU2)*WYAW-1/TAU2*Y(8)

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003680
003690

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003800
003840
003810
003820
003830
003840
003850
003860
003900
003910

STATE UPDATES (RECTANGULAR INTEGRATION)

Y(1)=Y(1)+P(1)*DX
Y(2)=Y(2)+P(2)*DX
Y(3)=Y(3)+P(3)*DX
Y(4)=Y(4)+P(4)*DX
Y(5)=Y(5)+P(5)*DX
Y(6)=Y(6)+P(6)*DX
Y(7)=Y(7)+P(7)*DX
Y(8)=Y(8)+P(8)*DX
CALL CROSS(MIS7,MCL,NORM,DX,0)

148 DO 150 I=1,3
ALYAW(I)=NORM(I)*Y(2)
ALPCH(I)=-MIS7(I)*Y(5)

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AN ACCELERATION LIMITER WOULD GO HERE TO LIMIT ALYAW AND ALPCH

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C      000270
C      000263
C      003500
C      003510
C      003520
C      004010
C      000371
C      000392
C      000333
C      000401
C      000411
C      000421
C      000431
C      000441
C      000233
C      000250
C      004290
C      004310
C      000120
C      004230
C      004270
C      000331
C      004330

      WMIS(I)=Y(1)*MISZ(I)+Y(5)*NORM(I)
150  ALM(I)=ALYAW(I)+ALPCH(I)

      *****
      TRAJECTORY PROPAGATION
      ACCELERATIONS, VELOCITIES, AND POSITION UNITS ARE FEET AND SECONDS
      *****

      X=X+DX
      AMIS(1)=(ALM(1)-ADRA3*VMIS(1)/VM)*G
      AMIS(2)=(ALM(2)-.707-ADRA3*VMIS(2)/VM)*G
      AMIS(3)=(ALM(3)-.707-ADRA3*VMIS(3)/VM)*G
      AOWN(1)=-K2*V**2*COS(W*X)
      AOWN(2)=-K4*V**2*SIN(W*X)
      AOWN(3)=-K6*V**2*SIN(W*X-.76)
      DO 175 I=1,3
      VMIS(I)=VMIS(I)+AMIS(I)*DX
      XMIS(I)=XMIS(I)+VMIS(I)*DX
      VOWN(I)=VOWN(I)+AOWN(I)*DX
      XOWN(I)=XOWN(I)+VOWN(I)*DX
170  CONTINUE

      *****
      UPDATE OF MISSILE AERODYNAMIC COEFFICIENTS
      *****

      VM=DSORT(ABS(VMIS(1))*2.00+ABS(VMIS(2))*2.00+ABS(VMIS(3))*2.00)
      MACH=VM/A
      DP=(RPO/2)*VM**2
      AL=DSORT(ABS(ALM(1))*2.00+ABS(ALM(2))*2.00+ABS(ALM(3))*2.00)
      CN=(AL*G*VASS**2)/(RHO*SR*V**2)
      CMQ=(-.4943+MACH*(-2503+MACH**2125))/(2.957+MACH*(-3.078+MACH))
      CMY=(-.8294+MACH*(-4.894+MACH**1.191))/(3.220+MACH*(-2.760+MACH))
      CMA=(-.2282+MACH*(-2.856+MACH**1.824))/(1.640+MACH*(-2.171+MACH))
      CVA=(1.250+MACH*(-.6398+MACH**2.634))/(2.393+MACH*(-2.132+MACH))

```

```

CND=(.3118+MACH*(-.2199+MACH+.06(5)))/(3.761+MACH*(-3.126+MACH))
CMA=CMA*57.235780
CMD=CMD*57.235780
CNA=CNA*57.235780
CND=CND*57.235780
MD=(DP*SURF*3**2*CMD)/(2*IYY*VM)
MA=(DP*SURF*3*MA)/IYY
MO=(DP*SURF*3*CMD)/IYY
LO=(DP*SURF*CMD)/(MASS*VM)
LA=(DP*SURF*CNA)/(MASS*VM)

*****
UPDATE OF AUTOPILOT FEEDBACK COEFFICIENTS AND GAIN
*****

H1=-LA*(MA-(MD/LD)*LA+OMEGA**2*(2*ZETA*OMEGA+MQ)*(MD/LD+MQ))/(MD*
X(MA-MD*LA/LD+OMEGA**2)*(4)+2*ZETA*OMEGA)*(LD*MA-MD*LA))
H2=(LD*MA*(LA-2*ZETA*OMEGA-MQ)+MD*(LA*(2*ZETA*OMEGA-LA)-OMEGA**2
X-MA))/(VM*LD*(MD*(MA-MD*LA/LD+OMEGA**2)+(MQ+2*ZETA*OMEGA)*(LD*
XMA-MD*LA)))
KO=H1/VM+H2-(1/VM)*((MA+LA*MQ)/(LA*MD-MA*LD))
CO=2/SQRT(MACH)+CN**2/CMA
ADRAG=((RHO/(2*MASS))*SURF*CD*VM**2)/G
IF (AMIS(1)**2+WMIS(2)**2+WMIS(3)**2).EQ.0.)GO TO 151
*****
UPDATE OF MISSILE FRAME ORIENTATION, RANGE, AND CLOSING VELOCITY
*****
CALL CROSS(WMIS,MCL,MCL,DX,2)
IF (Y(5).EQ.0.)GO TO 151
CALL CROSS(WMIS,MISZ,MISZ,DX,2)
151 DO 152 I=1,3
152 RANG(I)=XDOWN(I)-XMIS(I)
RANGE=DSQRT(ABS(RANG(1))**2+ABS(RANG(2))**2+ABS(RANG(3))
**2.00)
DO 153 I=1,3
153 LOS(I)=RANG(I)/RANGE

```

C C C C C

C C C

```

VM4=SQRT((VMIS(1)-VOWN(1))*LOS(1))*2+((VMIS(2)-VOWN(2))*LOS(2))
*2+((VMIS(3)-VOWN(3))*LOS(3))*2)
VC=VCM+NOISE3
76 CONTINUE

```

000253
000273

C
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C

UPDATE OF "TRUE STATES" AND PROGRAM INTERFACE QUANTITIES.

```

TS(1) = ATN((-LOS(3)/LOS(1))
SI=SIN(TS(1))
CO=COS(TS(1))
TS(2) = ASIN(LOS(2))
SIT=SIN(TS(2))
COT=COS(TS(2))
TS(3)=-RANGE/1000
TS(3)=VCH/1000
DA(1)=DA(3)=0
DA(2)=1
THETA=ACOS(MDL(2))
PHEE=1.5707953267948966-THETA
CALL TIN(MDL,DA,THETA,PHEE,DA)
CALL CROSS(MDL,DA,NORM,DX,0)
TS(7)=(DA(1)*ALM(1)+DA(2)*ALM(2)+DA(3)*ALM(3))*G
TS(3)=(NORM(1)*ALM(1)+NORM(2)*ALM(2)+NORM(3)*ALM(3))*G
TS(7)=TS(7)/1000
TS(3)=TS(3)/1000
B(1)=COT*DOWN(2)-SIT*(CO*DOWN(1)-SI*DOWN(3))
B(3)=SIT*DOWN(2)+COT*(CO*DOWN(1)-SI*DOWN(3))
B(2)=CO*DOWN(3)+SI*DOWN(1)
V(1)=COT*DOWN(2)-SIT*(CO*DOWN(1)-SI*DOWN(3))
V(3)=SIT*DOWN(2)+COT*(CO*DOWN(1)-SI*DOWN(3))
V(2)=CO*DOWN(3)+SI*DOWN(1)
VM1=COT*VMIS(2)-SIT*(CO*VMIS(1)-SI*VMIS(3))
VM2=CO*VMIS(3)+SI*VMIS(1)
TS(3)=(VM2-V(2))/RANGE

```

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TS(+)= (V(1)-V(11))/RANGE
DO 22 I=1,3
  B(I)=E(I)/1000
  V(I)=V(1)/1000
  IF(.NOT.TAP5) RETURN
  PRINT(5,450)X,XOWN(1),VOWN(1),XMIS(1),VMIS(1),AMIS(1),
  .ALPCH(1),ALYAW(1)
  PRINT(5,451) XOWN(2),VOWN(2),XMIS(2),VMIS(2),AMIS(2),
  .ALPCH(2),ALYAW(2)
  PRINT(5,451) XOWN(3),VOWN(3),XMIS(3),VMIS(3),AMIS(3),
  .ALPCH(3),ALYAW(3)
  PRINT(4,15)X,TS(1),TS(2),TS(3),TS(5),TS(7),Y(8),Y(4)
  PRINT(5,455)
  PRINT(5,550)X,MCL(1),MIS(1),LOS(1),ALOS(1),ANCL(1),WIN(1)
  PRINT(6,551) MCL(2),MIS(2),LOS(2),ALOS(2),ANCL(2),WIN(2)
  PRINT(6,551) MCL(3),MIS(3),LOS(3),ALOS(3),ANCL(3),WIN(3)
  PRINT(6,455)
455 FORMAT(7,2X,"...")
551 FORMAT(15X,5(G9.2,2X))
451 FORMAT(15X,9(G9.2,2X))
510 FORMAT(5X,9(G9.2,2X))
450 FORMAT(5X,9(G9.2,2X))
  RETURN
END
SUBROUTINE NOISE(RMSCOR,XMEAN,CORRJP)
  *****
  SURROUTINE NOISE GENERATES THE TFIH MODEL NOISES
  FOR FIRST ORDER LAG NOISE,
  RMSCOR=(1+DT)**.5 WHERE DT IS THE EULER INTEGRATION TIME STEP
  *****
  GAUSS=0.
  DO 10 I=1,12
    GAUSS=GAUSS+RANF(DUM)
  CONTINUE
  GAUSS=GAUSS-.5.

```

10

CORRUP=GAUSS+RMSCORR+XMEAN
RETURN
END

SUBROUTINE CROSS(D,E,F,DX,IT)
 SUBROUTINE CROSS WILL CROSS TWO VECTORS, A X B = C,
 WHERE C IS A PRODUCED UNIT VECTOR. ZERO VECTORS OR COLINEAR
 VECTORS ARE NOT ALLOWED.
 IF "IT" DOES NOT EQUAL AN INTEGER 0, THEN SUBROUTINE CROSS
 WILL PERFORM THE EULER VECTOR UPDATE
 $R(T+1) = B(T) + (A(T) \times B(T)) \cdot DX$

```

10 DIMENSION A(3),B(3),C(3),D(3),E(3),F(3)
20 DOUBLE PRECISION A,B,C,CN
30 DO 5 I=1,3
40 A(I)=C(I)
50 B(I)=E(I)
60 C(1)=A(2)*B(3)-A(3)*B(2)
70 C(2)=A(3)*B(1)-A(1)*B(3)
80 C(3)=A(1)*B(2)-A(2)*B(1)
90 IF(17.EC.0) GO TO 40
100 DO 30 I=1,3
110 C(I)=C(I)*DX+B(I)
120 CH=DSQRT(C(1)**2+C(2)**2+C(3)**2)
130 DO 10 I=1,3
140 F(I)=C(I)/CN
150 RETURN
160 END

```

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SUBROUTINE OXCOVAR(N,DT)
COMMON/SITE/PI(11,11),B2(11,11),P4(11,11),B5(6,6),B7(11)
COMMON/SITE1A/V(3),A(3)
COMMON/SITE2/COT2,SIT2,COA2,SIA2,COA1,SIA1,VM,R,B,G,AD,COT1,SIT1
COMMON/SITE3/O(11,11),F(11,11),X(11),FP(11,11)
DIMENSION XOT(8)

C OXCOVAR PROPAGATES THE FILTER STATES AND THE FILTER COVARIANCE.
C FMAT IS USED TO PROPAGATE THE FILTER COVARIANCE.
C N IS THE NUMBER OF STEPS IN TIME INTERVAL DT.
C

DO 100 IOLD=1,N
COT1=COS(X(1))
SIT1=SIN(X(1))
COT2=COS(X(2))
SIT2=SIN(X(2))
A2=ATAN(-(V(1)+X(4)*X(5))/(V(3)+X(5)))
COA2=COS(A2)
SIA2=SIN(A2)
A1=ATAN((V(2)-X(3)+X(5))/(V(3)+X(5)))*COA2-(V(1)+X(4)+X(5))*SIA2)
COA1=COS(A1)
SIA1=SIN(A1)
VM=SORT((V(1)+X(4)+X(5))*2+(V(2)-X(3)+X(5))*2+(V(3)+X(5))*2)
AO=R/X(11)*SORT((VM**3+B)*2*X(11)*(X(7)**2+X(8)**2)/(R+B*V1*57.3)
CALL FMAT
CALL MOPY(F,FP,B1,11,11)
CALL MTRAN(11,11,B1,B2)
CALL MADD(11,11,B1,B2,B1)
CALL MADD(11,11,B1,B1)
DO 17 J=1,11
DO 17 I=J,11
FP(I,J)=FP(I,J)+B1(I,J)*DT/N
17 FP(J,I)=FP(I,J)
XOT(1)=X(3)/COT2
XOT(2)=X(4)
XOT(3)=(AO*SIA1-X(8)*COA1+1(2)-2*X(3)*X(5)+X(3)*X(4)+X(5)*SIT2/COT

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      2+G*DOT1)/X(3)
      XDT(4)=(X(7)*COF2+SIA2*(SIA1*X(8)+A3*COA1)-G*DOT2-A(1)-2*X(4)*X(5)
      -X(3)*2*X(3)*SIT2/DOT2-G*SIF2*SIT1)/X(5)
      XDT(5)=X(3)
      XDT(6)=X(7)-SIA2-COA2*(X(6)*SIA1+A3*COA1)-G*SIT2-A(3)+X(5)*(X(3)+*
      2+X(4)*2)+G*DOT2*SIT1
      XDT(7)=(X(4)*X(6)+X(9)-X(7))/X(10)
      XDT(8)=-((X(3)+X(6)+X(9)+X(5))/X(10)
      CO 18 I=1,3
      19 X(I)=X(I)+XDT(I)*DT/N
      100 CONTINUE
      RETURN
      END

```

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SUBROUTINE FMAT
COMMON/SITE11/V(3),A(3)
COMMON/SITE2/COT2,SIT2,COA2,SIA2,COA1,SIA1,VM,R,B,G,AD,COT1,SIT1
COMMON/SITE3/7(11,11),F(11,11),X(11),FP(11,11)

SUBROUTINE FMAT EVALUATES THE F PARTIALS, WHICH ARE
NEEDED TO PROPAGATE THE COVARIANCE MATRIX

AD7 IS THE PARTIAL OF DRAS WITH RESPECT TO X(7)
AD8 IS THE PARTIAL OF DRAS WITH RESPECT TO X(8)
AD11 IS THE PARTIAL OF DRAS WITH RESPECT TO X(11)
X IS THE FILTER STATES, F IS THE PARTIALS MATRIX, V IS THE
VELOCITY OF THE TRACKER, A IS THE ACCELERATION OF THE TRACKER

AD7=X(7)*(4*X(11)/(R*B*VM*57.3))
AD8=X(8)*(4*X(11)/(R*B*VM*57.3))
AD11=-R*SQRT(VM*3*R)/X(11)*2+2*(X(7)*2+X(8)*2)/(R*B*VM*57.3)

F(1,2)=X(3)*SIT2/COT2+2
F(1,3)=1/COT2
F(2,4)=1
F(3,1)=-G*SIT1/X(5)
F(3,2)=X(3)*X(4)/COT2+2
F(3,3)=-2*X(5)/X(5)+X(4)*SIT2/COT2
F(3,4)=X(3)*SIT2/COT2
F(3,5)=-AD7*SIA1-X(6)*COA1+A(2)+3*COT1-2*X(3)+X(6)/X(5)+2
F(3,6)=-2*X(3)/X(5)
F(3,7)=AD7*SIA1/X(5)
F(3,8)=AD7*SIA1/X(5)-COA1/X(5)
F(3,11)=AD11*SIA1/X(5)
F(4,1)=-G*SIT2*COT1/X(5)
F(4,2)=G*(SIT2-COT2*SIT1)/X(5)-X(3)+2/COT2+2
F(4,3)=-2*X(3)*SIT2/COT2
F(4,4)=-2*X(3)/X(5)
F(4,5)=-X(7)*COA2+SIA2*(SIA1*X(8)+AD*COA1)-G*COT2-A(1)-2*X(5)
*X(4)-G*SIT2*SIT1/X(5)+2
F(4,6)=-2*X(4)/X(5)

000130
000130
000200
000220
000230
000240

000260
000270
000280
000290

000310
000320
000330
000350

000360
000370
000380
000390

000410
000420
000430
000440
000450
000460

F(4,7)=(COA2+STA2+COA1+AD7)/X(5)
F(4,8)=SIA2/X(5)*(SIA1+COA1+AD8)
F(4,11)=SIA2+COA1+AD11/X(5)
F(5,6)=1
F(5,1)=G*CO11*CO12
F(5,2)=-G*(CO12+SIT2+SIT1)
F(5,3)=2*X(3)*X(5)
F(5,4)=2*X(4)*X(5)
F(5,5)=X(7)*2+X(4)*2
F(5,7)=SIA2+COA2+COA1+AD7
F(5,8)=-COA2*(SIA1+COA1+AD8)
F(5,11)=-COA2+COA1+AD11
F(7,4)=X(1)*X(9)/X(10)
F(7,6)=X(1)*X(9)/X(10)
F(7,7)=-1/X(10)
F(7,9)=X(4)*X(6)/X(10)
F(7,10)=-X(4)*X(6)*X(9)-X(7)/X(10)*2
F(8,3)=-X(5)*X(7)/X(10)
F(8,6)=-X(3)*X(9)/X(10)
F(8,8)=F(7,7)
F(8,9)=-X(3)*X(6)/X(10)
F(8,10)=(X(3)+X(6)*X(9)+X(8))/X(10)*2
RETURN
END

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```

C
C
C
SUBROUTINE DYGAIN
*****
SUBROUTINE DYGAIN COMPUTES THE KALMAN FILTER GAIN
*****
COMMON/SITE/A1(11,11),A2(11,11),A4(11,6),A5(6,6),A7(11)
COMMON/SITE3/O(11,11),F(11,11),FS(11),FP(11,11)
COMMON/SITE5/EK(11,6)
COMMON/SITE5/H(6,11),P(6,6)
CALL MTRAN(6,11,H,FK)
CALL NMPY(FP,FK,A4,11,11,6)
CALL NMPY(H,A6,A5,6,11,6)
CALL MADD(6,6,A5,R,A5)
CALL MINV(A5,A5,6)
CALL NMPY(A4,A5,FK,11,6,6)
RETURN
END

```

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```

SUBROUTINE DXPPLUS
COMMON/SITE/A1(11,11),A2(11,11),A7(11,6),A5(6,6),A7(11)
COMMON/SITE3/O(11,11),F(11,11),X(11),FP(11,11)
COMMON/SITE5/FK(11,6)
COMMON/SITE6/H(6,11),R(6,5)
SUBROUTINE DXPPLUS PERFORMS THE MEASUREMENT UPDATE OF THE
COVARIANCE MATRIX.
*****
CALL MPMY(FK,H,A1,11,6,11)
CALL MPMY(A1,FP,A2,11,11,11)
CALL MSUT(11,11,FP,A2,FP)
RETURN
END

```

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```

SUBROUTINE DXSPLUS
COMMON/SITE/A1(11,11),A2(11,11),A4(11,6),A5(6,6),A7(11)
COMMON/SITE3/7(11,11),F(11,11),FS(11),FP(11,11)
COMMON/SITE4/MEAS(6)
COMMON/SITE5/FK(11,6)
DIMENSION DIFF(6)
REAL MEAS
*****
SUBROUTINE DXSPLUS PERFORMS THE MEASUREMENT UPDATE OF THE
STATE ESTIMATES.
*****
DO 1 I=1,6
DIFF(I)=MEAS(I)-FS(I)
CONTINUE
CALL NMPY(FK,DIFF,A7,11,6,1)
CALL PADD(11,1,FS,A7,FS)
RETURN
END

```

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```

C
C
C
SUBROUTINE REED(FSDUM,FPDUM,RDUM,ODUM,N,RN)
DIMENSION FSDUM(N),FPDUM(N),RDUM(N),ODUM(N,N)
INTEGER N,RN
*****
SUBROUTINE REED READS THE VALUES REQUIRED BY EIGEN.
*****
READ*,RN
DO 1 I=1,N
  READ*,FSDUM(I)
CONTINUE
DO 3 J=1,N
  DO 2 I=1,N
    FPDUM(I,J)=0
    IF(I.EQ.J) READ*,FPDUM(I,J)
  CONTINUE
CONTINUE
DO 5 J=1,N
  DO 4 I=1,N
    RDUM(I,J)=0
    IF(I.EQ.J) READ*,RDUM(I,J)
  CONTINUE
CONTINUE
DO 7 J=1,N
  DO 6 I=1,N
    ODUM(I,J)=0
    IF(I.EQ.J) READ*,ODUM(I,J)
  CONTINUE
CONTINUE
RETURN
END
1
2
3
4
5
6
7

```

```

C
C
C
SUBROUTINE MIPY(A,B,C,M,K,N)
*****
SUBROUTINE MIPY MULTIPLIES TWO MATRICES TO PRODUCE C(M,N)
*****
DIMENSION A(1,K),B(K,N),C(M,N)
DO 10 J=1,N
DO 10 I=1,M
S=0
DO 11 L=1,K
11 S=S+A(I,L)*B(L,J)
10 C(I,J)=S
RETURN
END

```

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```

C
C
C
SUBROUTINE MTRAN (K,N,G,GT)
  DIMENSION G(K,N),GT(N,K)
  *****
  SUBROUTINE MTRAN TRANSPOSES THE MATRIX
  *****
  DO 1 I=1,K
    DO 2 J=1,N
      GT(J,I)=G(I,J)
    1 CONTINUE
  RETURN
  END
  2

```

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```

C
C
C
SUBROUTINE MSUB(K,N,A,R,C)
  DIMENSION A(K,N),B(K,N),C(K,N)
  *****
SUBROUTINE MSUB SUBTRACTS TWO MATRICES
  *****
DO 4 J=1,N
DO 4 I=1,K
  C(I,J)=A(I,J)-B(I,J)
  RETURN
  END
4

```

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```

C
C
C
SUBROUTINE MADD(K,N,A,B,C)
  DIMENSION A(K,N), B(K,N), C(K,N)
  *****
SUBROUTINE MADD ADDS TWO MATRICES
  *****
  DO 3 J=1,N
    DO 3 I=1,K
      C(I,J)=A(I,J)+B(I,J)
    RETURN
  END
3

```

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Appendix E

This appendix contains the graphical results of the Monte Carlo analyses of the 11 State Filter. For each K Set trajectory, the filter states are initialized to the initial true values. The tuning parameters used in the filter for all K Set trajectories are (Note: The state vector is $[\theta_1, \theta_2, \omega_1, \omega_2, R_{tm}, \dot{R}_{tm}, A_{L1}, A_{L2}, n_f, \tau_f, (m/s)_f]^T$):

$$R = \begin{bmatrix} 3.E-5 & 0 & 0 & 0 & 0 & 0 \\ 0 & 3.E-5 & 0 & 0 & 0 & 0 \\ 0 & 0 & 3.E-5 & 0 & 0 & 0 \\ 0 & 0 & 0 & 3.E-5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 5.E-4 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1.E-4 \end{bmatrix}$$

$$P_o = \begin{bmatrix} 4.E-6 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 4.E-6 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 3.E-5 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 3.E-5 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 5.E-4 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1.E-4 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & .009 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 4 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & .05 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1.E13 \end{bmatrix}$$

$$Q = \begin{bmatrix} 1.E-5 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1.E-5 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1.E-5 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1.E-5 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1.E-2 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 2.E-3 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 3.E-3 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 3.E-3 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & .001 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 4.E12 \end{bmatrix}$$

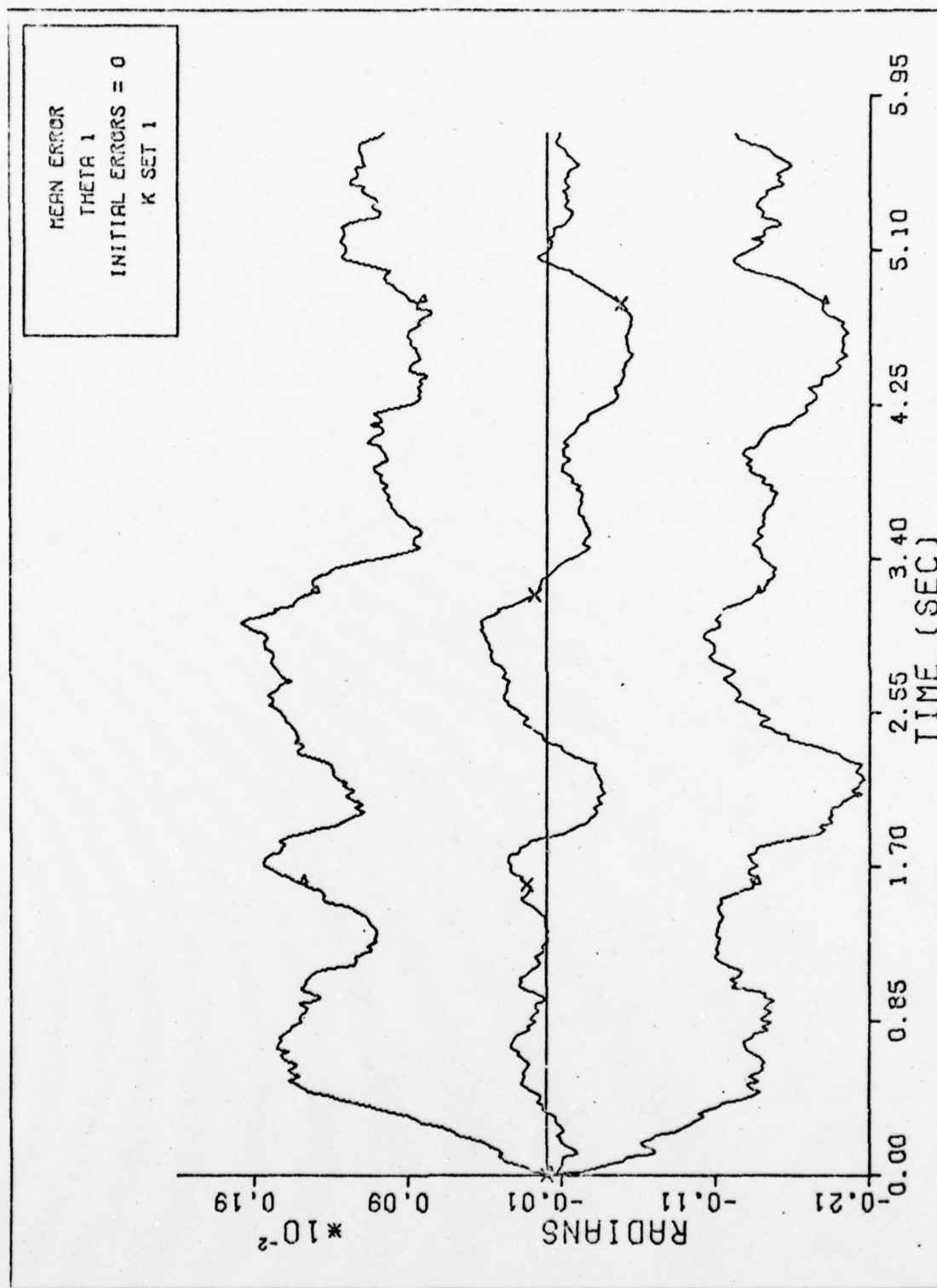


Fig. E-1

THETA 1 MEAN ERROR, L1 STATE FILTER

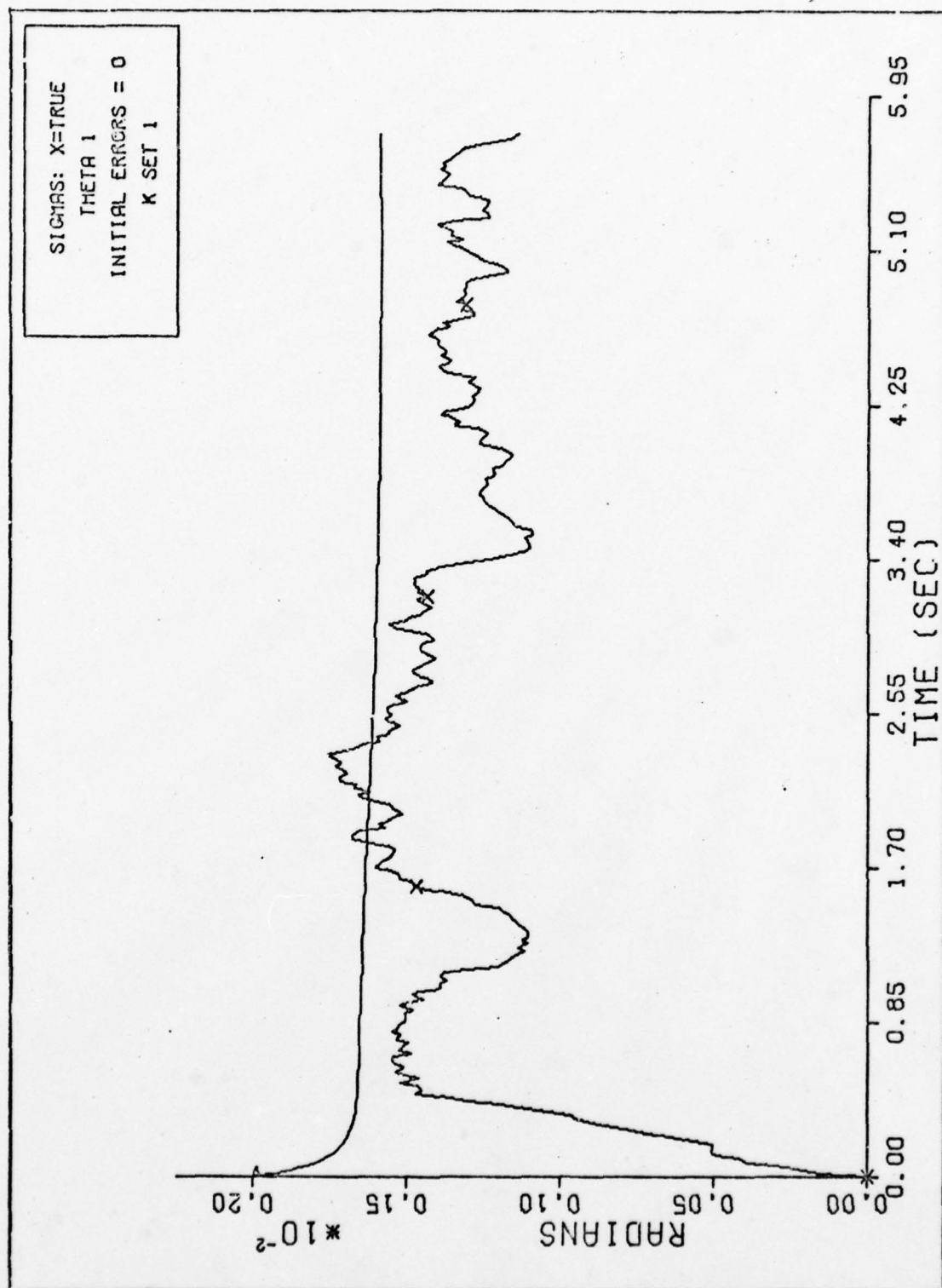


Fig. E-2 THETA 1 FILTER & TRUE SIGMAS, L1 STATE FILTER

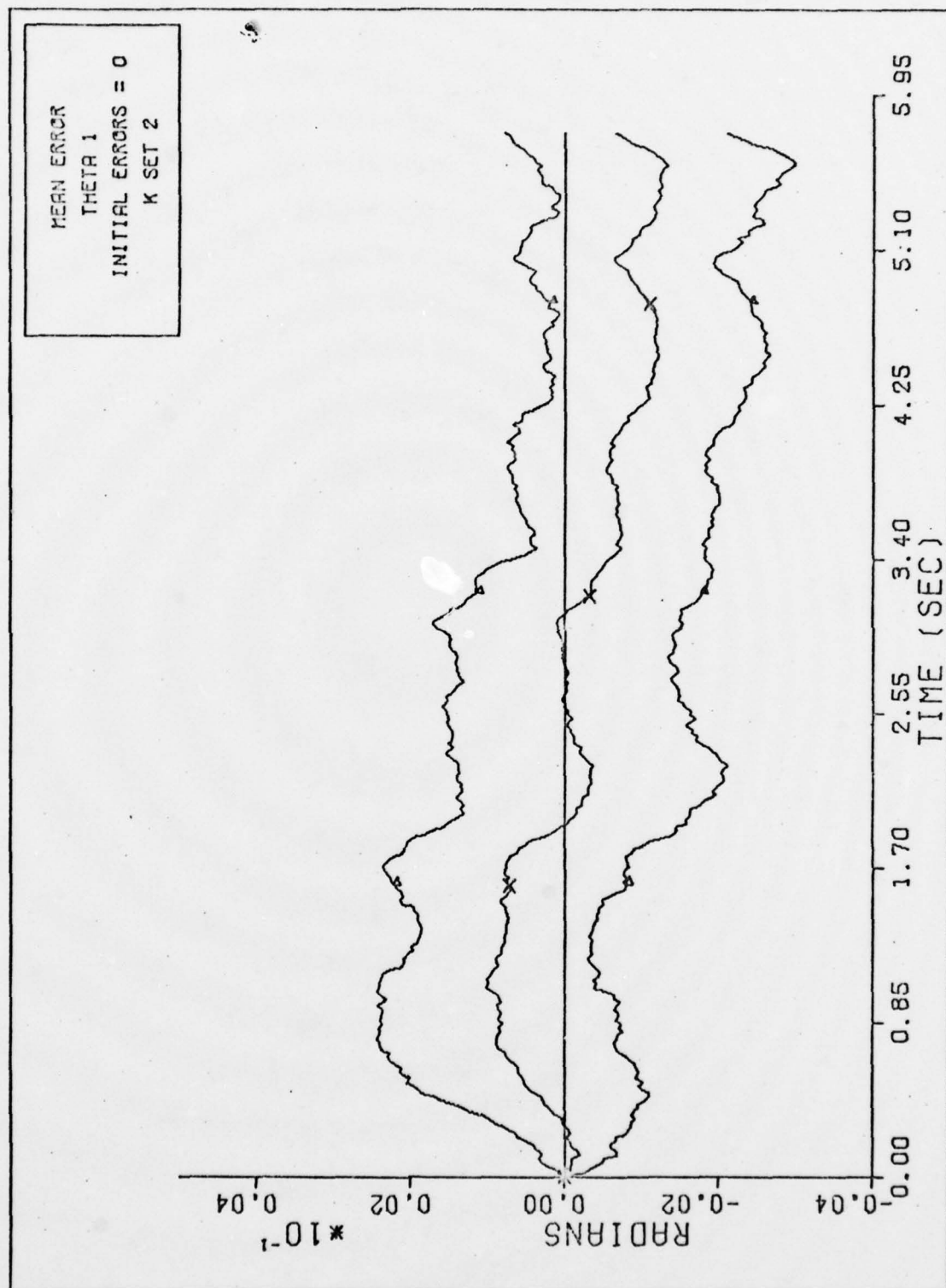


Fig. E-3

THETA 1 MEAN ERROR, L1 STATE FILTER

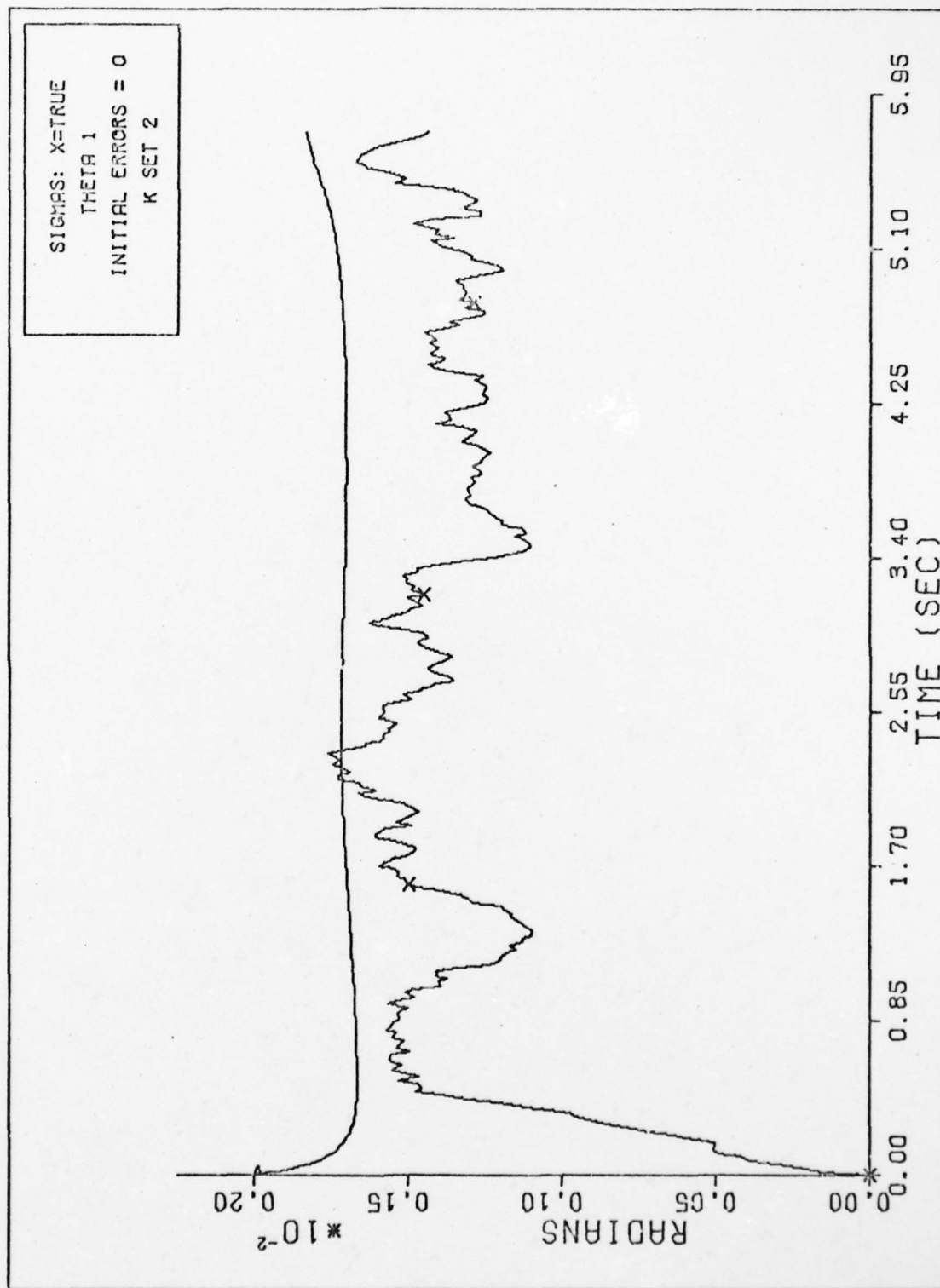


Fig. E-4

THETA 1 FILTER & TRUE SIGMAS, 11 STATE FILTER

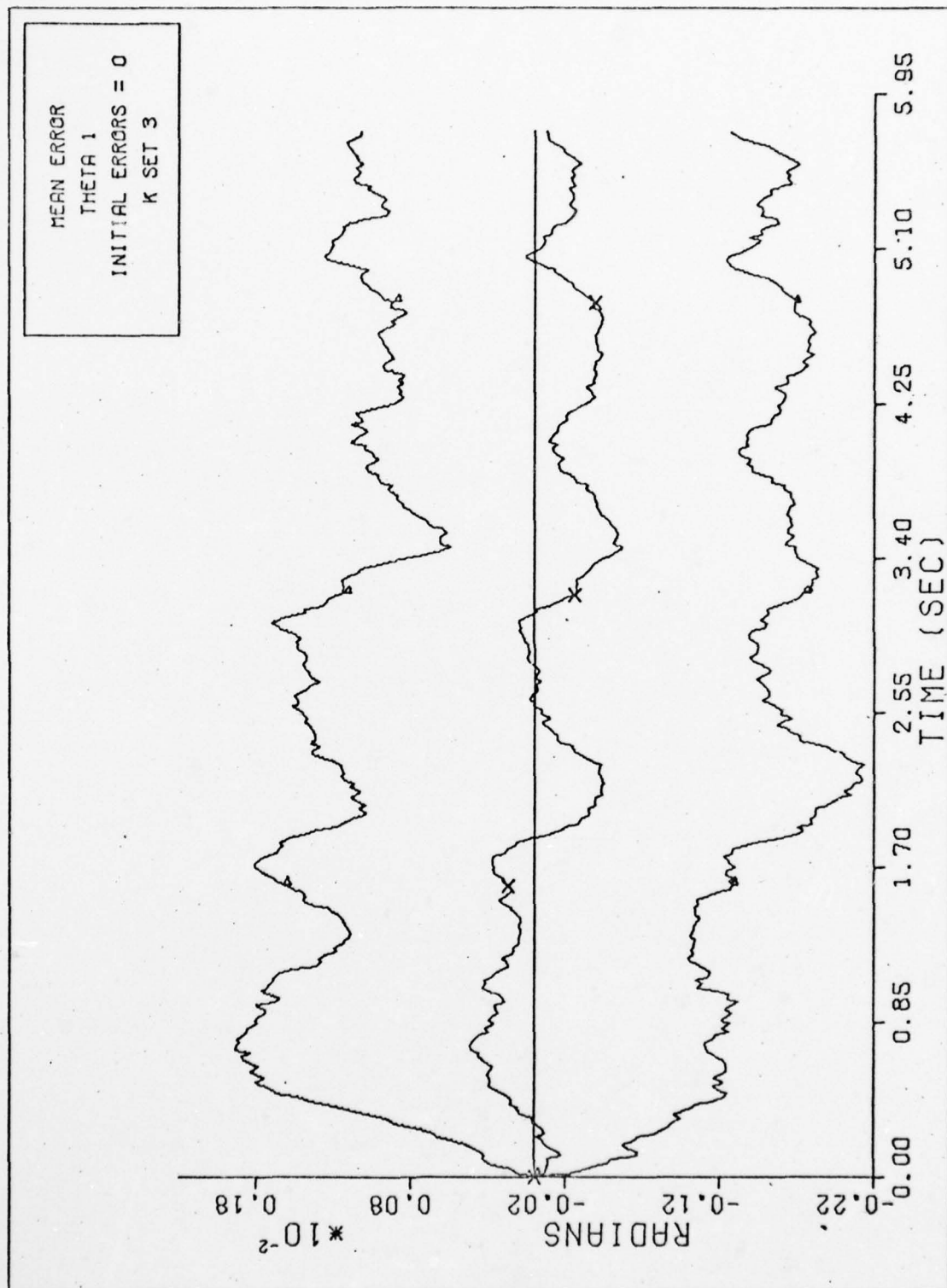


Fig. E-5

THETA 1 MEAN ERROR, L1 STATE FILTER

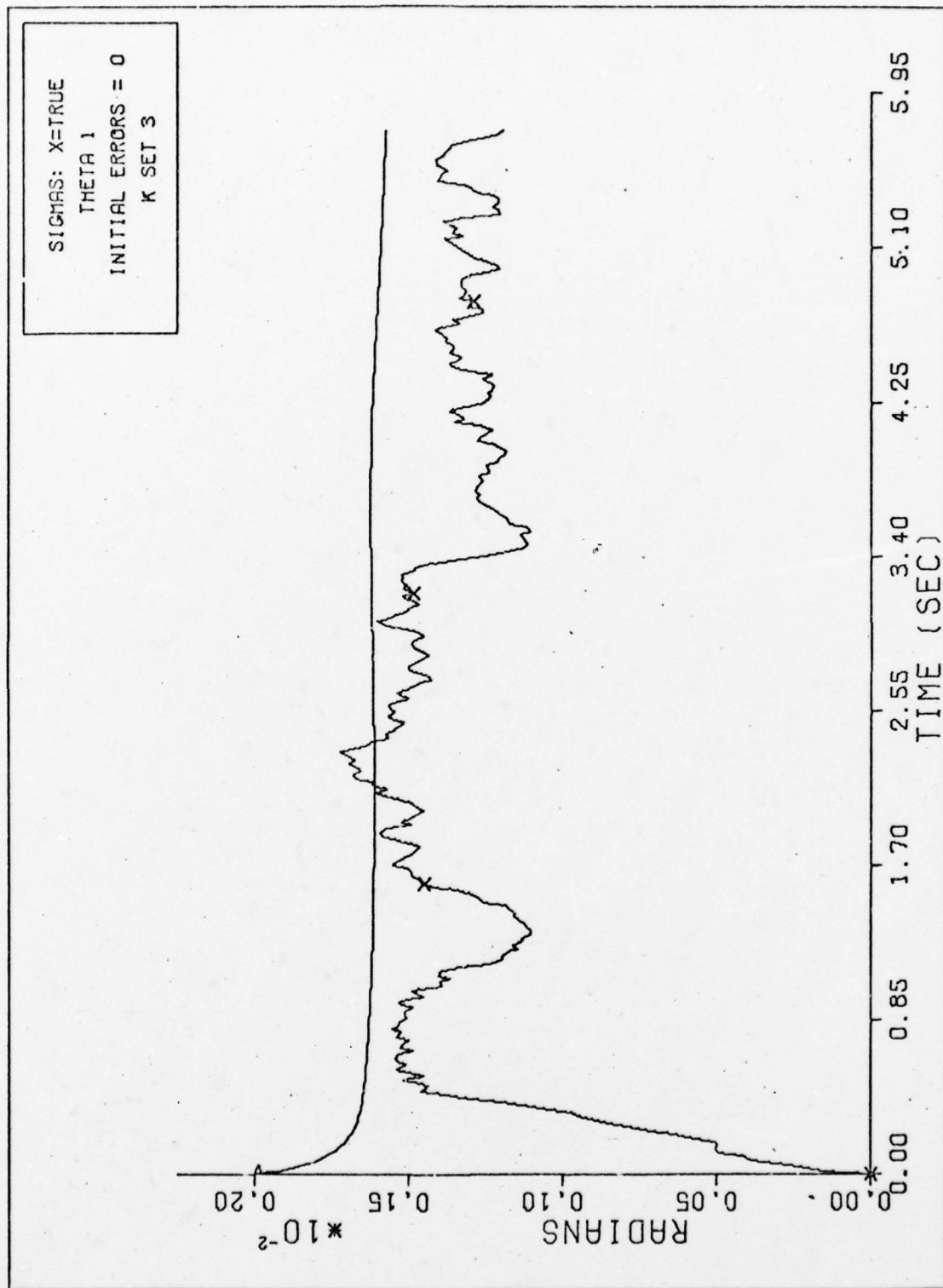


Fig. E-6 THETA 1 FILTER & TRUE SIGMAS, 11 STATE FILTER

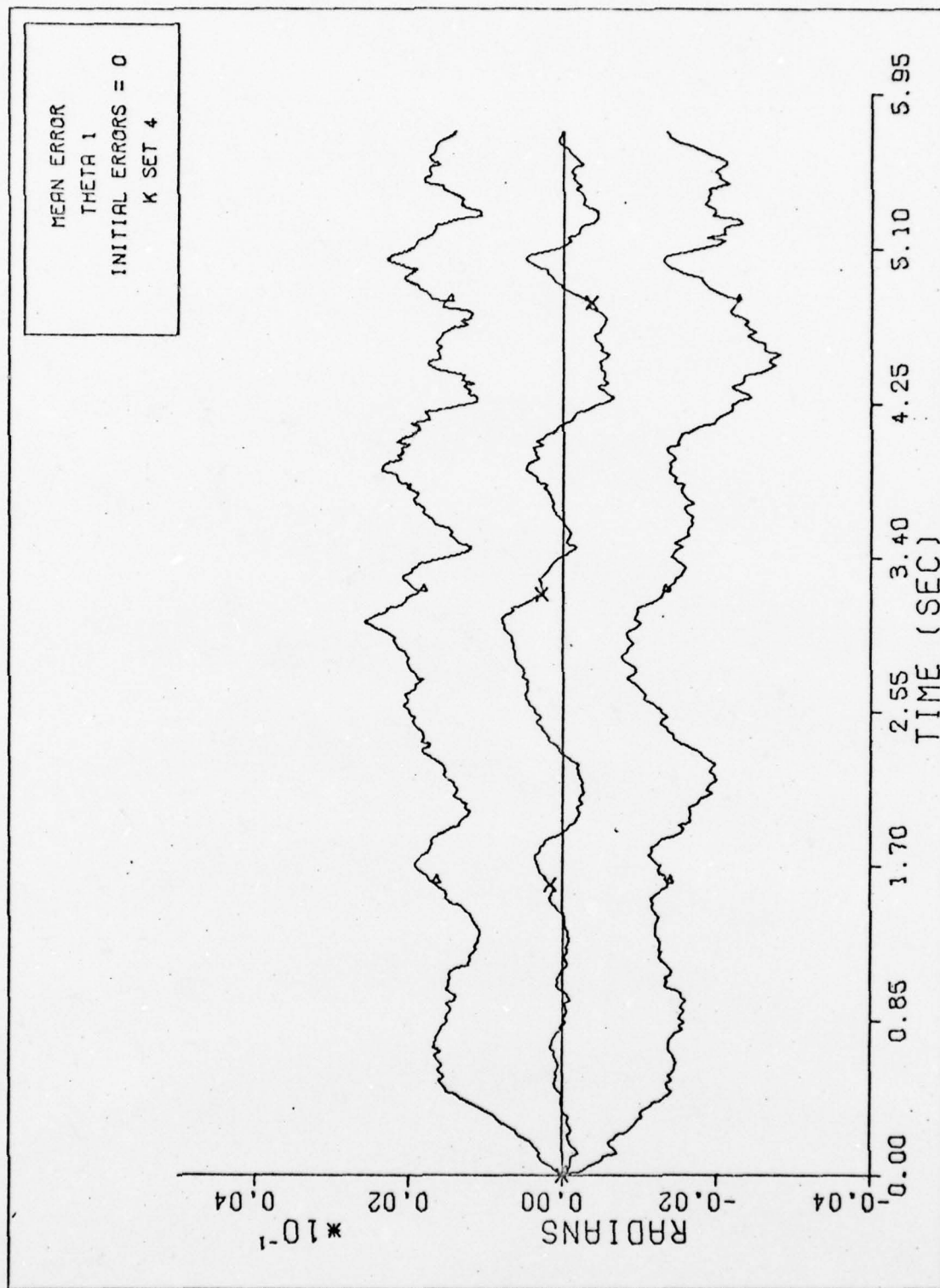


Fig. E-7

THETA 1 MEAN ERROR, 11 STATE FILTER

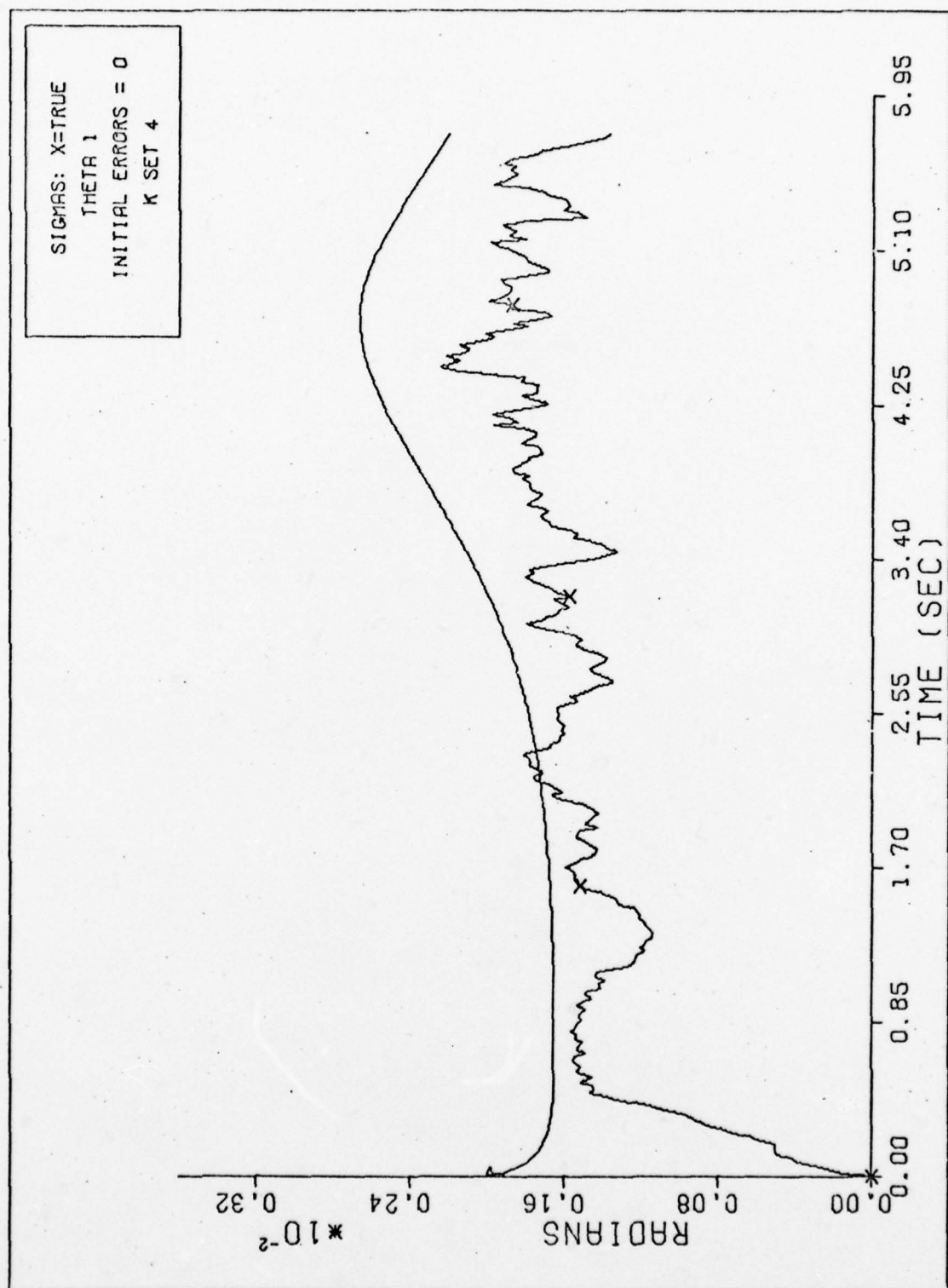


Fig. E-8 THETA 1 FILTER & TRUE SIGMAS, 11 STATE FILTER

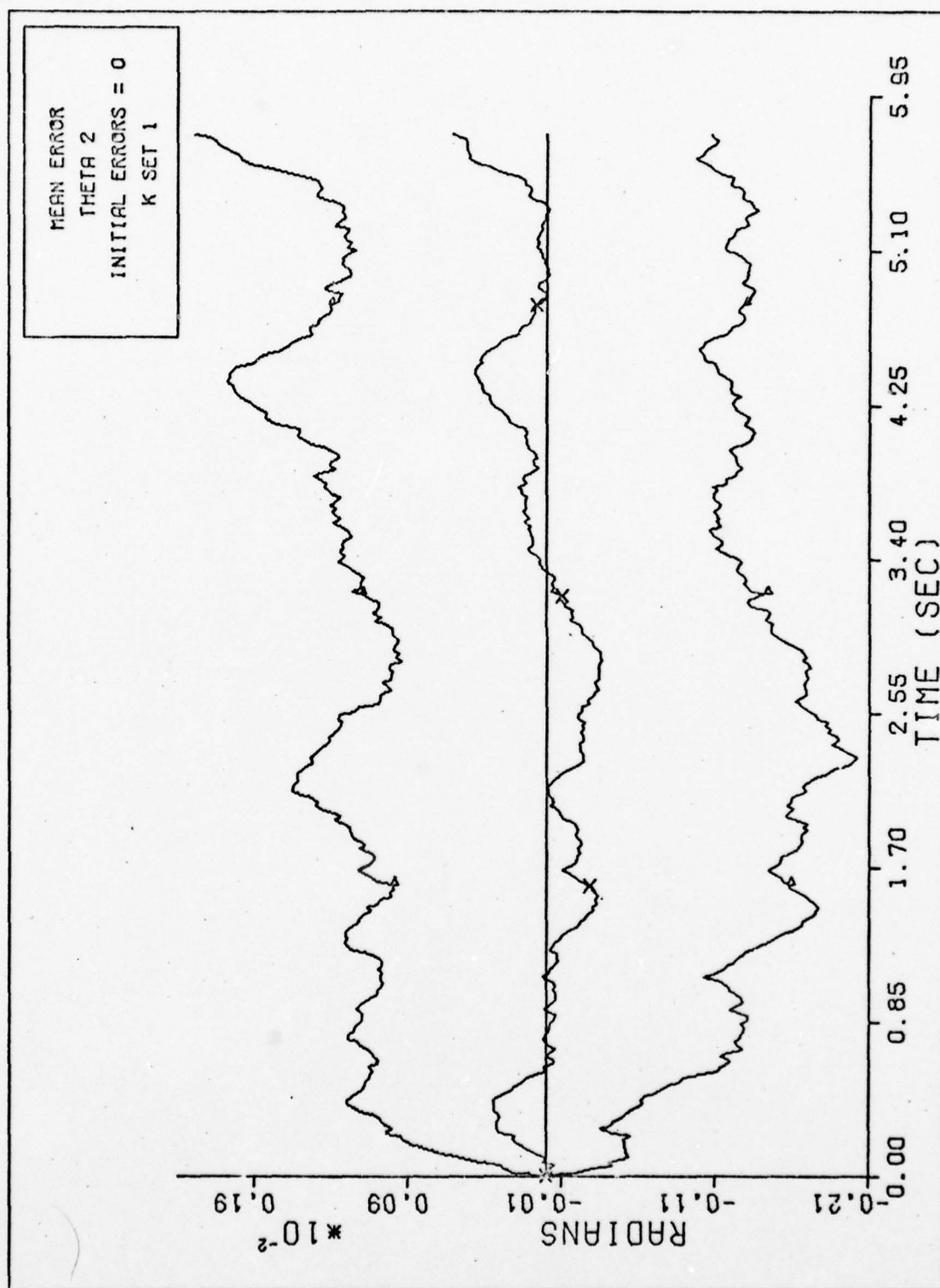


Fig. E-9

THETA 2 MEAN ERROR, L1 STATE FILTER

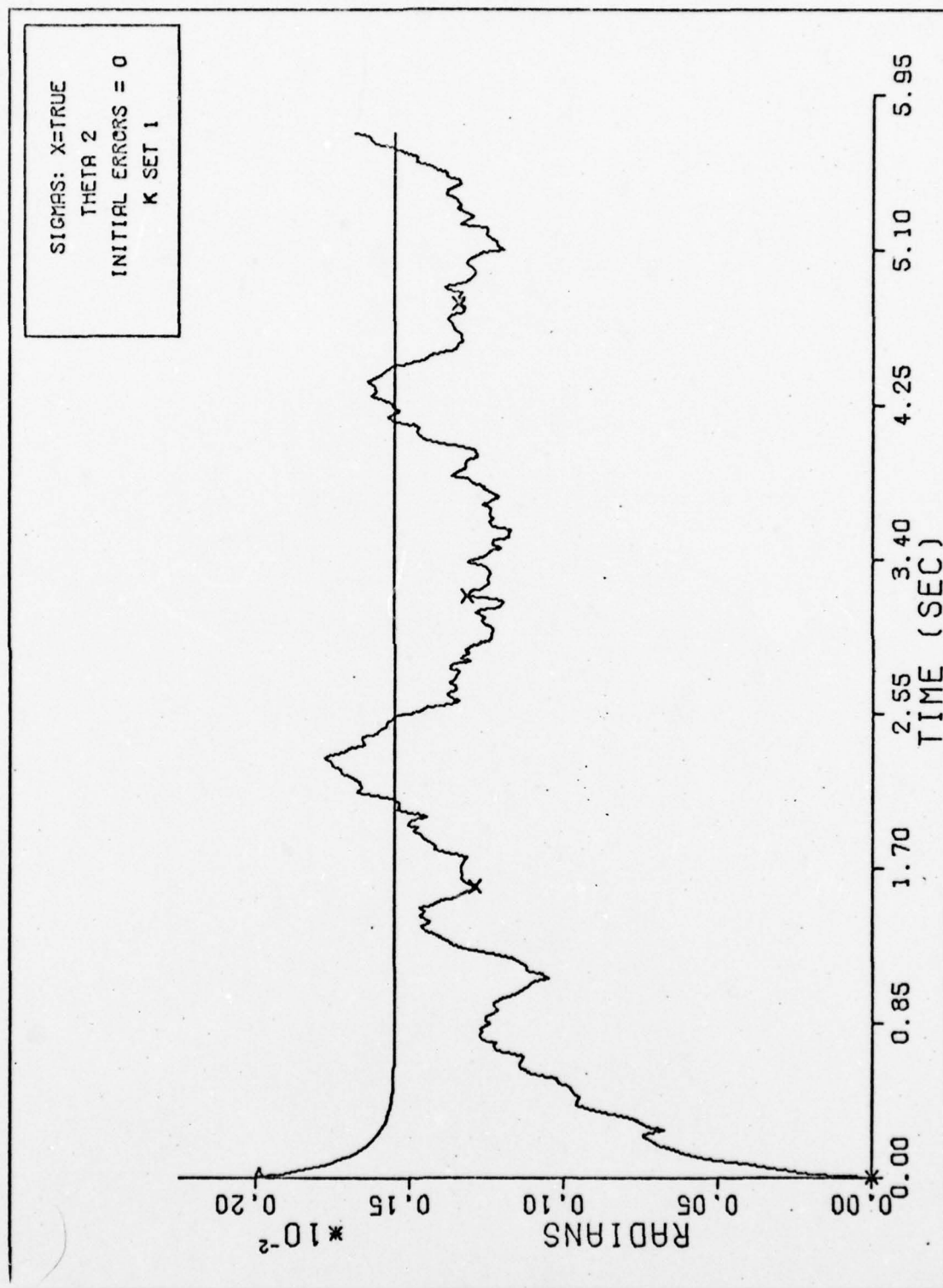


Fig. E-10 THETA 2 FILTER & TRUE SIGMAS, 11 STATE FILTER

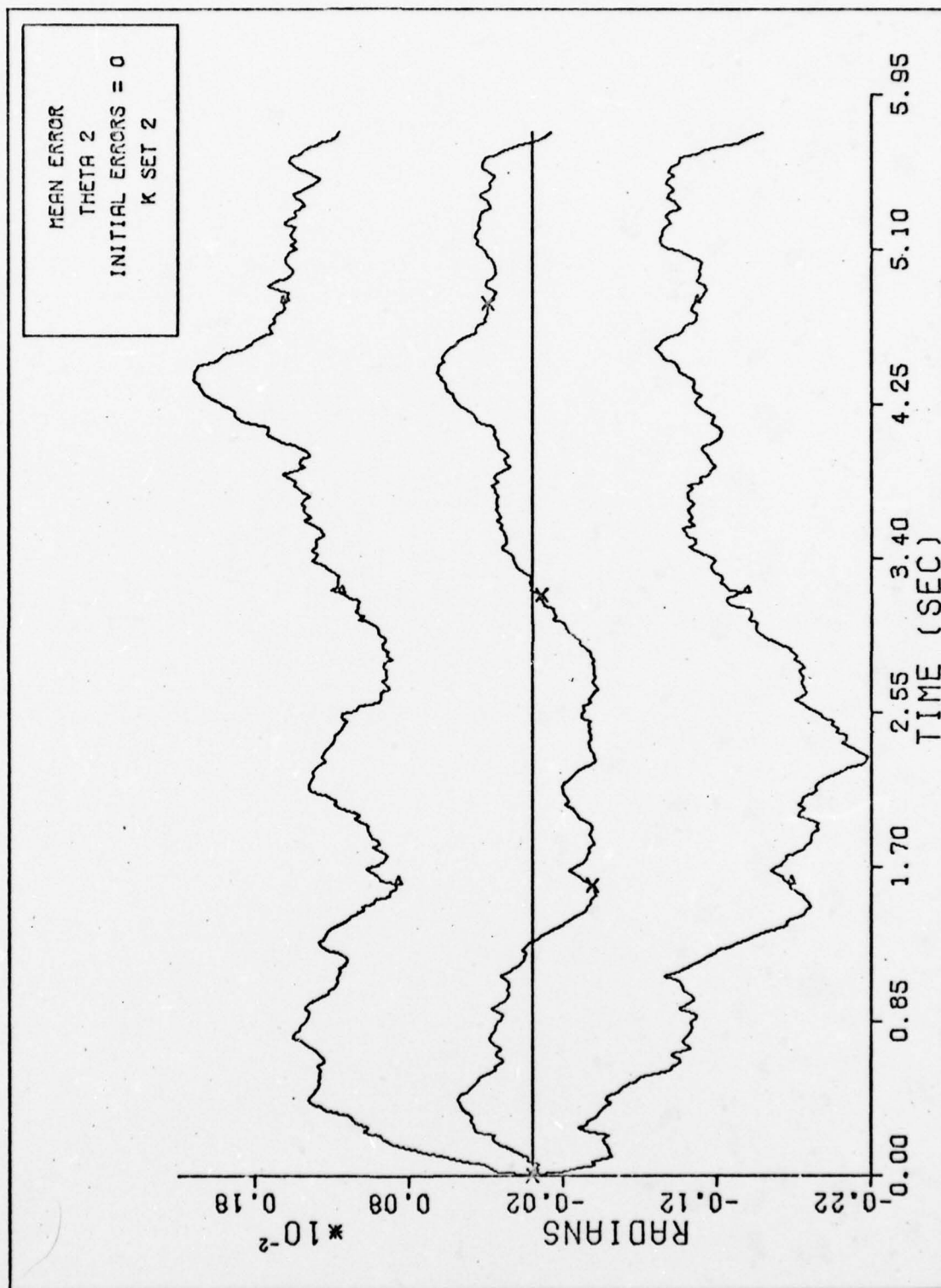


Fig. E-11

THETA 2 MEAN ERROR, L1 STATE FILTER

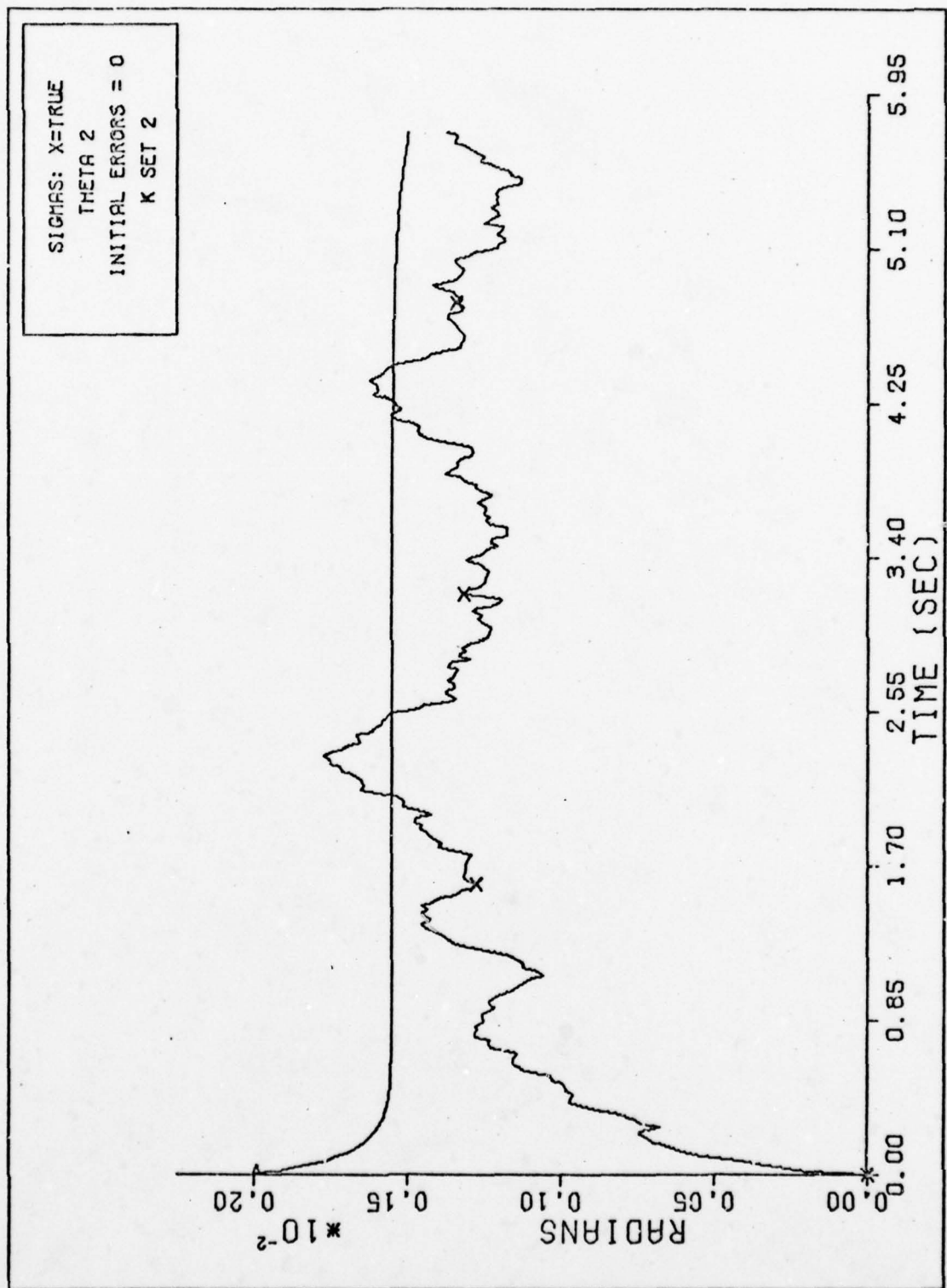


Fig. E-12 THETA 2 FILTER & TRUE SIGMAS, 11 STATE FILTER

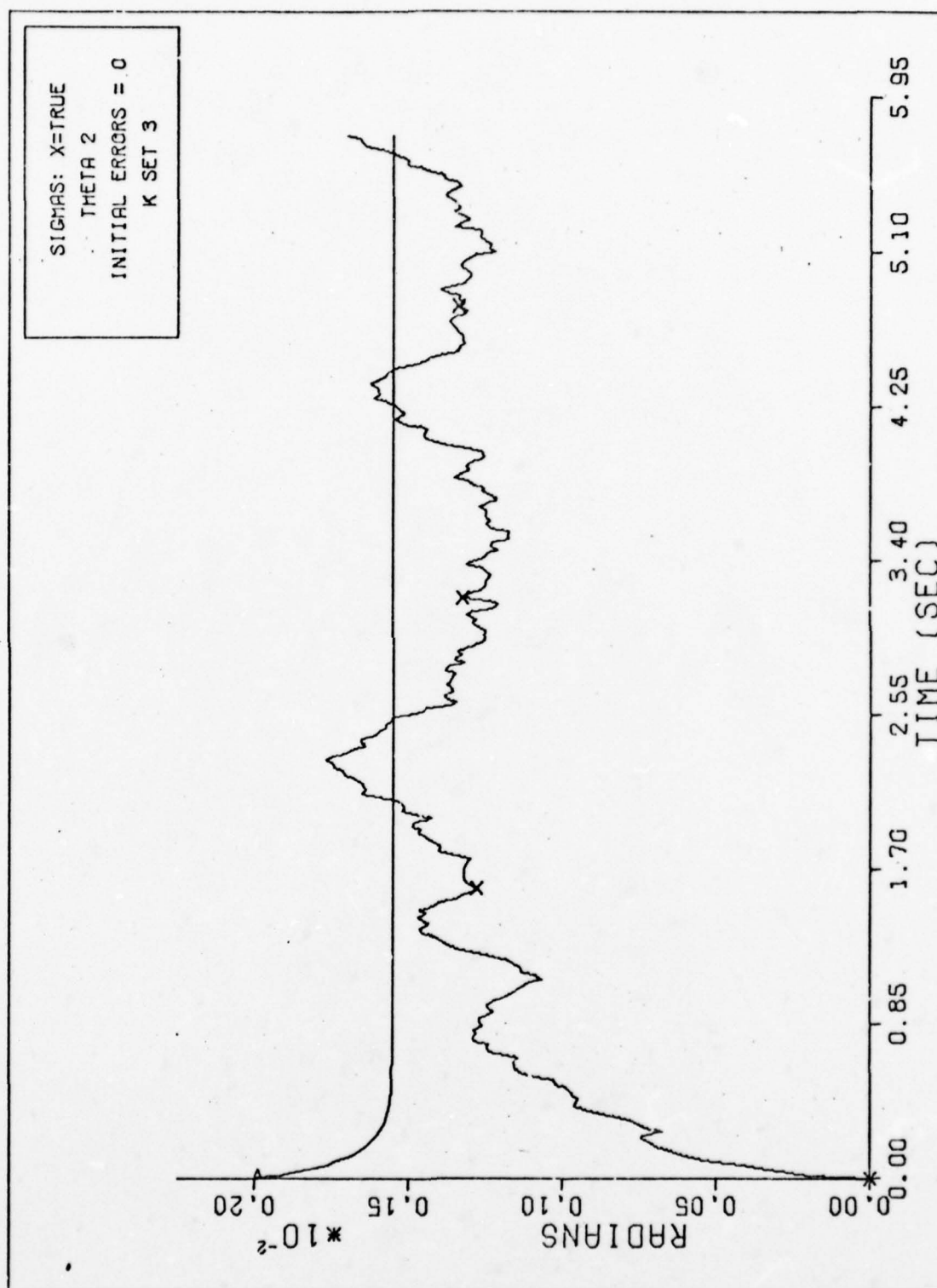


Fig. E-13 THETA 2 FILTER & TRUE SIGMAS, L1 STATE FILTER

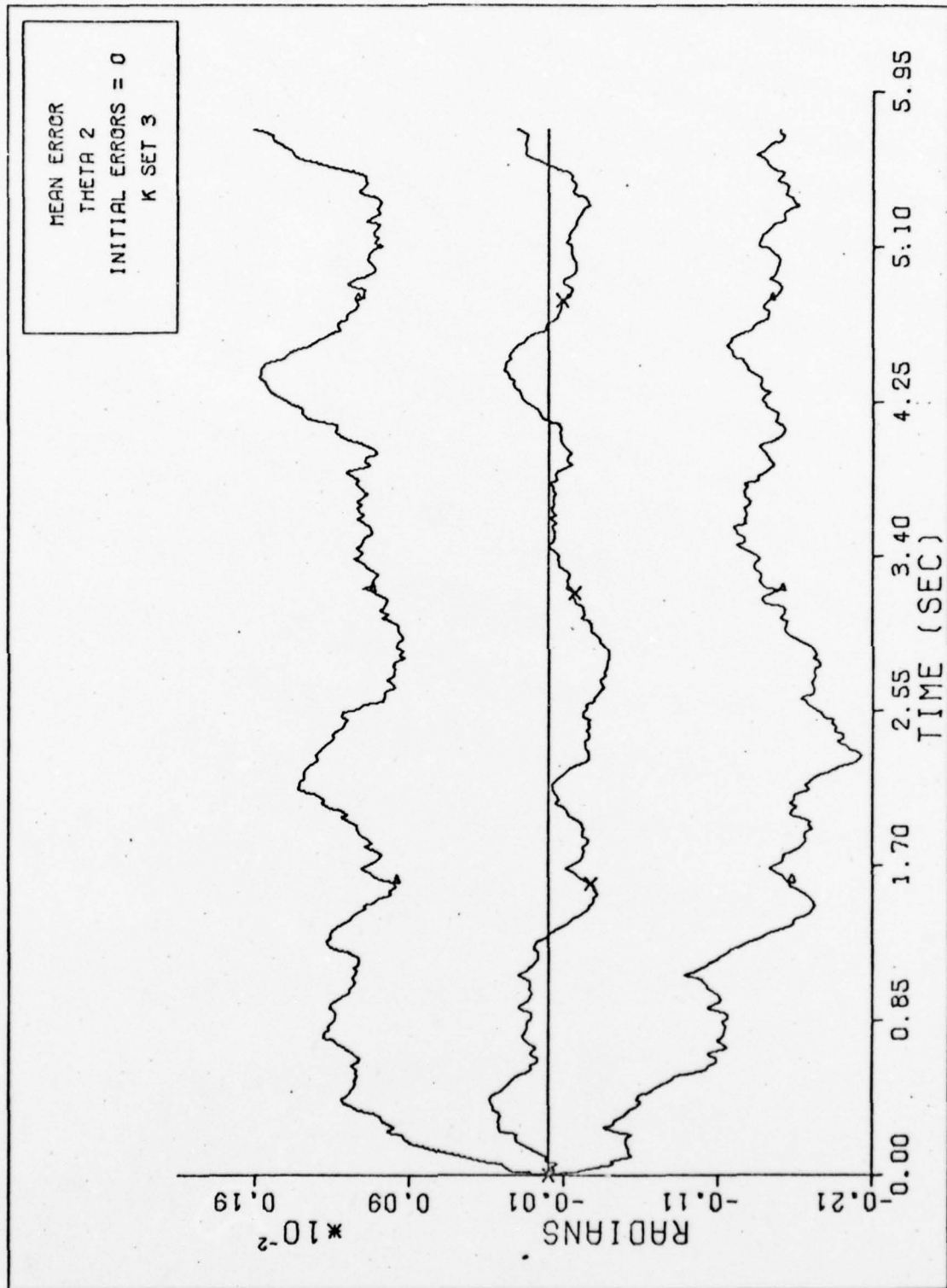


Fig. E-14

THETA 2 MEAN ERROR, 11 STATE FILTER

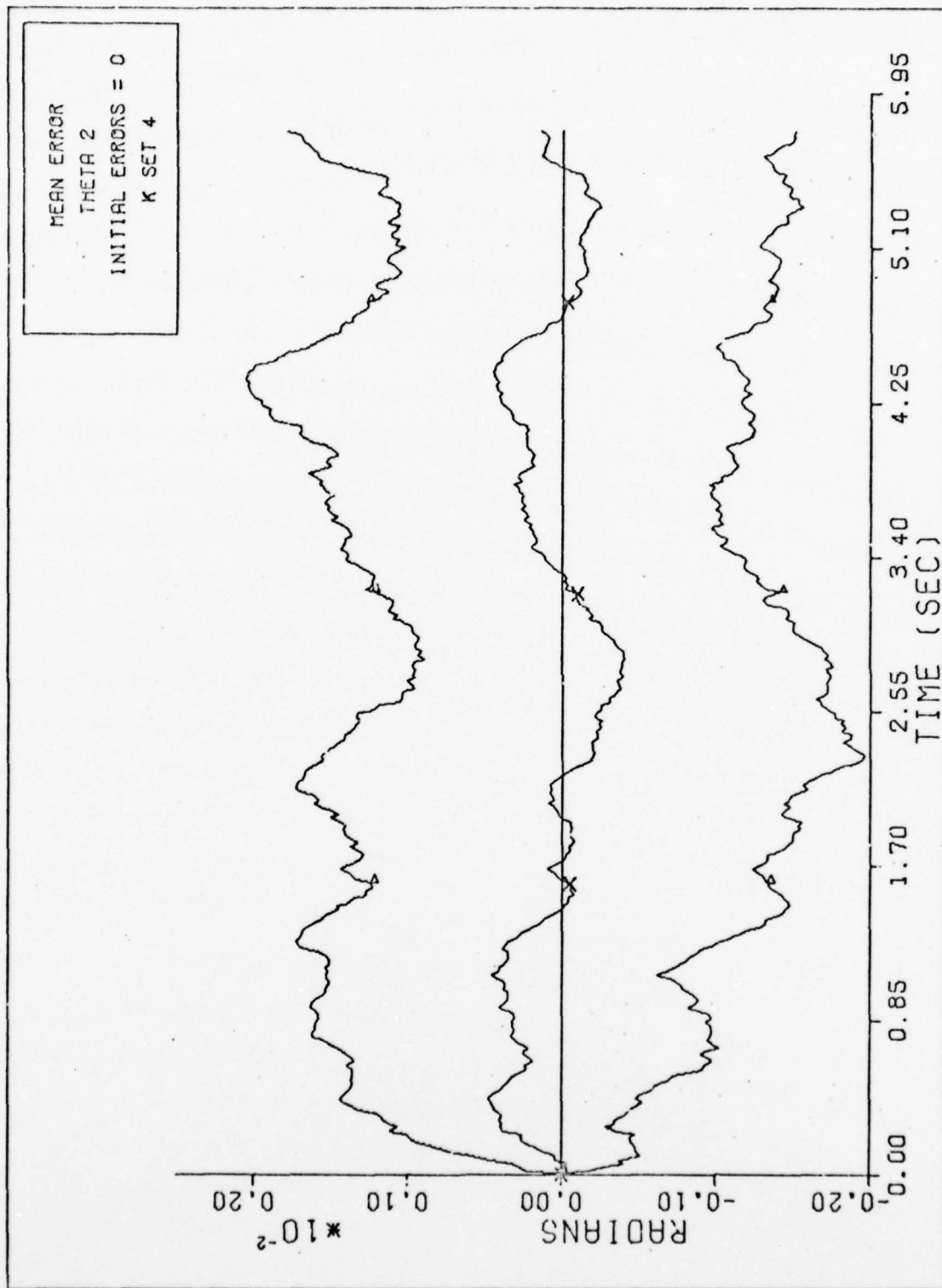


Fig. E-15

THETA 2 MEAN ERROR, L1 STATE FILTER

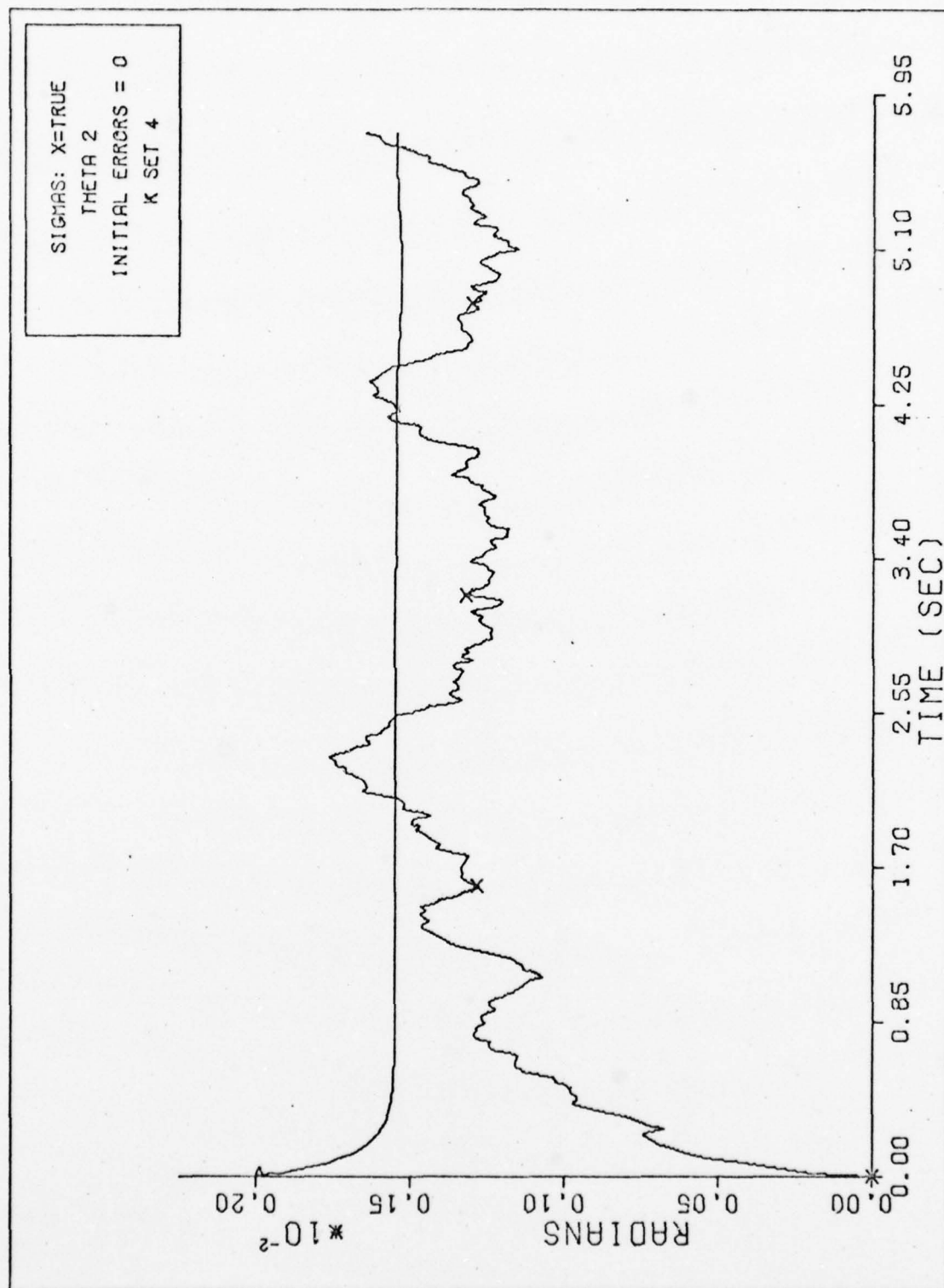


Fig. E-16 THETA 2 FILTER & TRUE SIGMAS, 11 STATE FILTER

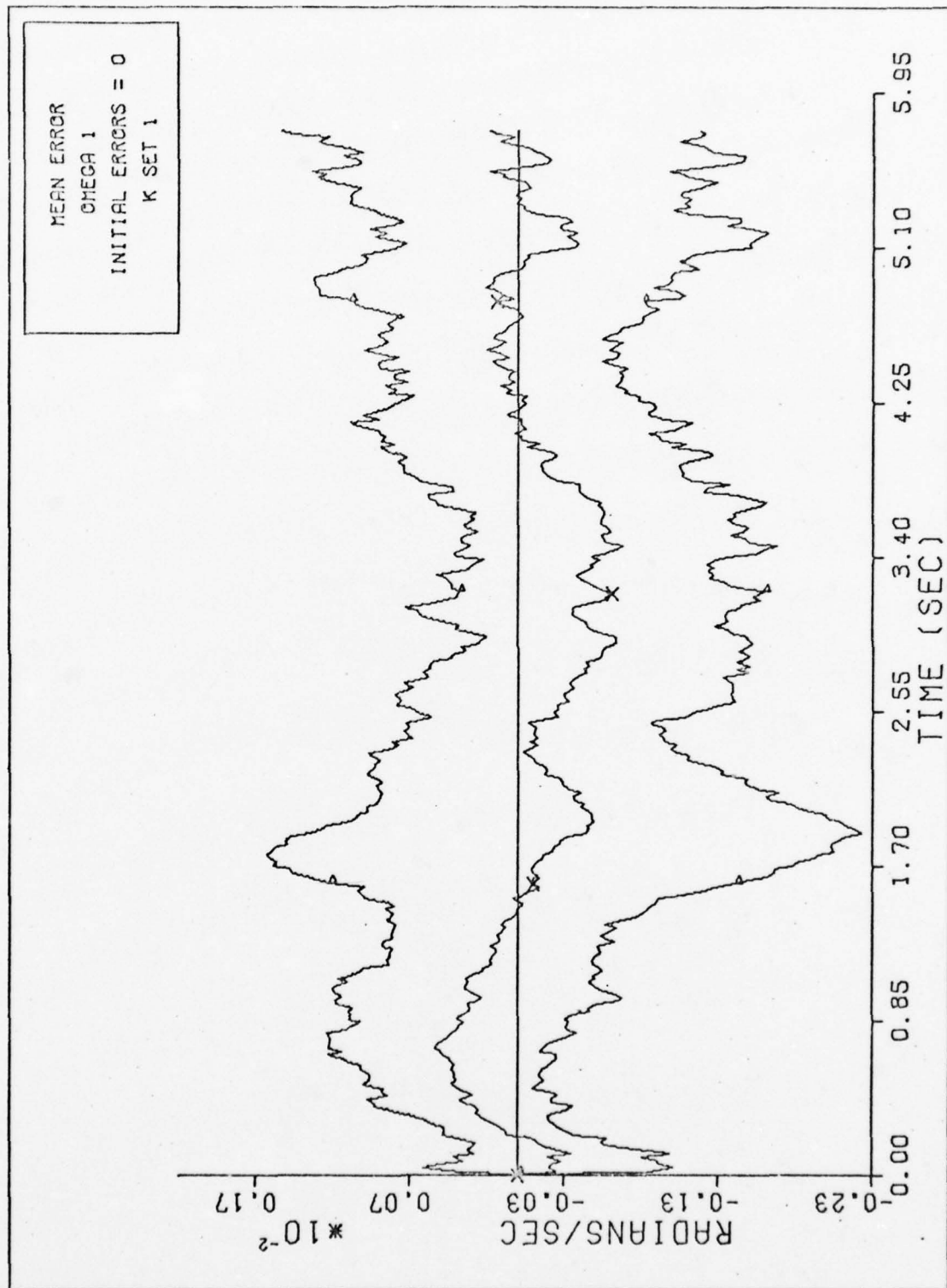


Fig. E-17

OMEGA 1 MEAN ERROR, 11 STATE FILTER

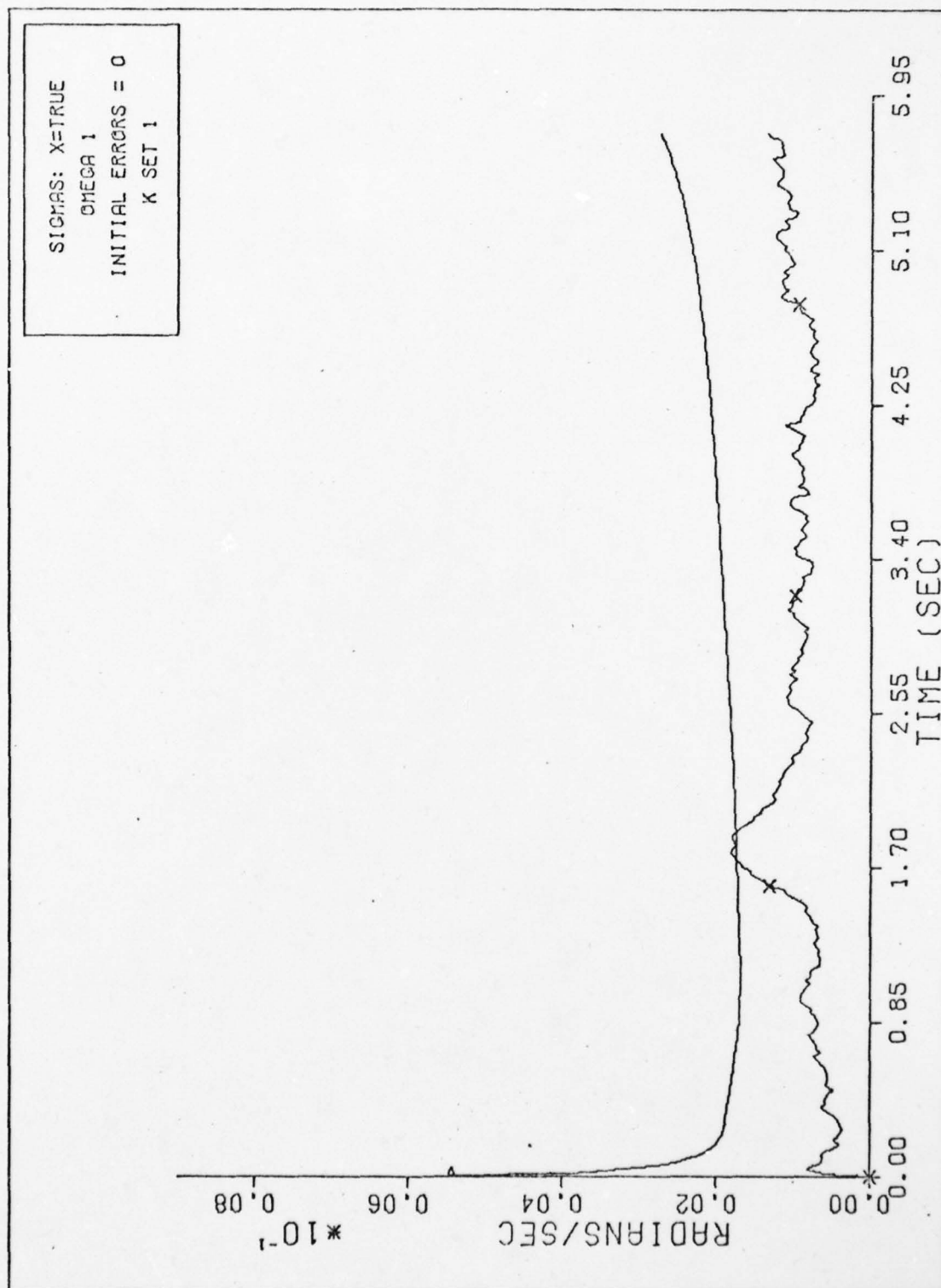


Fig. E-18 OMEGA 1 FILTER & TRUE SIGMAS, 11 STATE FILTER

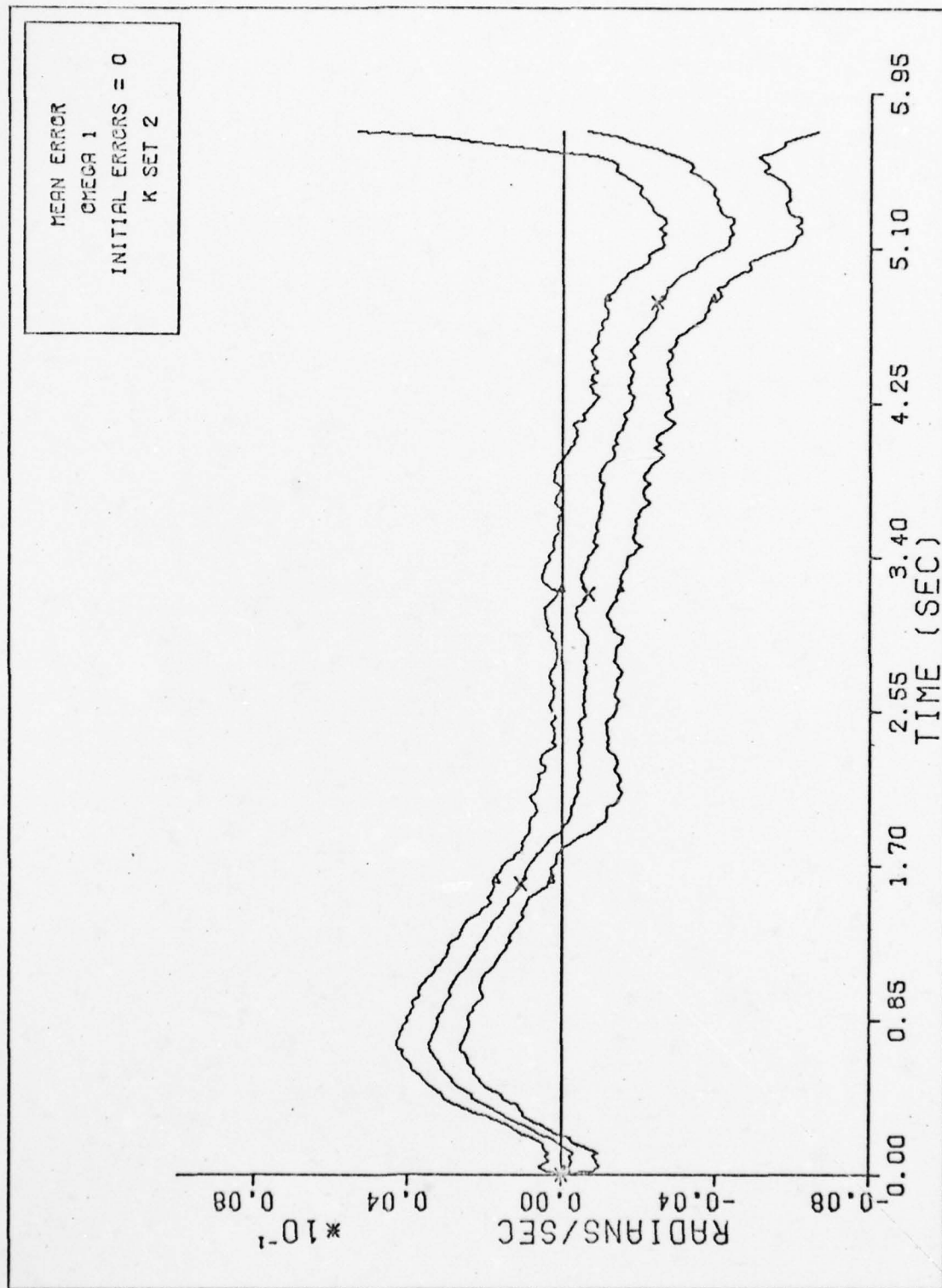


Fig. E-19

OMEGA 1 MEAN ERROR, 11 STATE FILTER

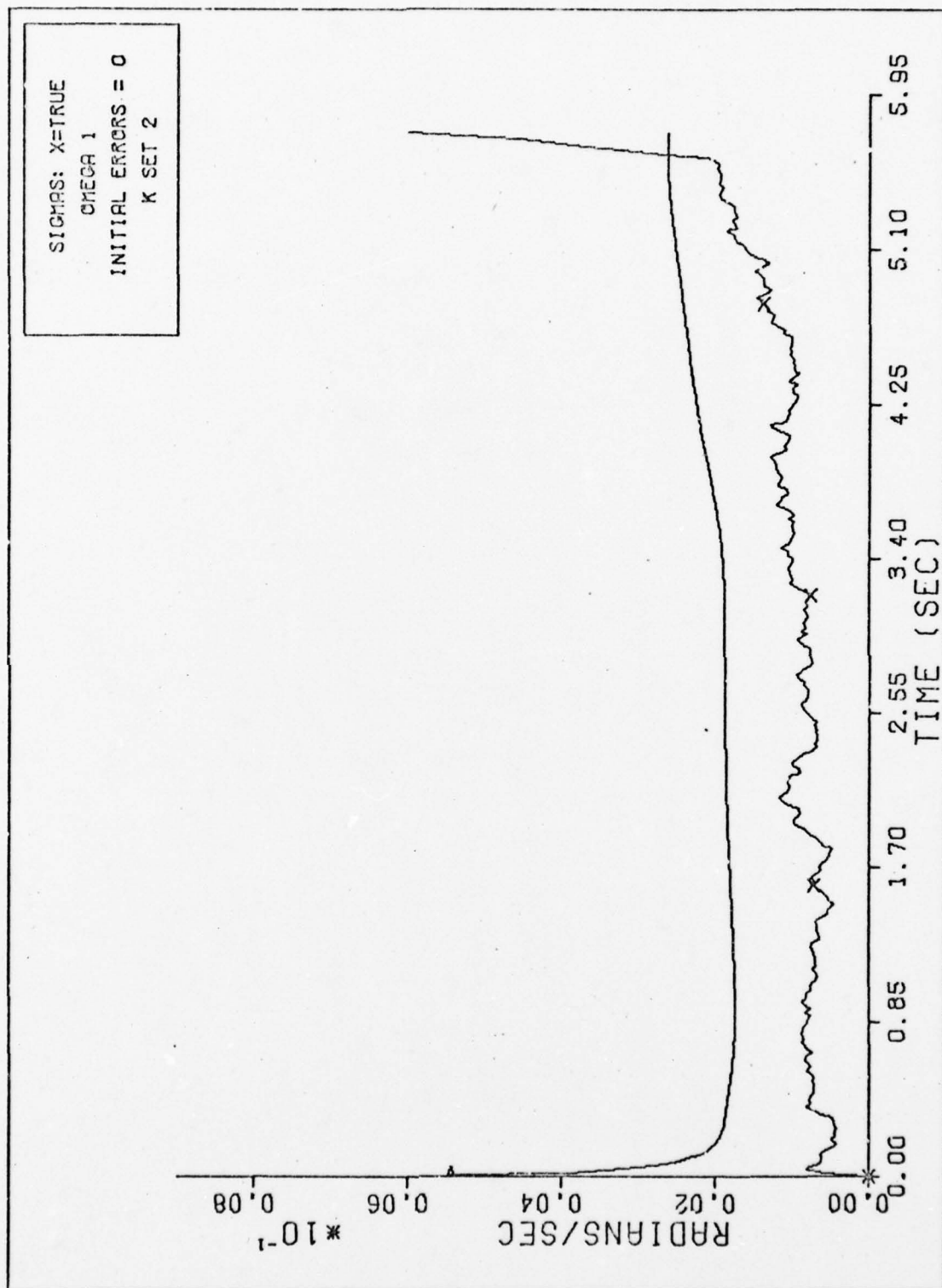


Fig. E-20 OMEGA 1 FILTER & TRUE SIGMAS, 11 STATE FILTER

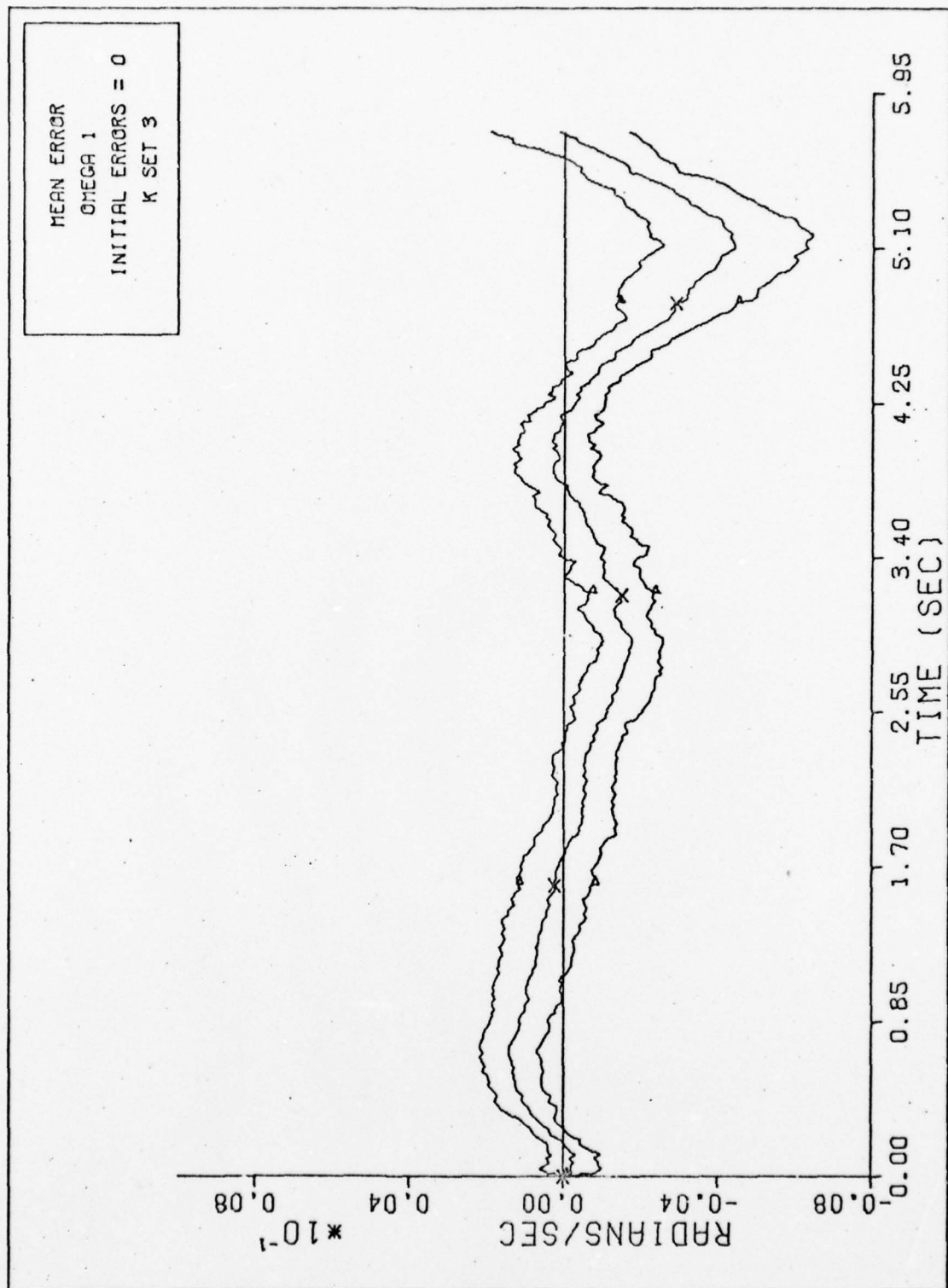


Fig. E-21

OMEGA 1 MEAN ERROR, 11 STATE FILTER

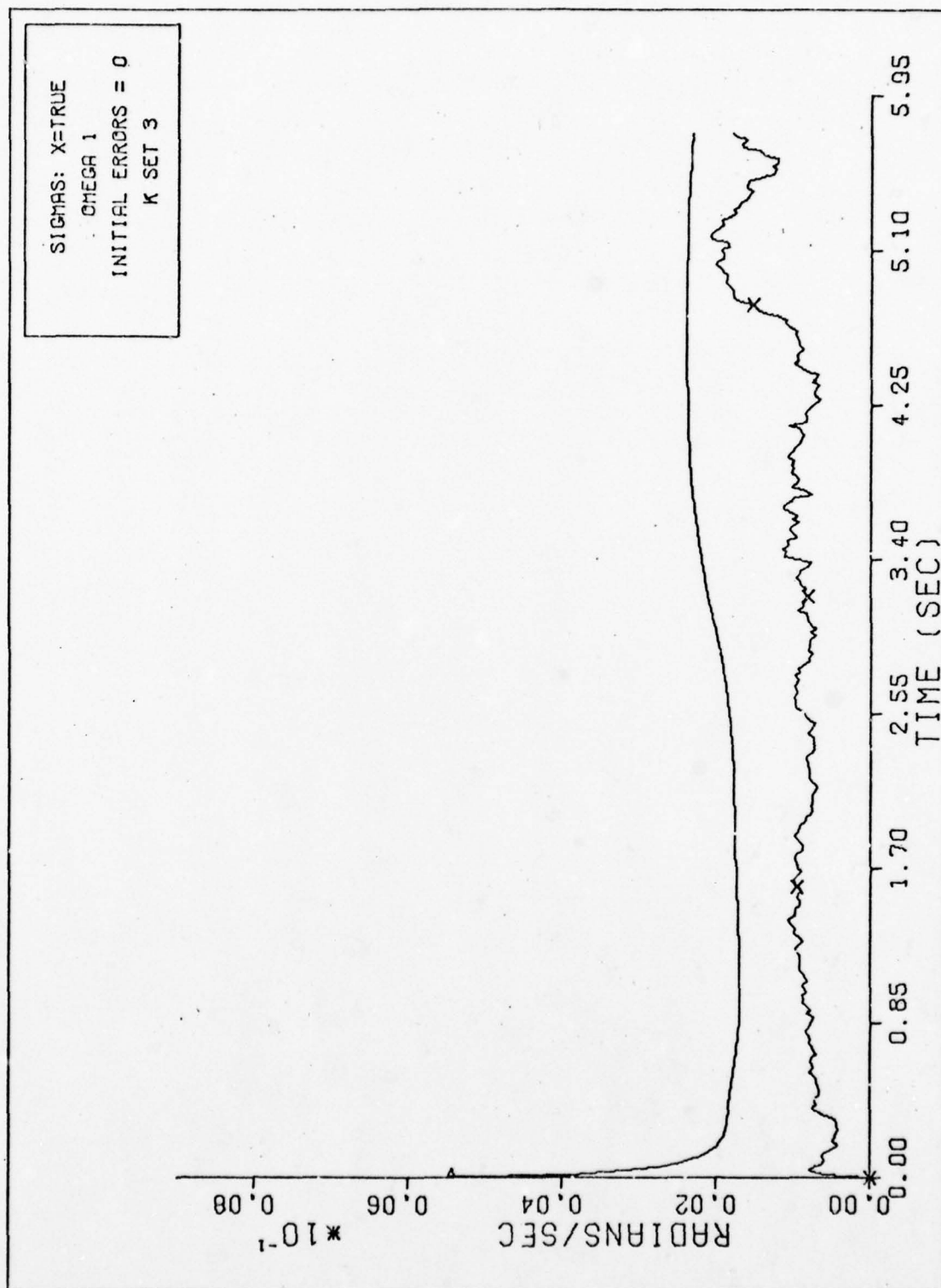


Fig. E-22 OMEGA 1 FILTER & TRUE SIGMAS, LI STATE FILTER

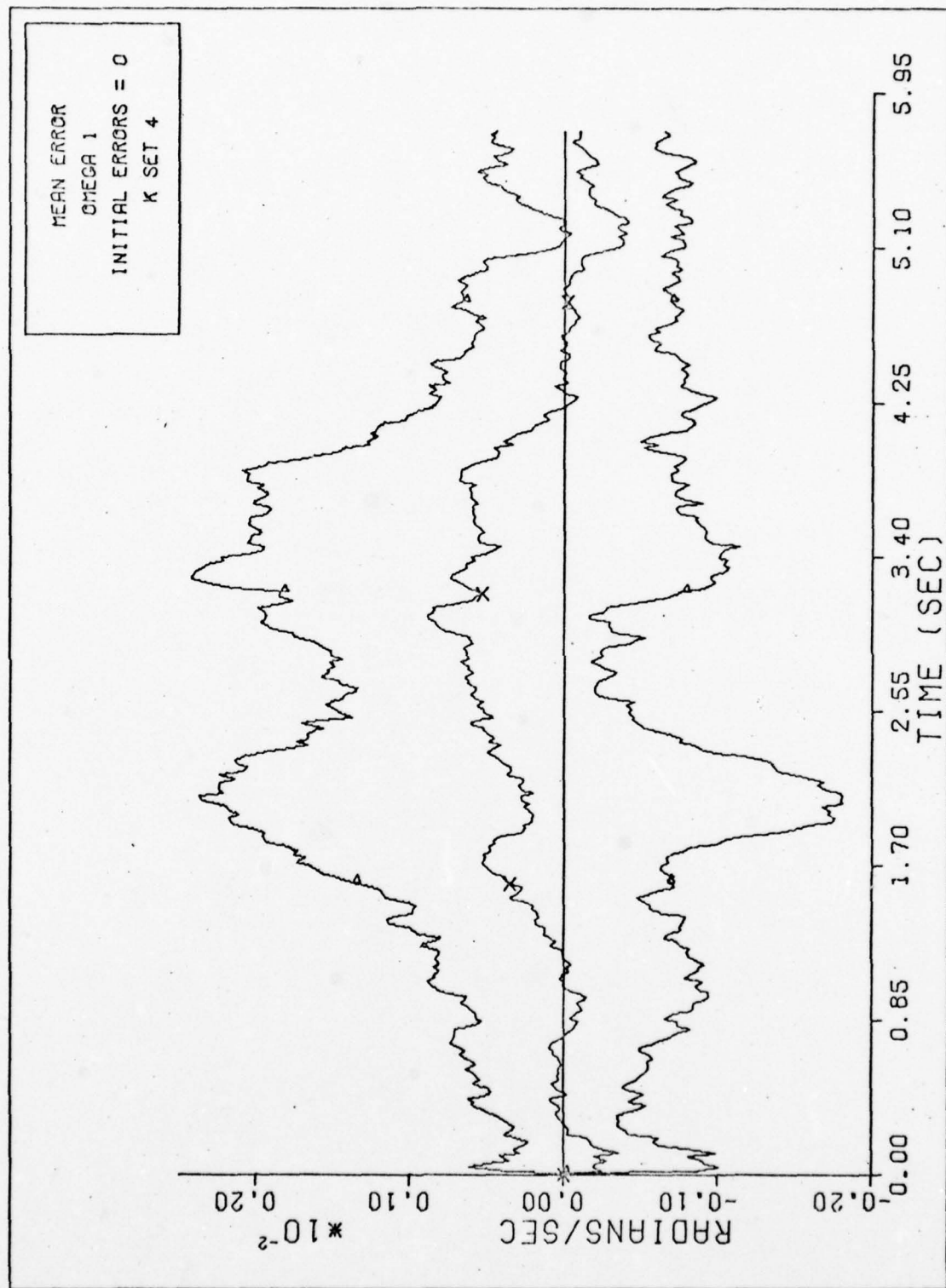


Fig. E-23

OMEGA 1 MEAN ERROR, 11 STATE FILTER

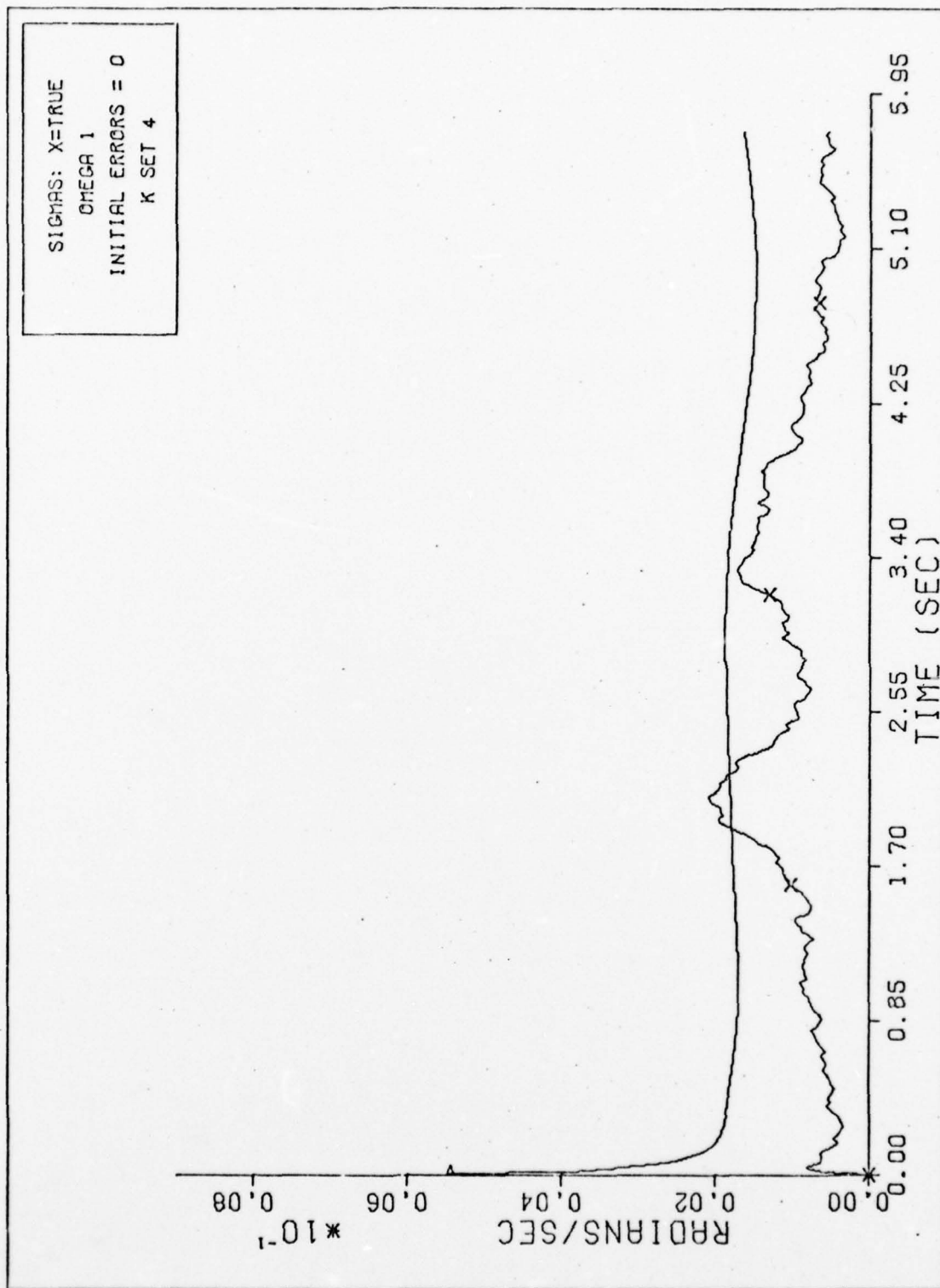


Fig. E-24 OMEGA 1 FILTER & TRUE SIGMAS, 11 STATE FILTER

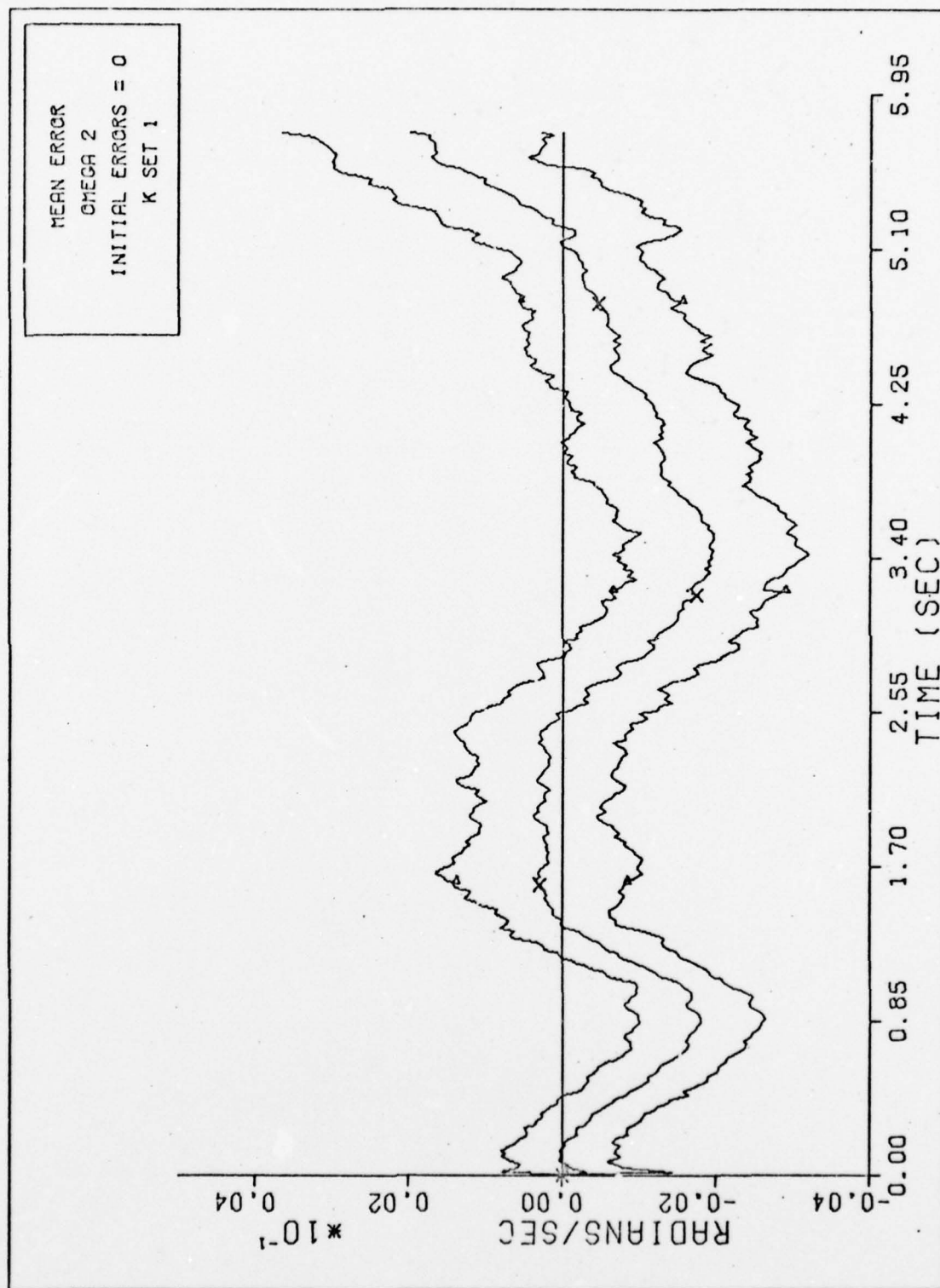


Fig. E-25

OMEGA 2 MEAN ERROR, 11 STATE FILTER

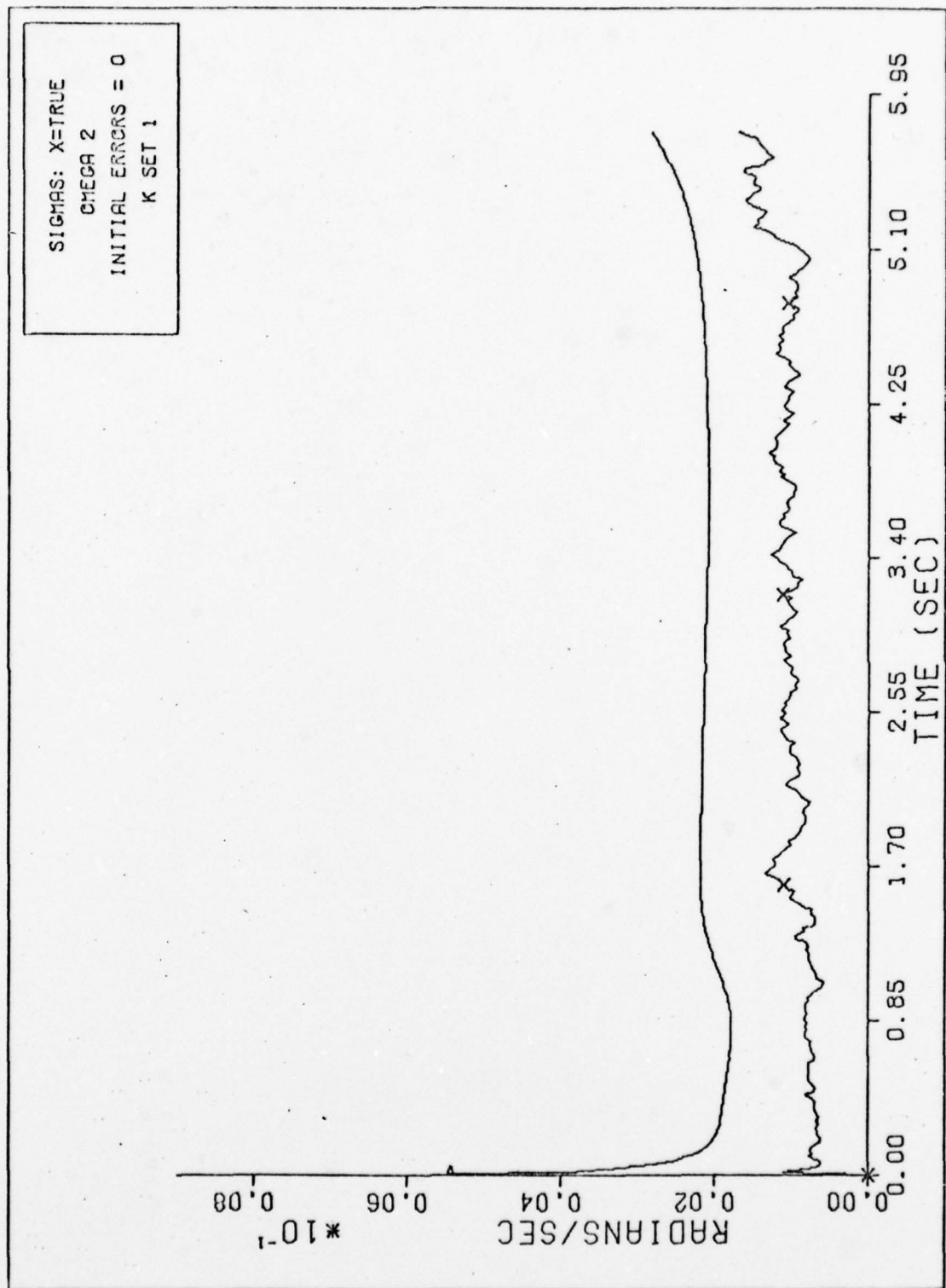


Fig. E-26 OMEGA 2 FILTER & TRUE SIGMAS, 11 STATE FILTER

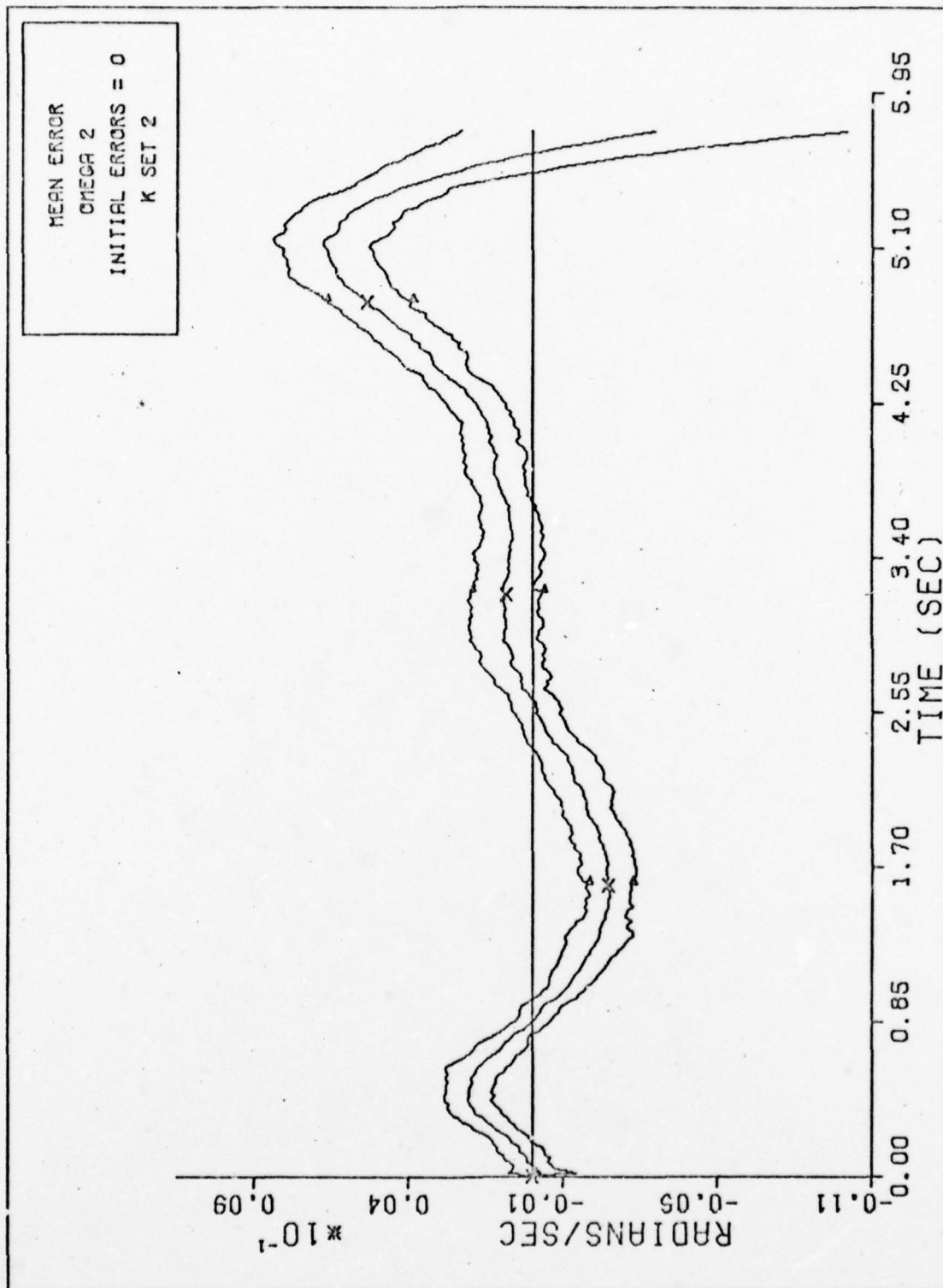


Fig. E-27

OMEGA 2 MEAN ERROR, 11 STATE FILTER

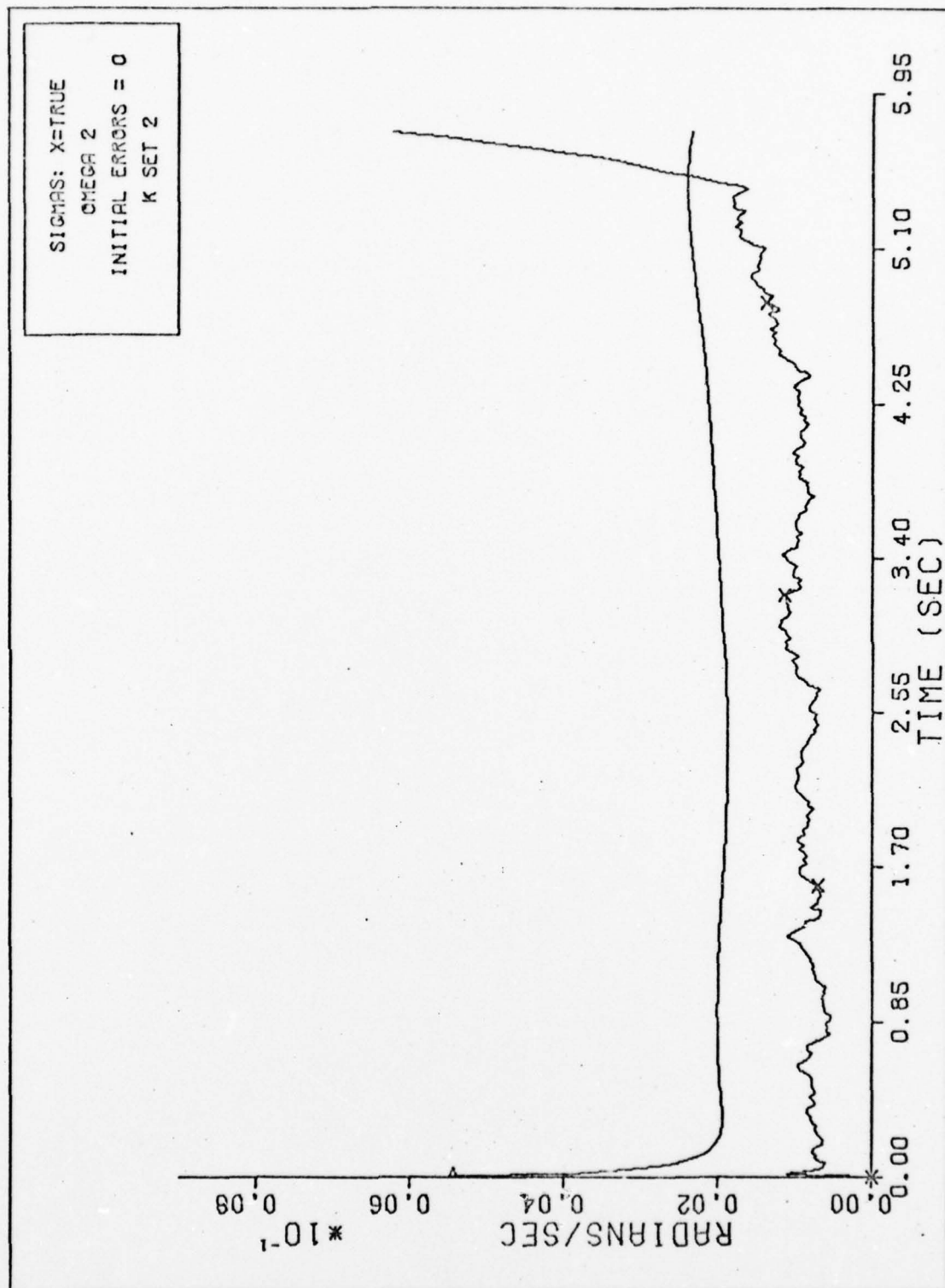


Fig. E-28

OMEGA 2 FILTER & TRUE SIGMAS, 11 STATE FILTER

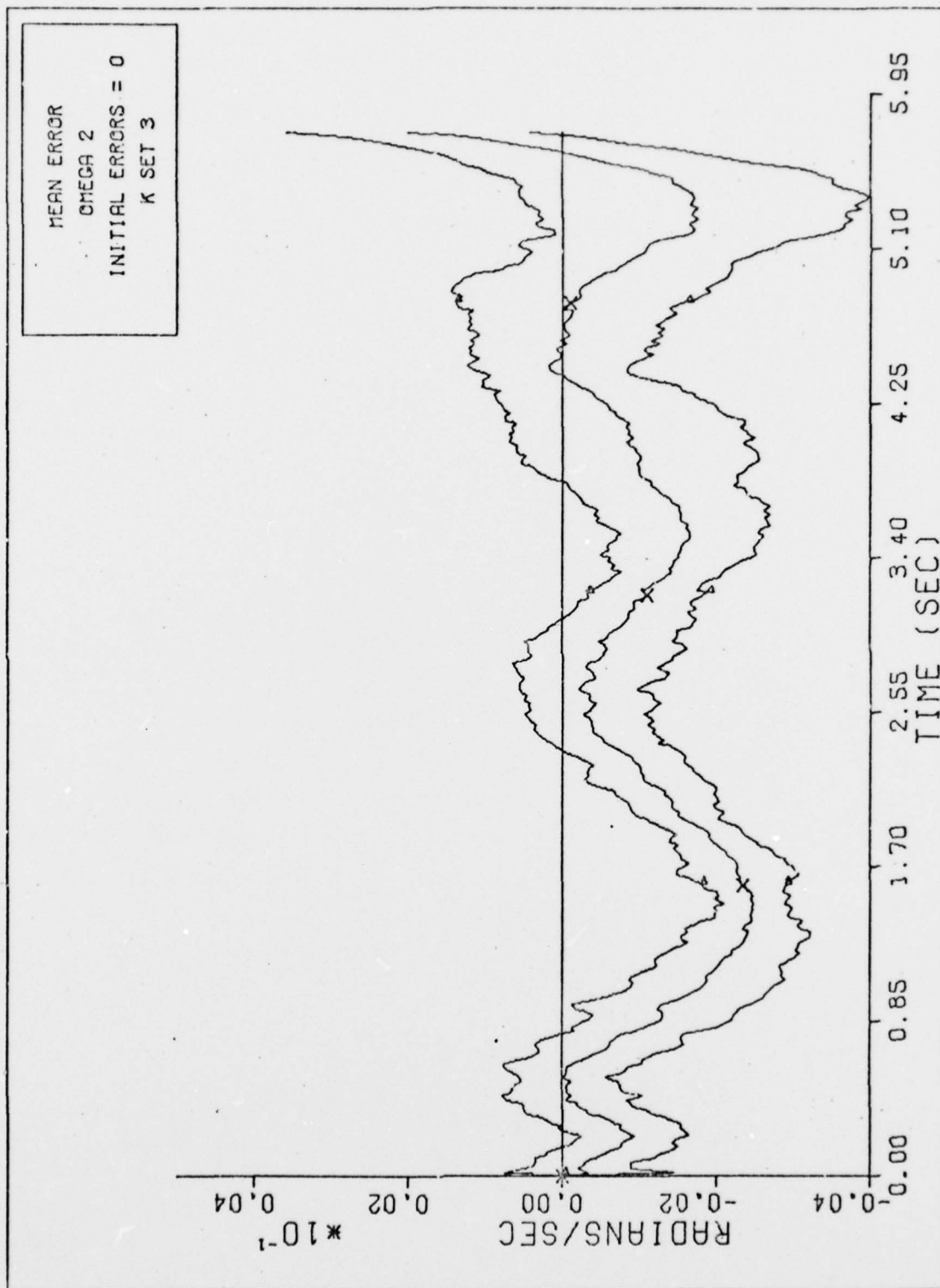


Fig. E-29

OMEGA 2 MEAN ERROR, L1 STATE FILTER

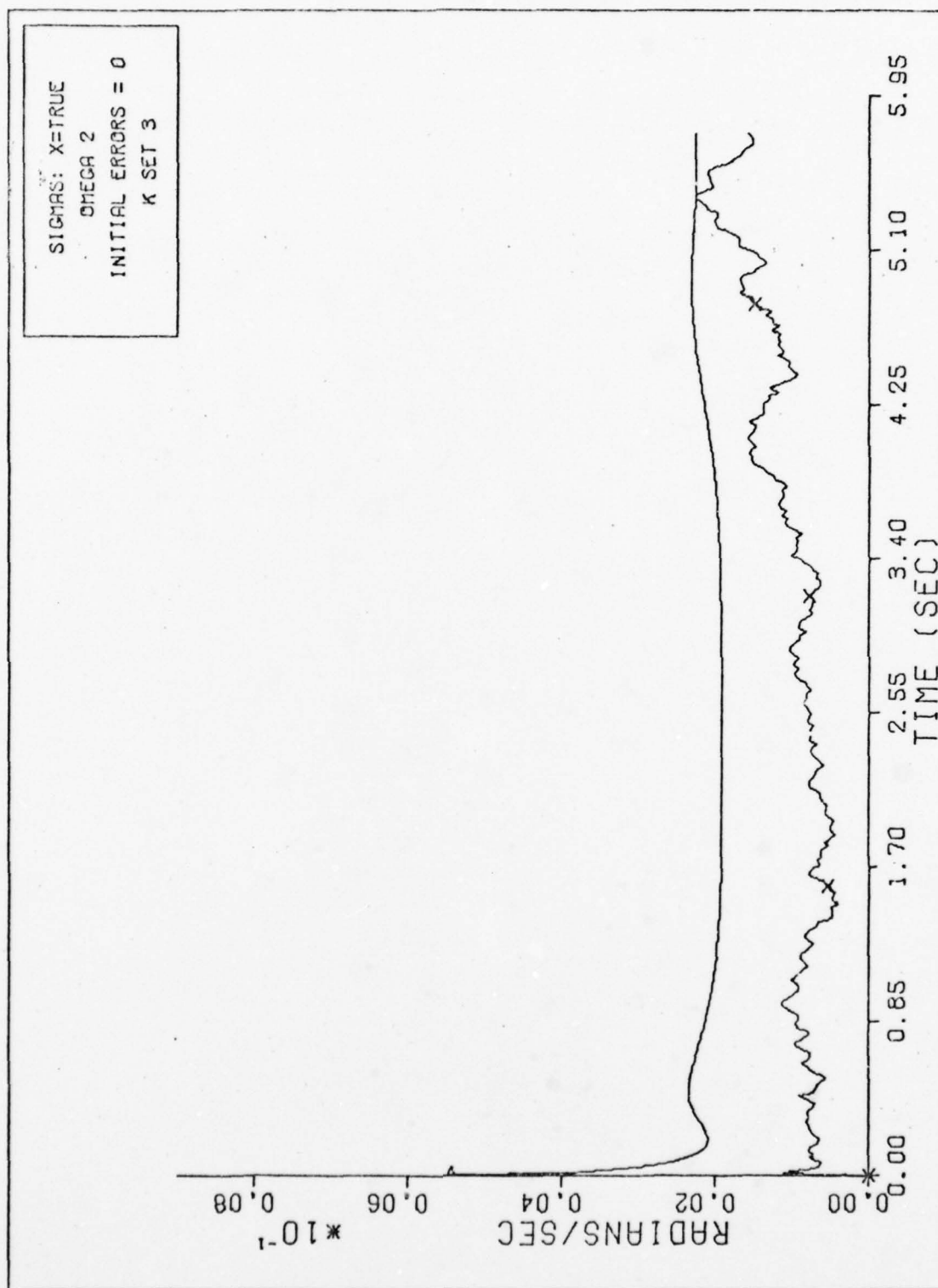


Fig. E-30 OMEGA 2 FILTER & TRUE SIGMAS, L1 STATE FILTER

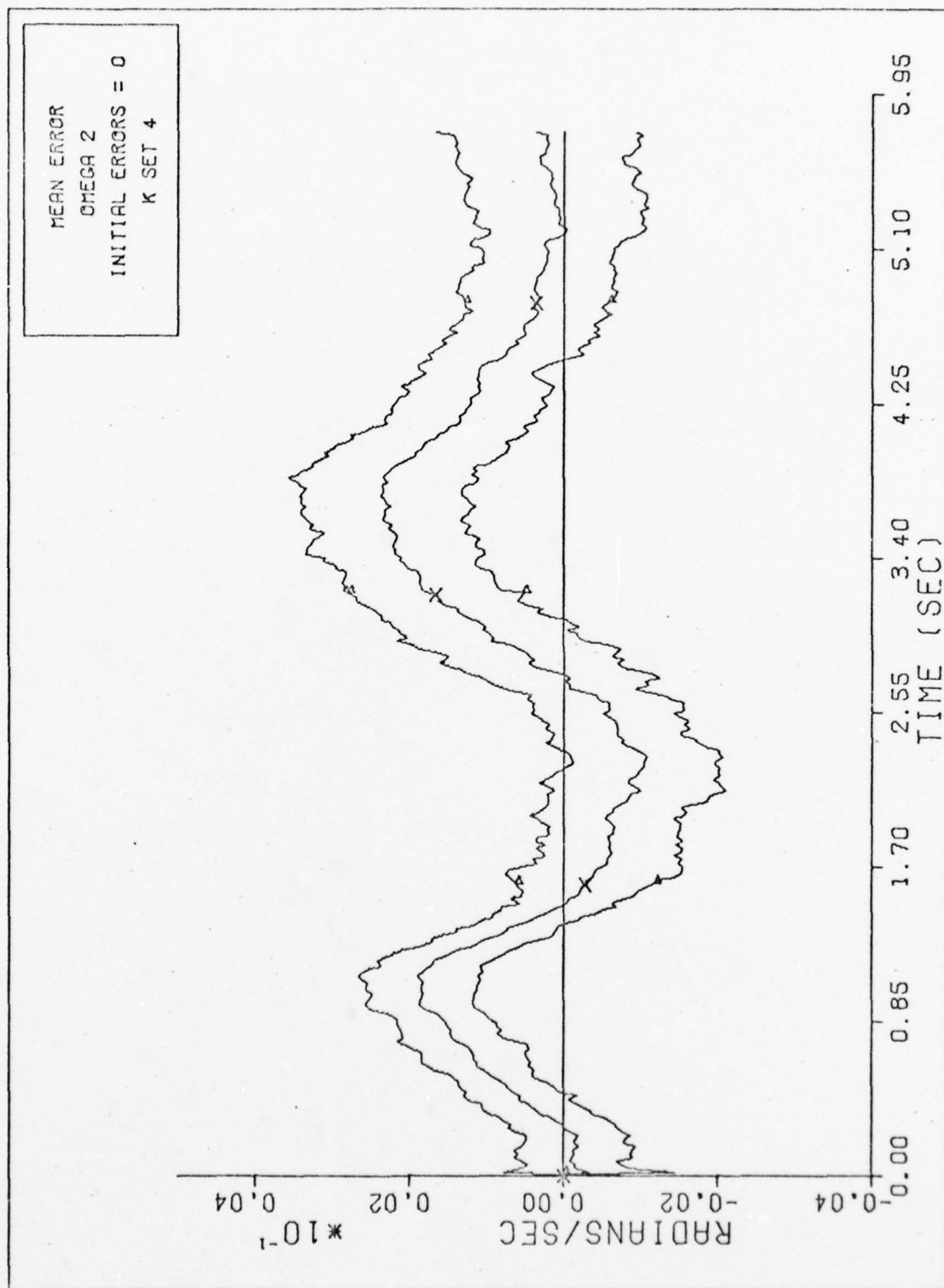


Fig. E-31

OMEGA 2 MEAN ERROR, L1 STATE FILTER

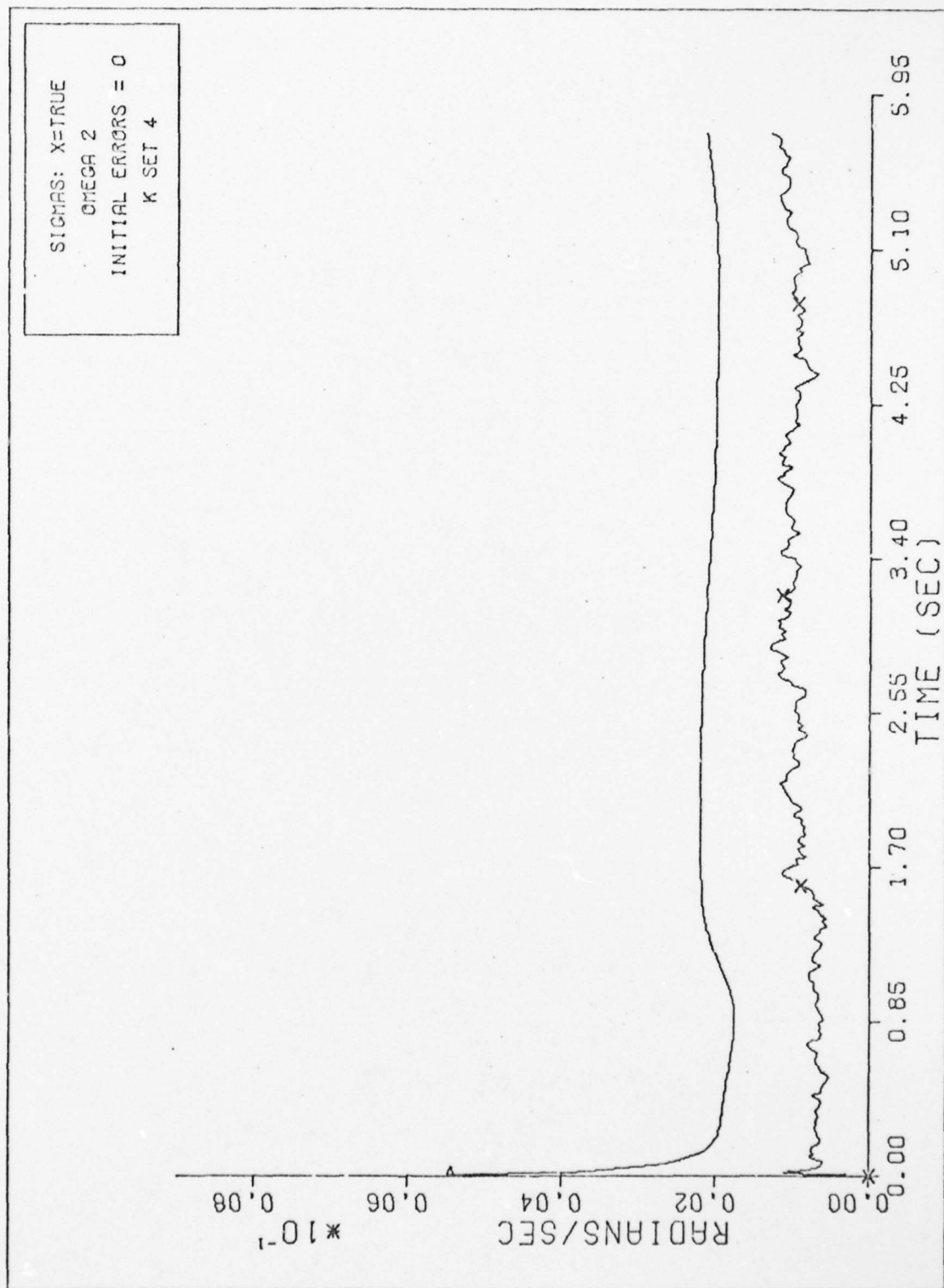


Fig. E-32 OMEGA 2 FILTER & TRUE SIGMAS, 11 STATE FILTER

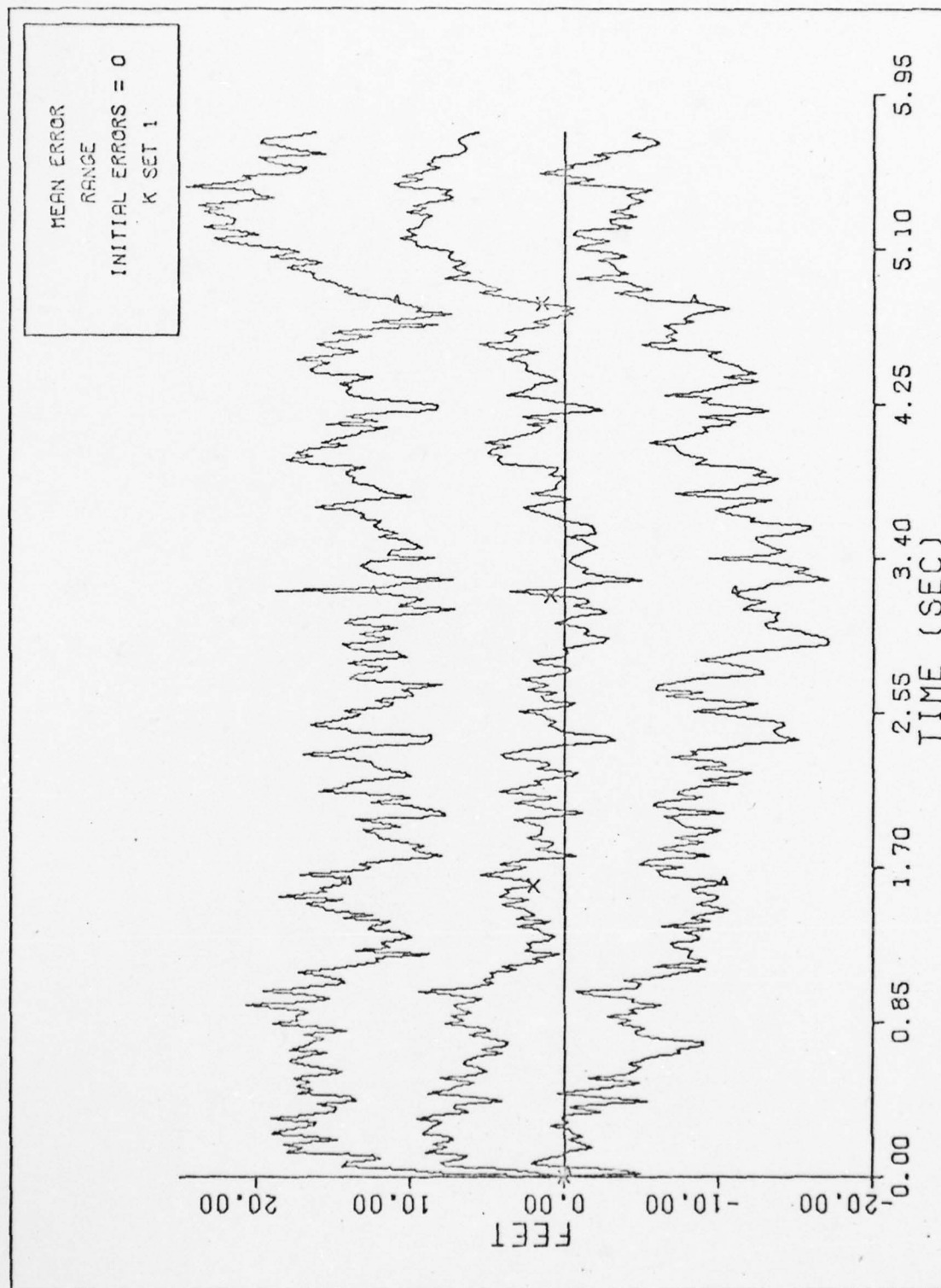


Fig. E-33

RANGE MEAN ERROR, L1 STATE FILTER

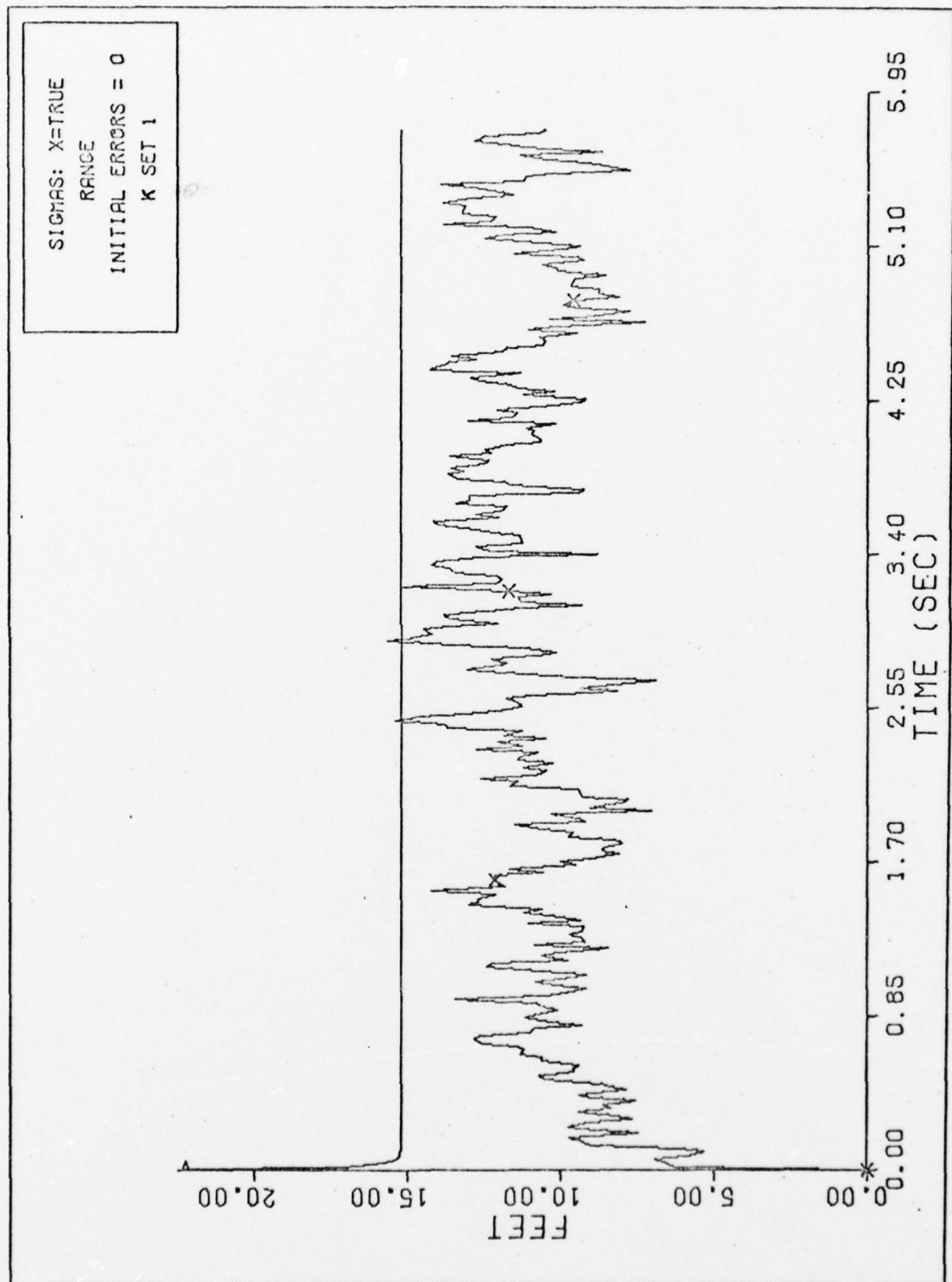


Fig. E-34

RANGE FILTER & TRUE SIGMAS, 11 STATE FILTER

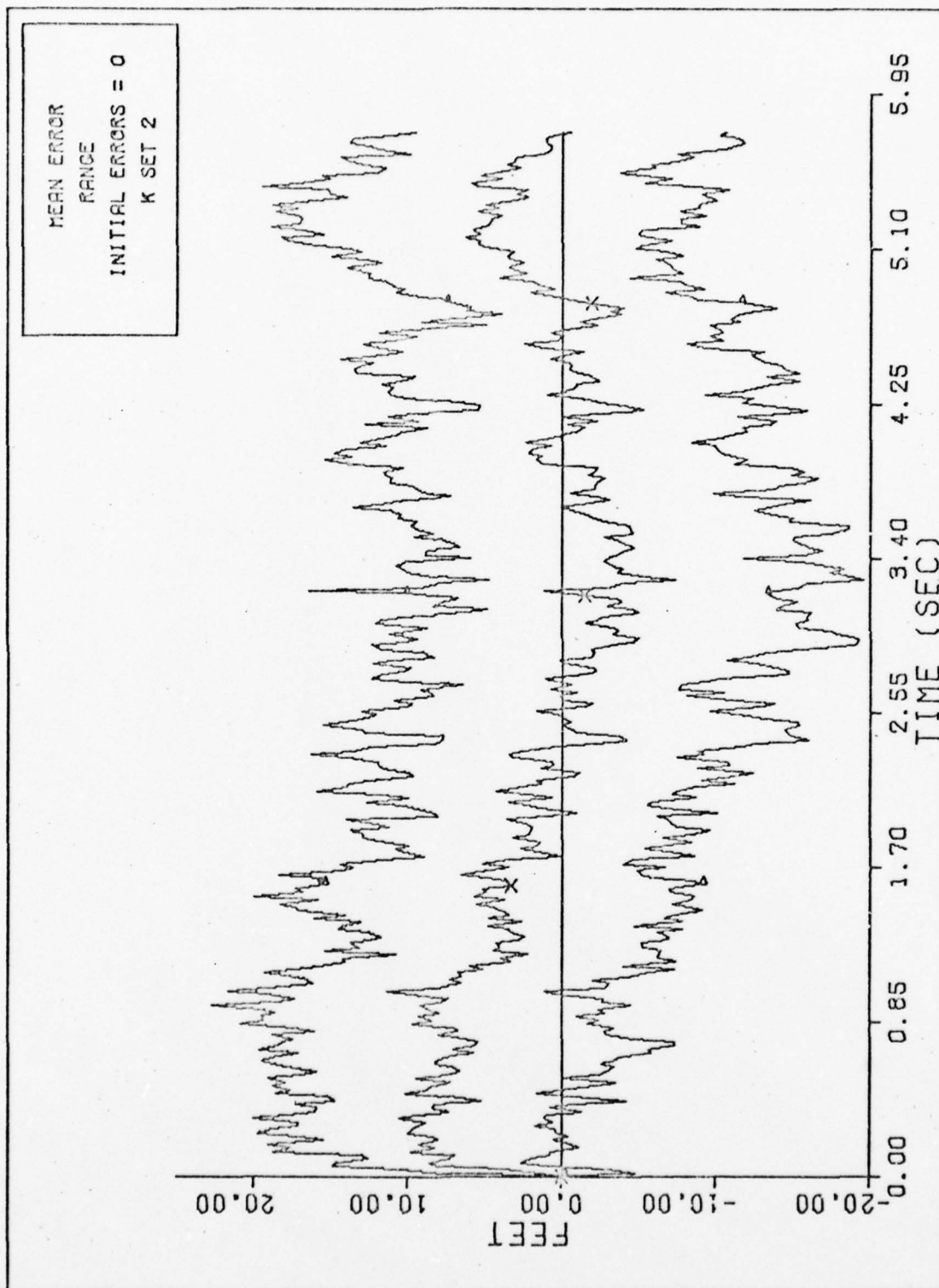


Fig. E-35

RANGE MEAN ERROR, L1 STATE FILTER

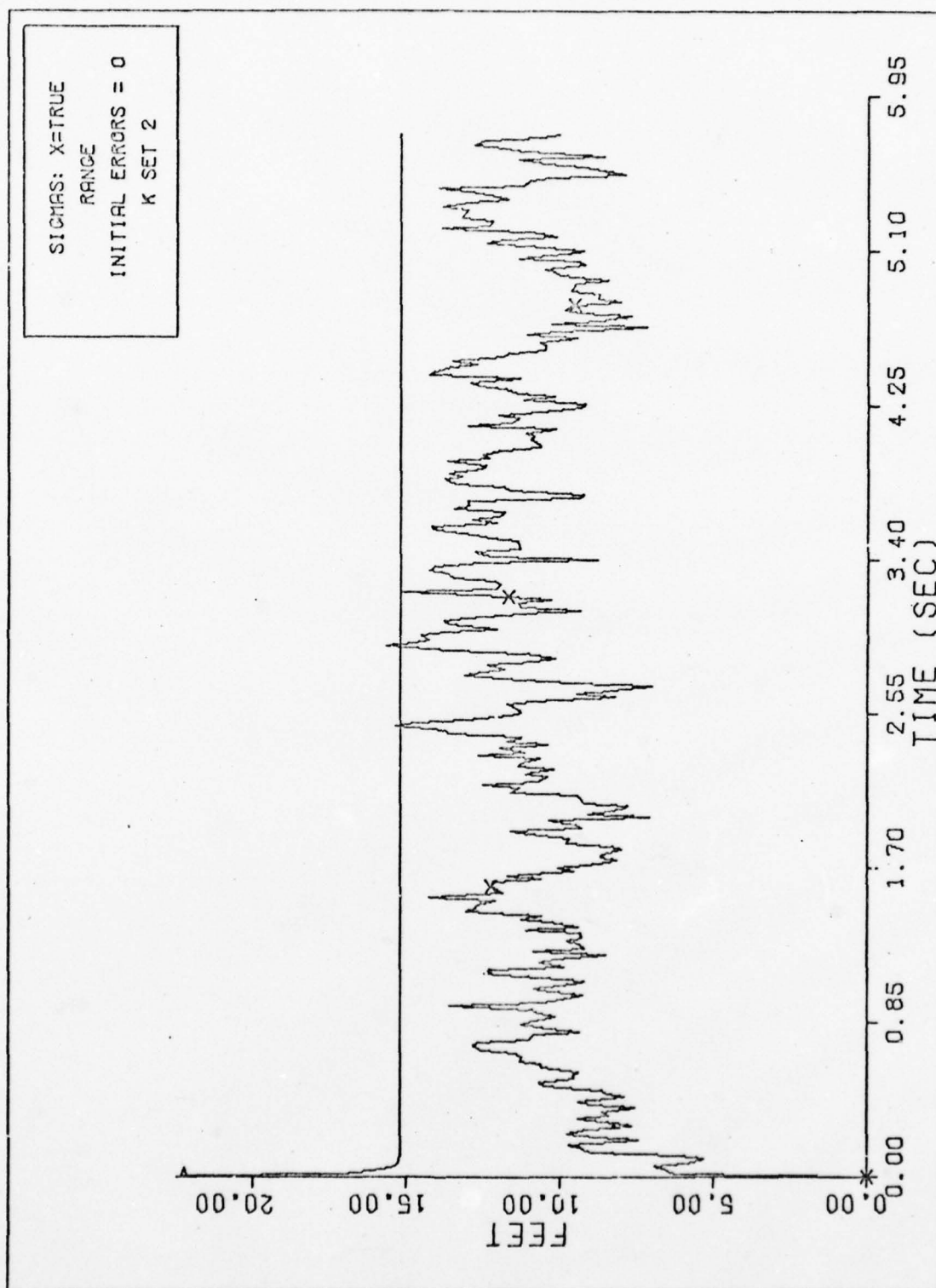


Fig. E-36

RANGE FILTER & TRUE SIGMAS, 11 STATE FILTER

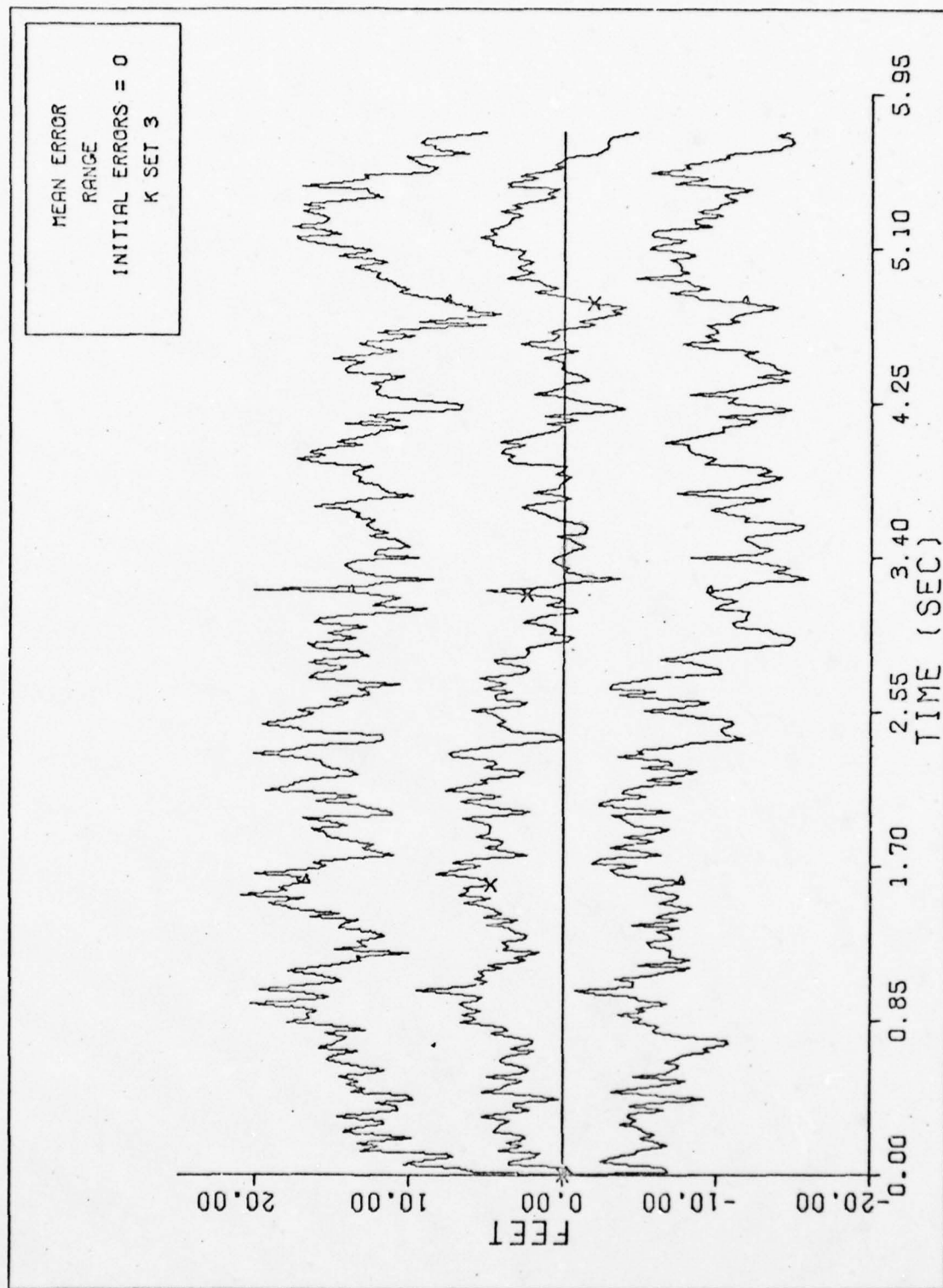


Fig. E-37

RANGE MEAN ERROR, 11 STATE FILTER

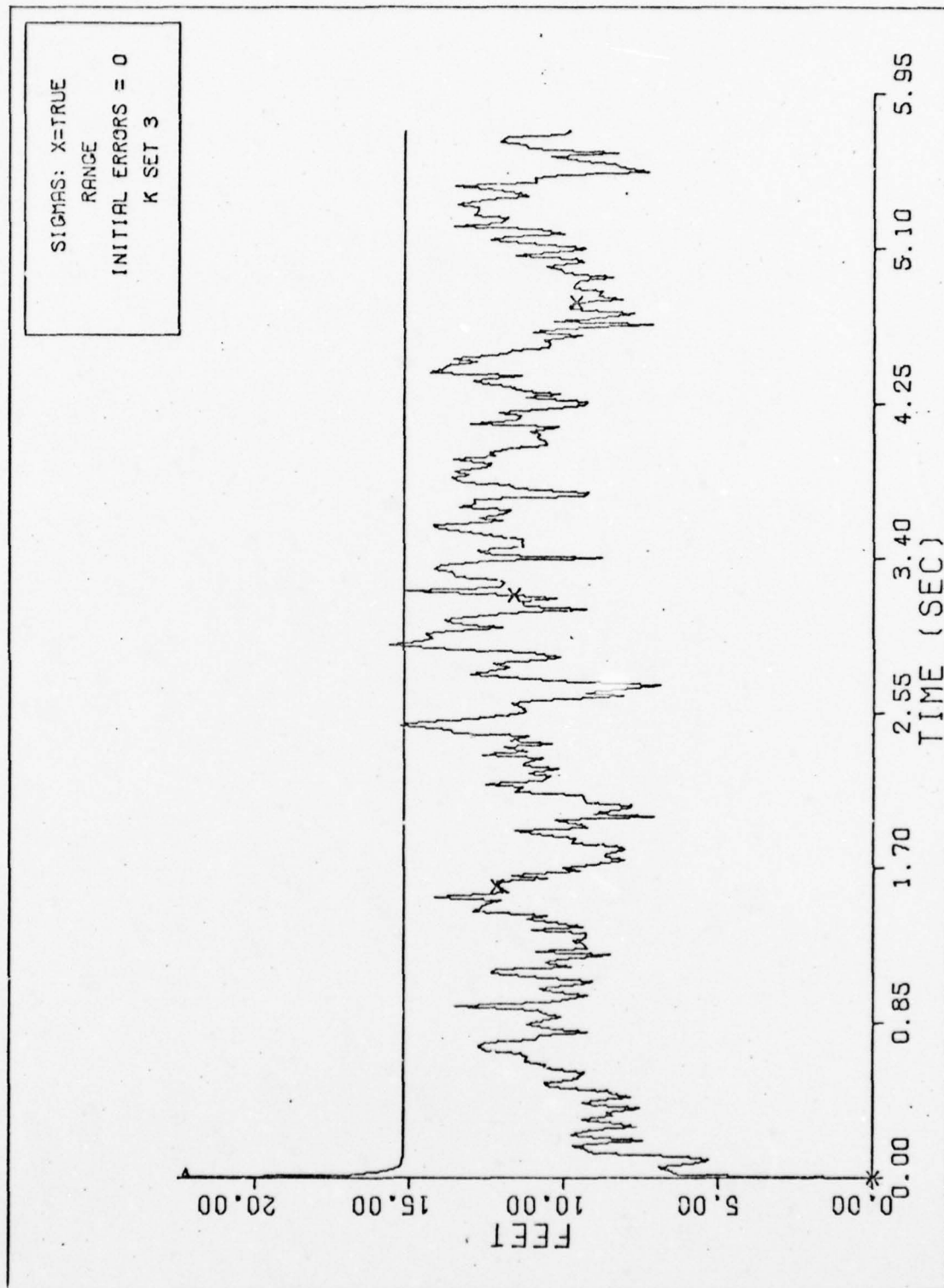


Fig. E-38

RANGE FILTER & TRUE SIGMAS, 11 STATE FILTER

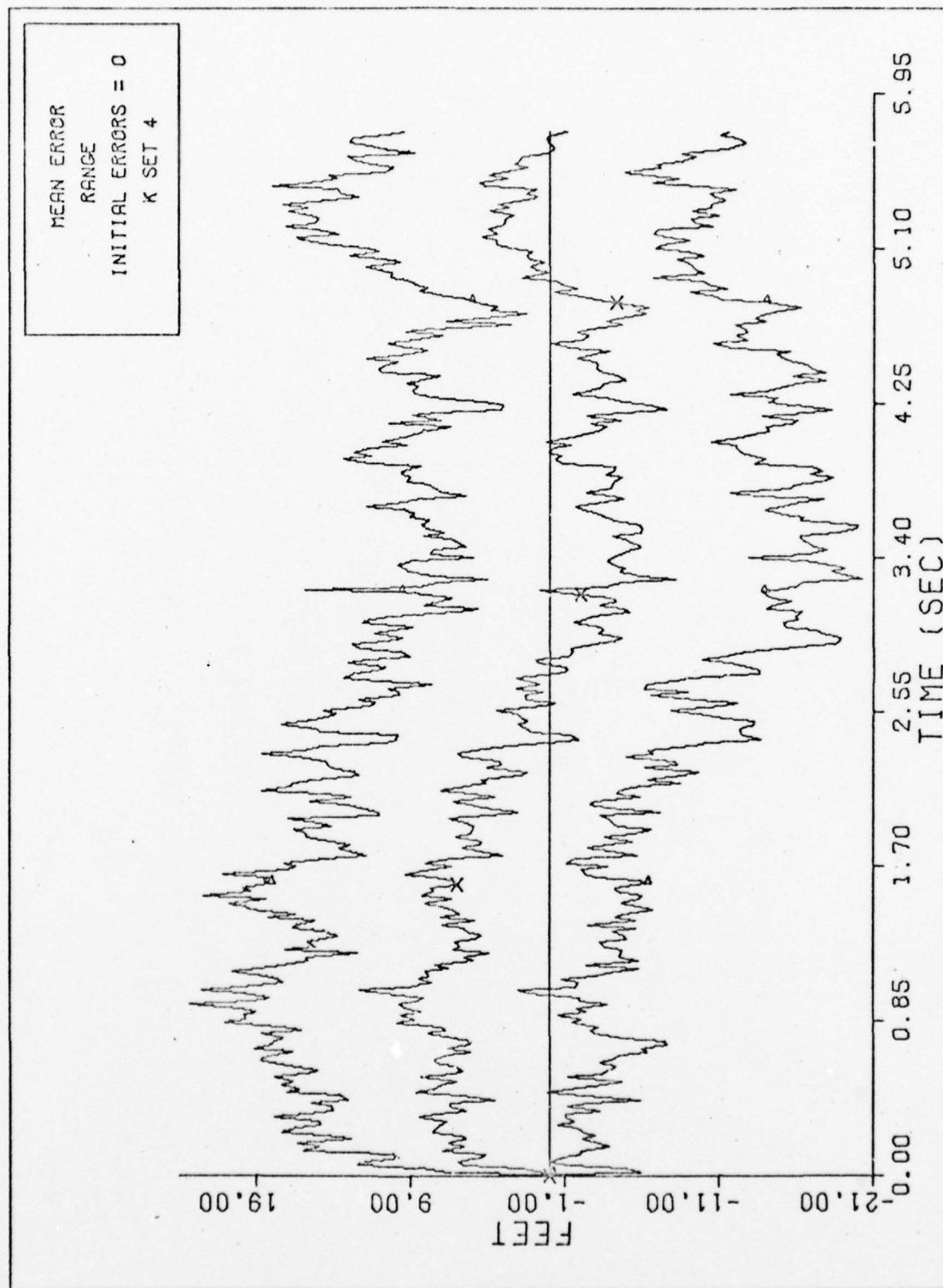


Fig. E-39

RANGE MEAN ERROR, L1 STATE FILTER

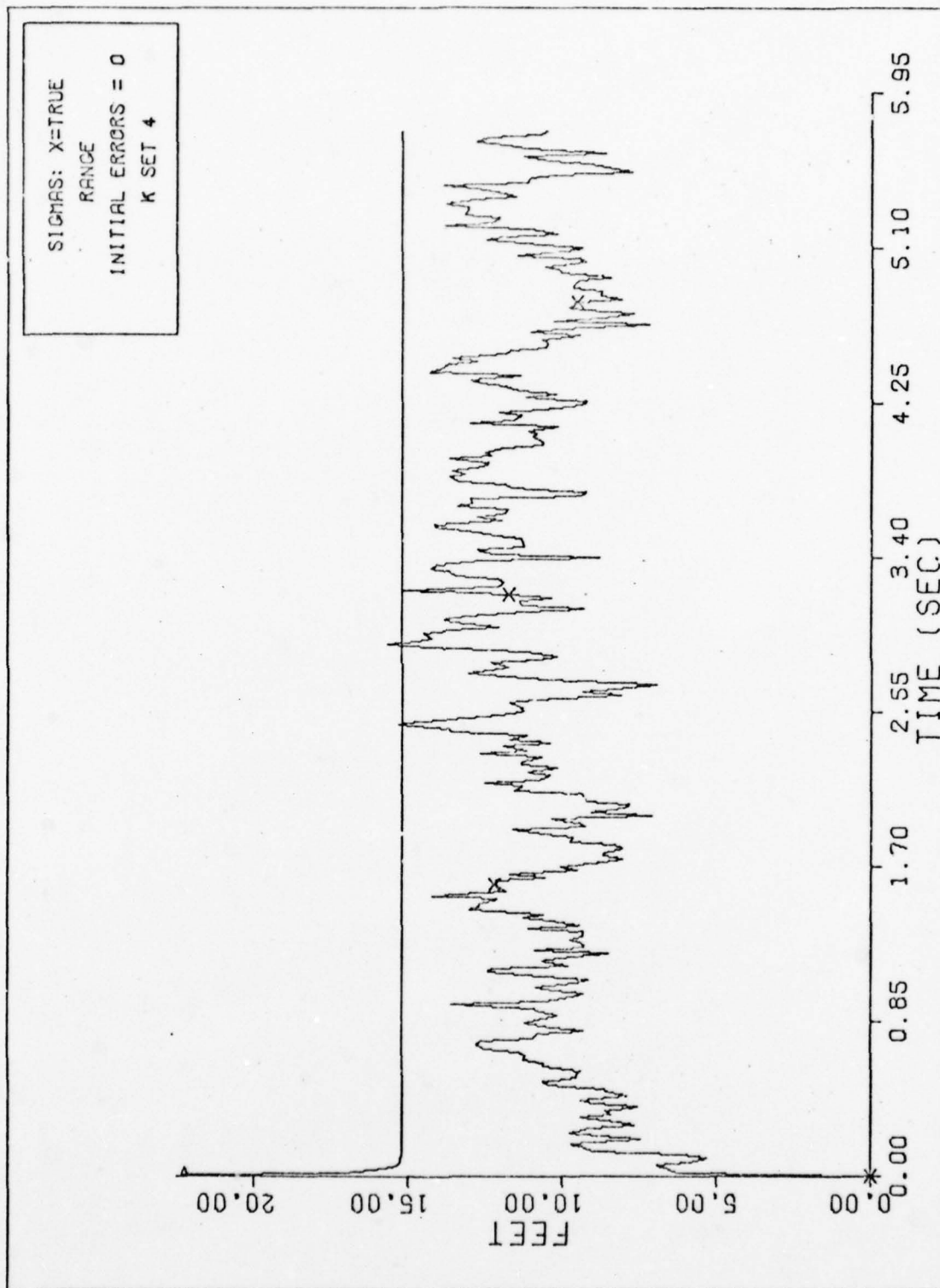


Fig. E-40

RANGE FILTER & TRUE SIGMAS, 11 STATE FILTER

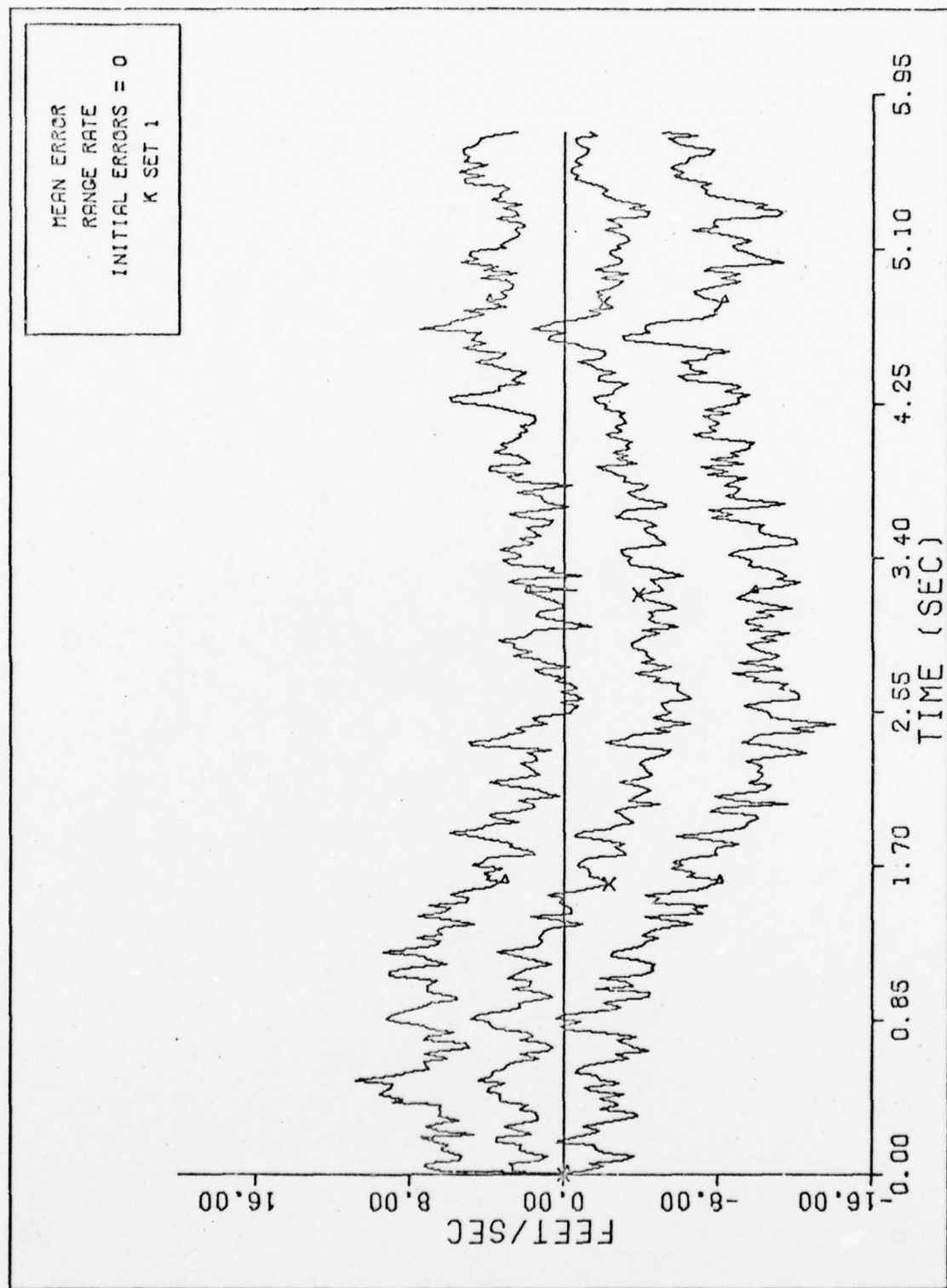


Fig. E-41

RANGE RATE MEAN ERROR, 11 STATE FILTER

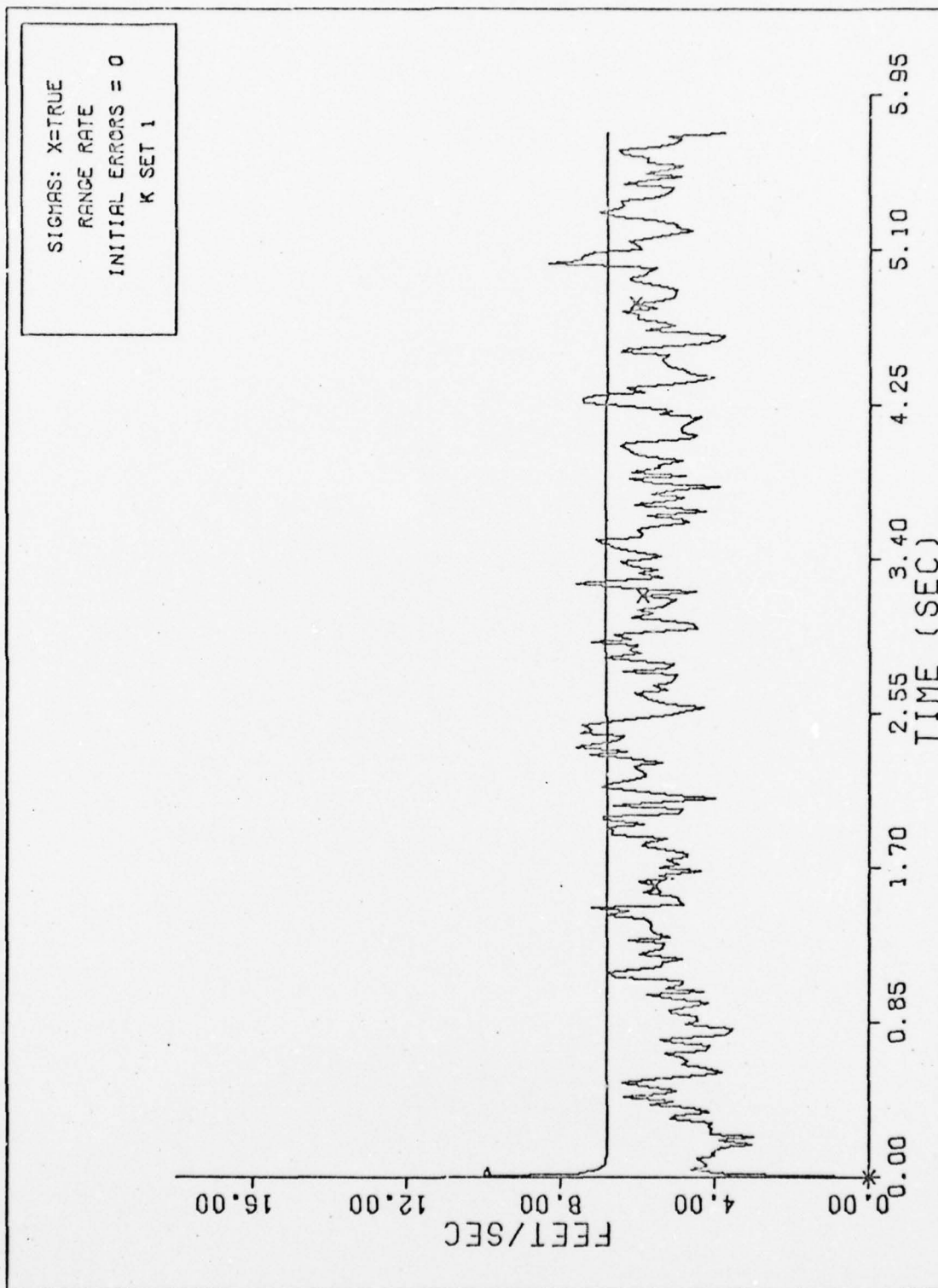


Fig. E-42 RANGE RATE FILTER & TRUE SIGMAS, 11 STATE FILTER

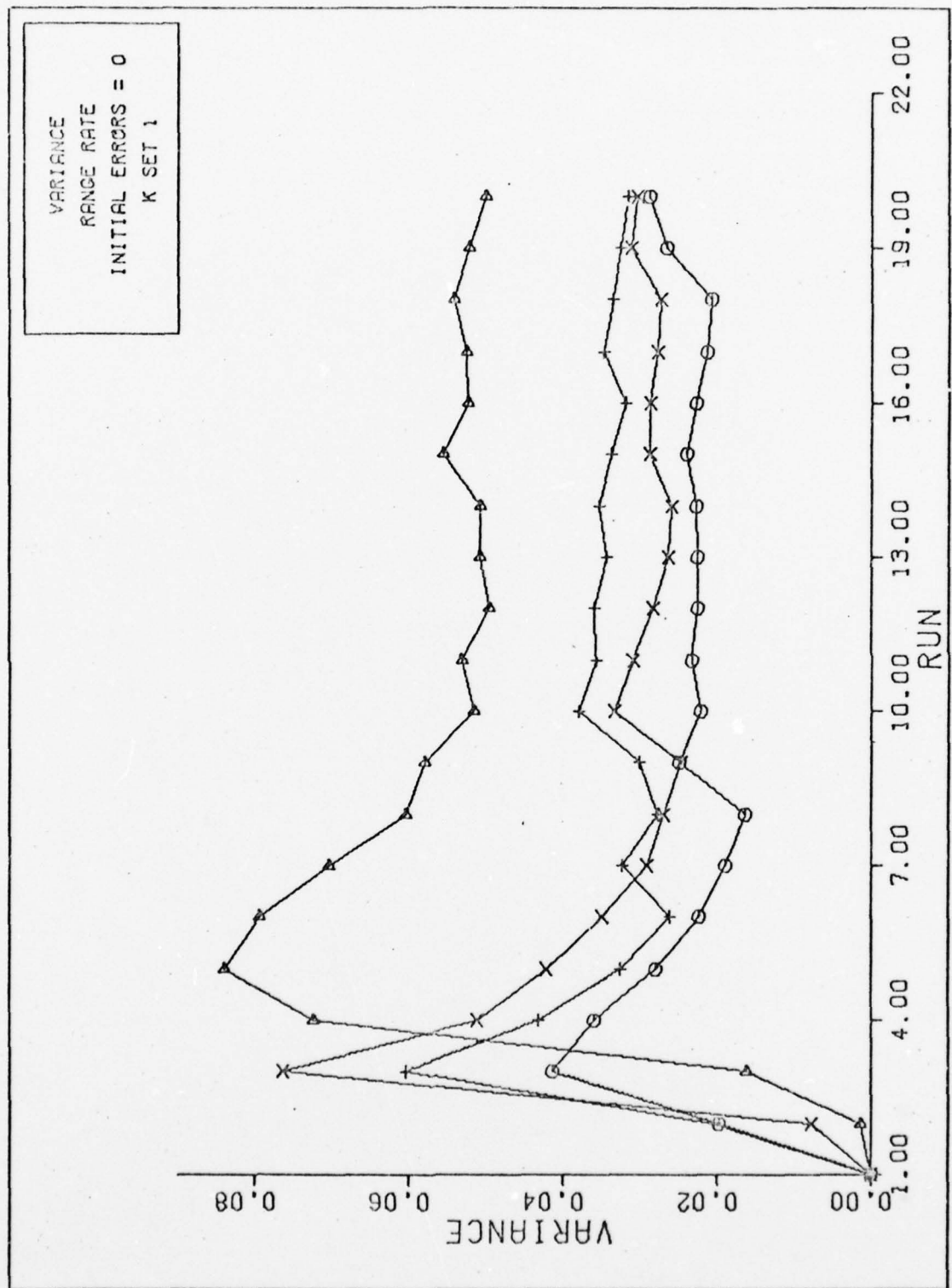


Fig. E-43

VARIANCE CONVERGENCE

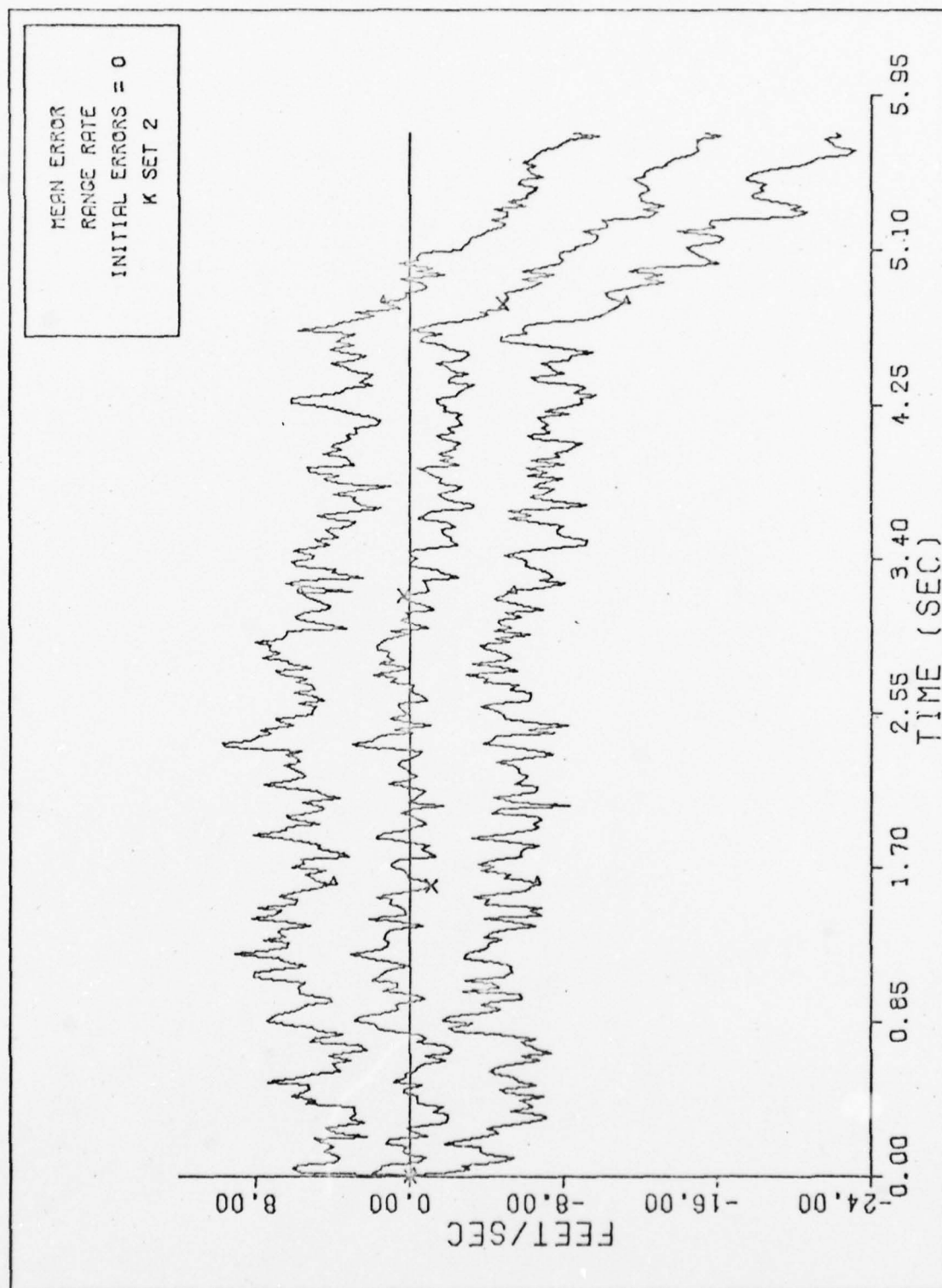


Fig. E-44

RANGE RATE MEAN ERROR, 11 STATE FILTER

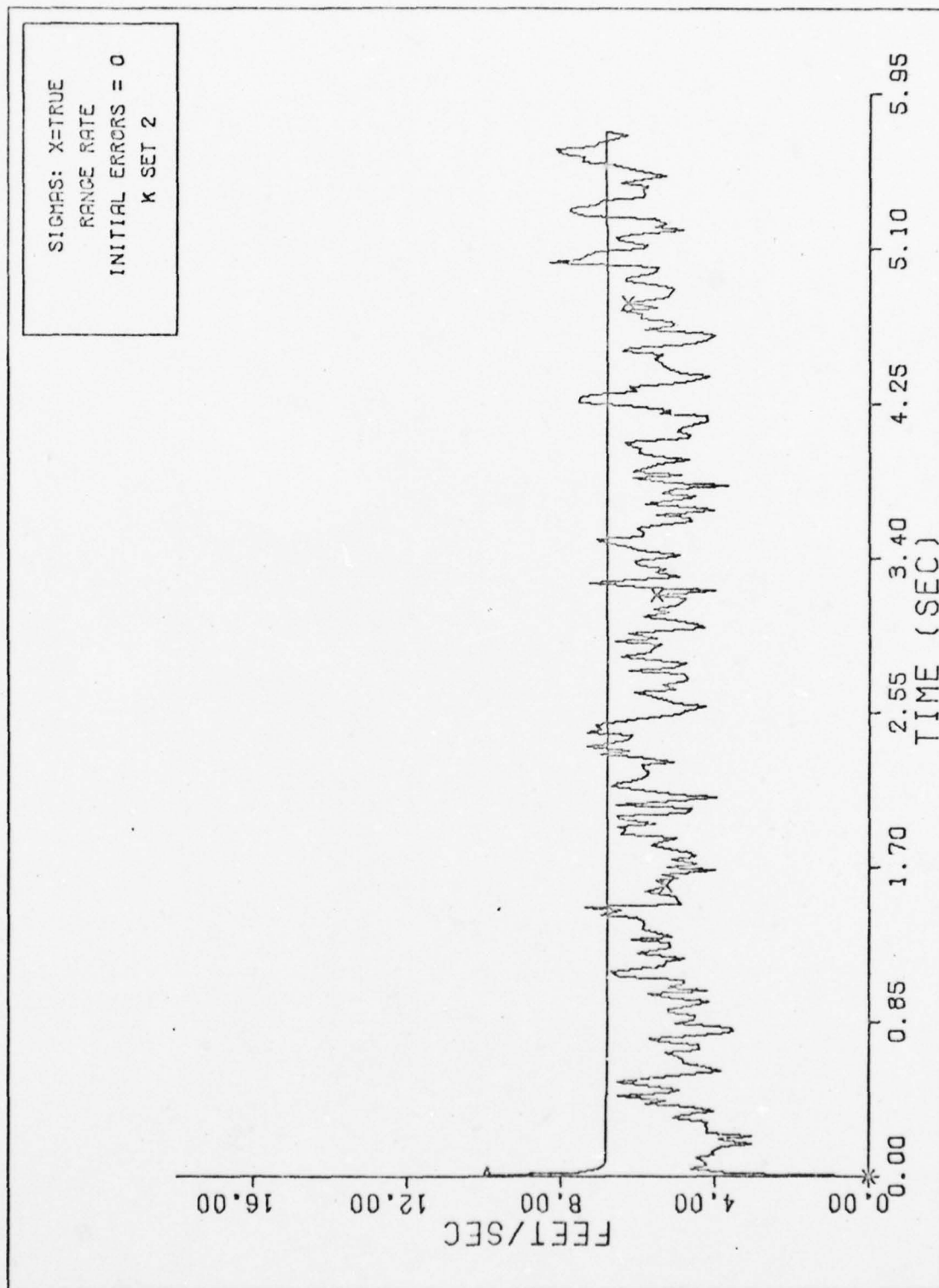


Fig. E-45 RANGE RATE FILTER & TRUE SIGMAS, 11 STATE FILTER

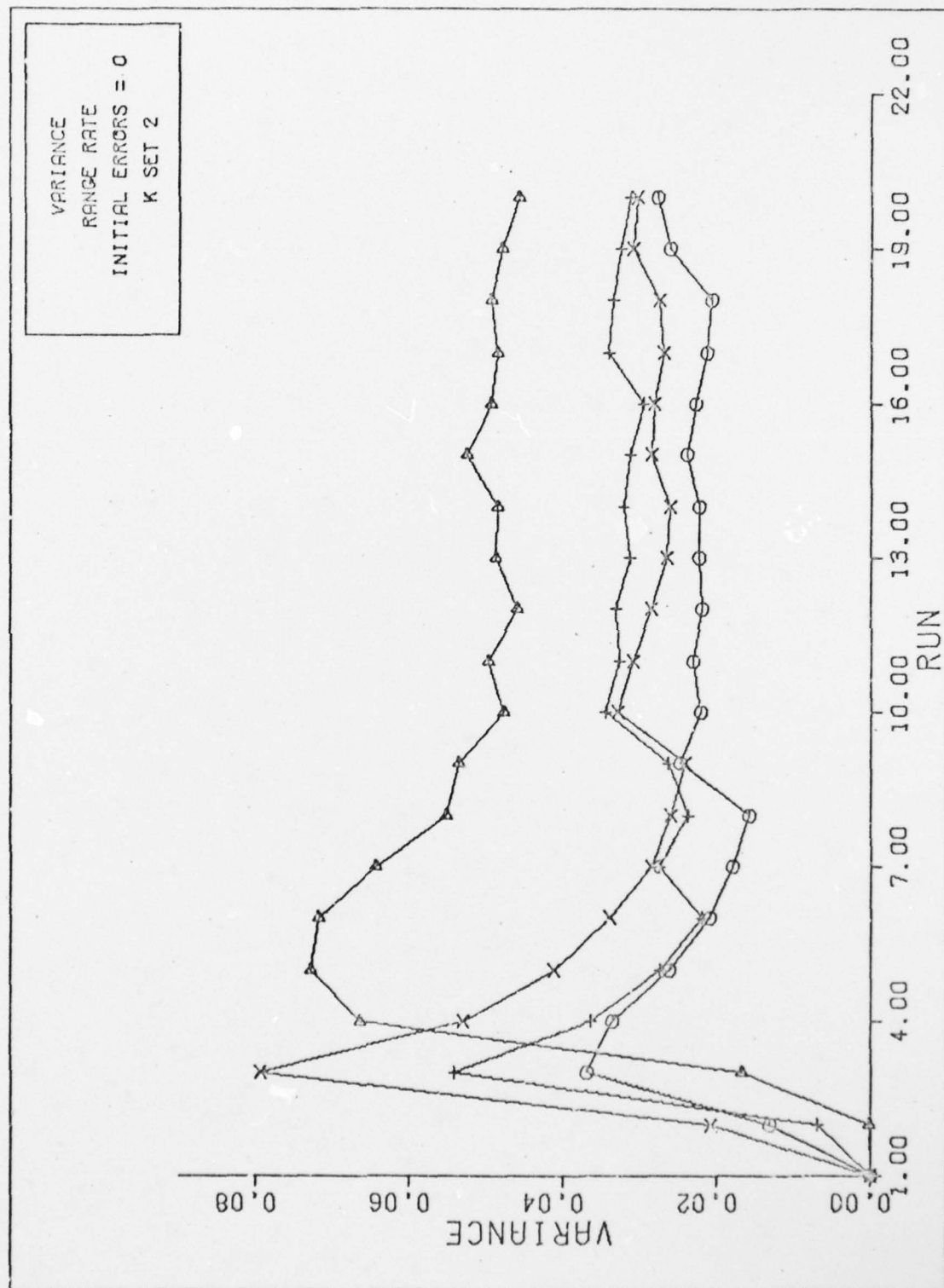


Fig. E-46

VARIANCE CONVERGENCE

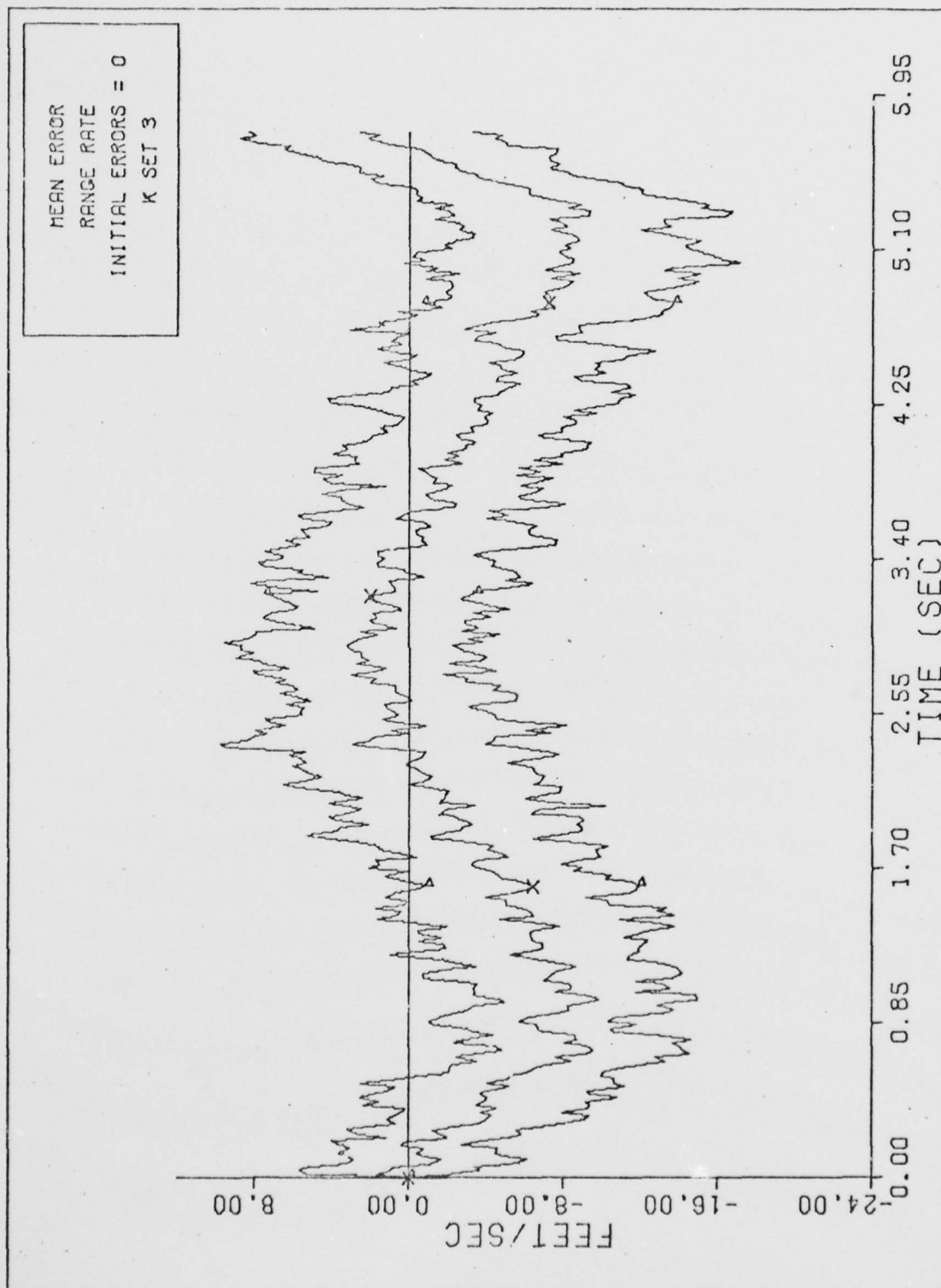


Fig. E-47

RANGE RATE MEAN ERROR, 11 STATE FILTER

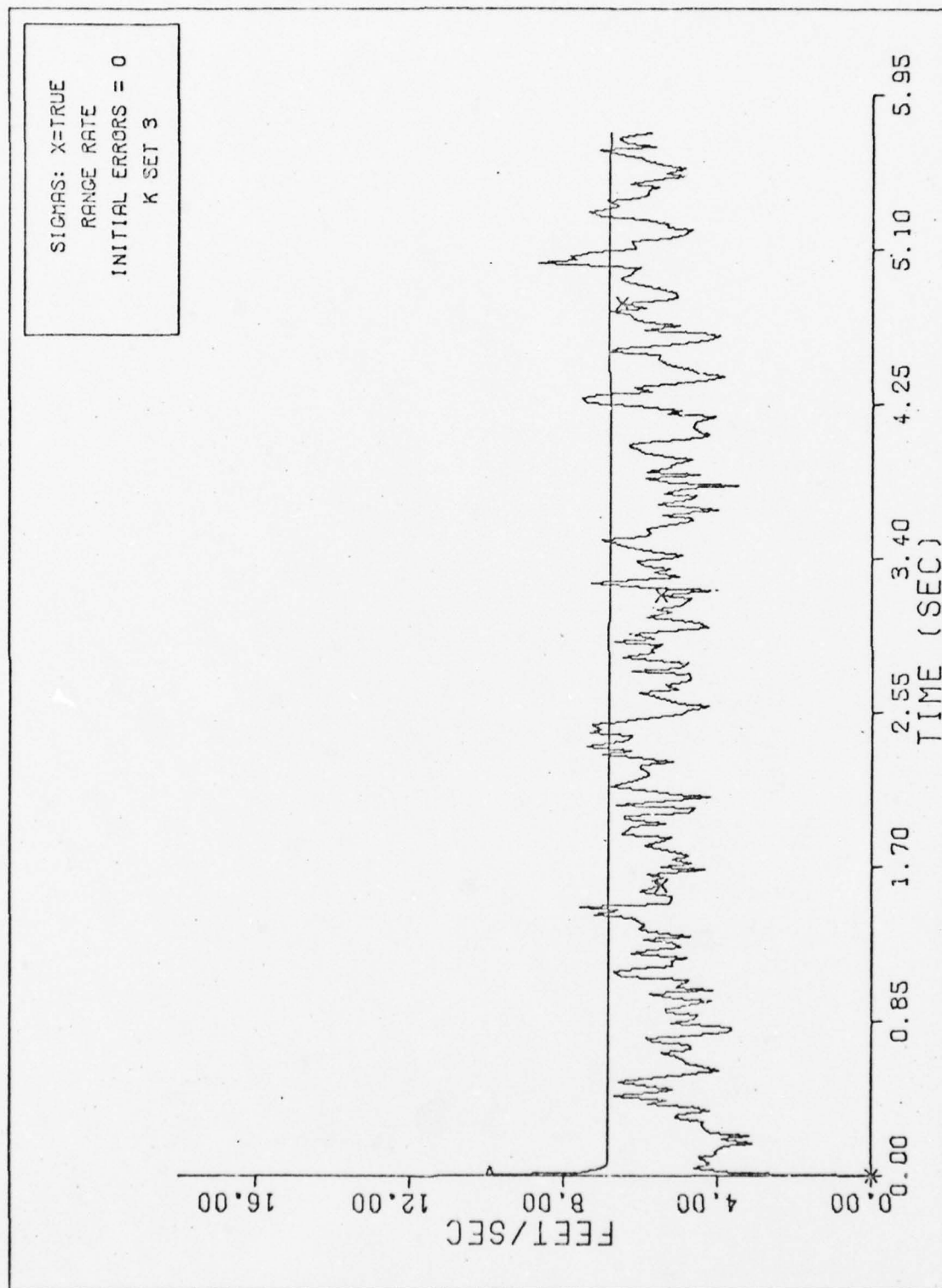


Fig. E-48 RANGE RATE FILTER & TRUE SIGMAS, 11 STATE FILTER

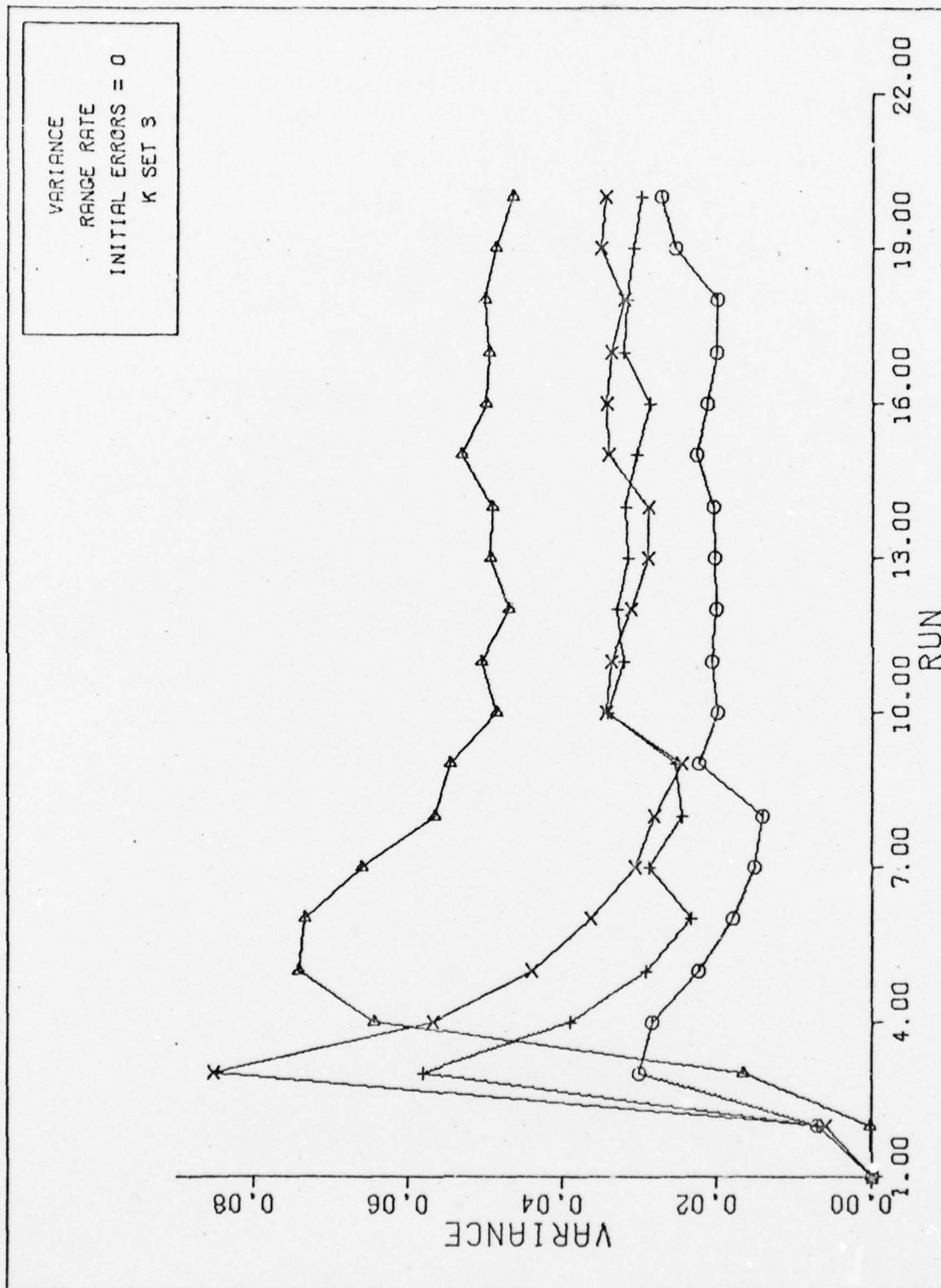


Fig. E-49

VARIANCE CONVERGENCE

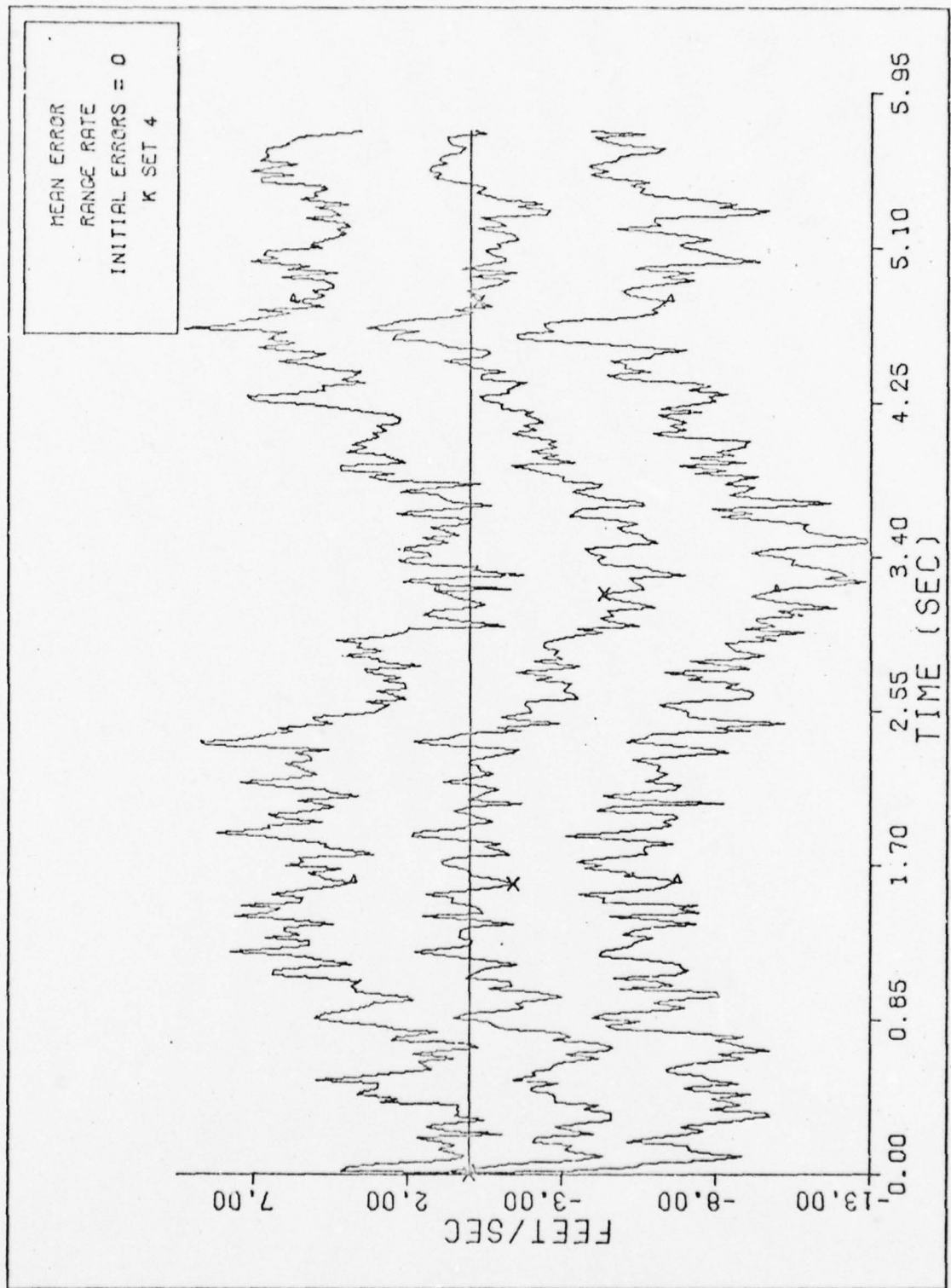


Fig. E-50

RANGE RATE MEAN ERROR, L1 STATE FILTER

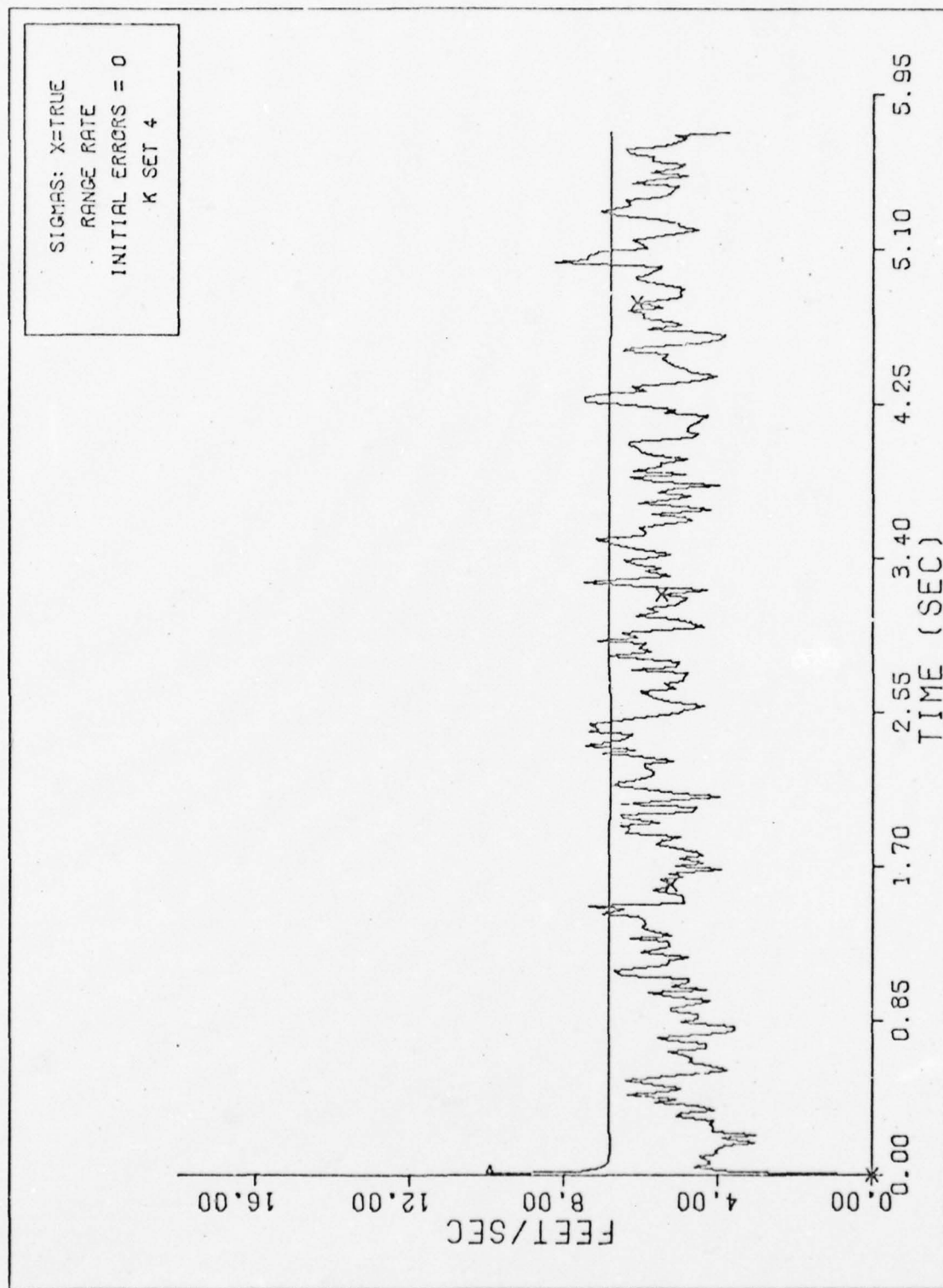


Fig. E-51 RANGE RATE FILTER & TRUE SIGMAS, 11 STATE FILTER

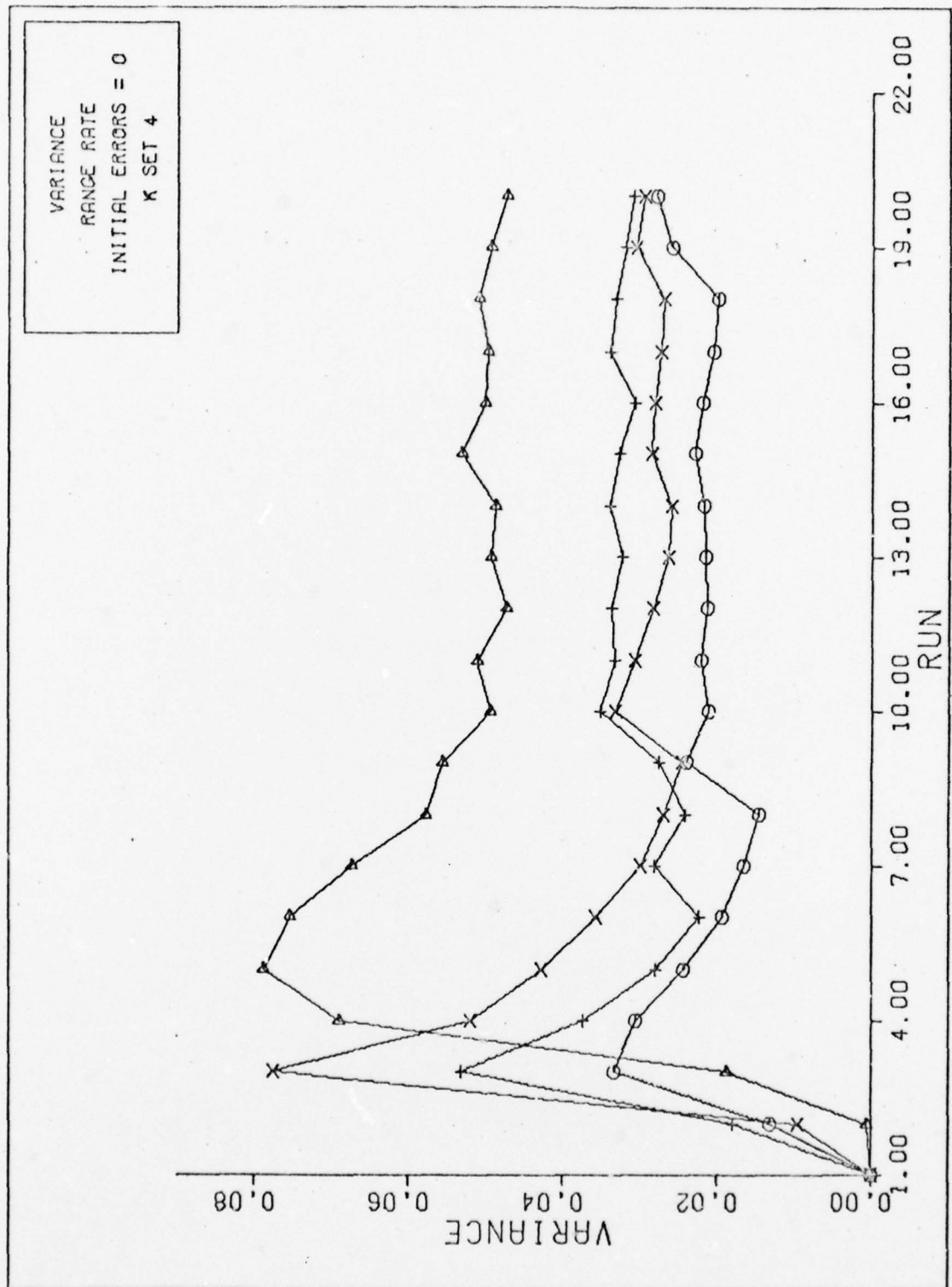


Fig. E-52

VARIANCE CONVERGENCE

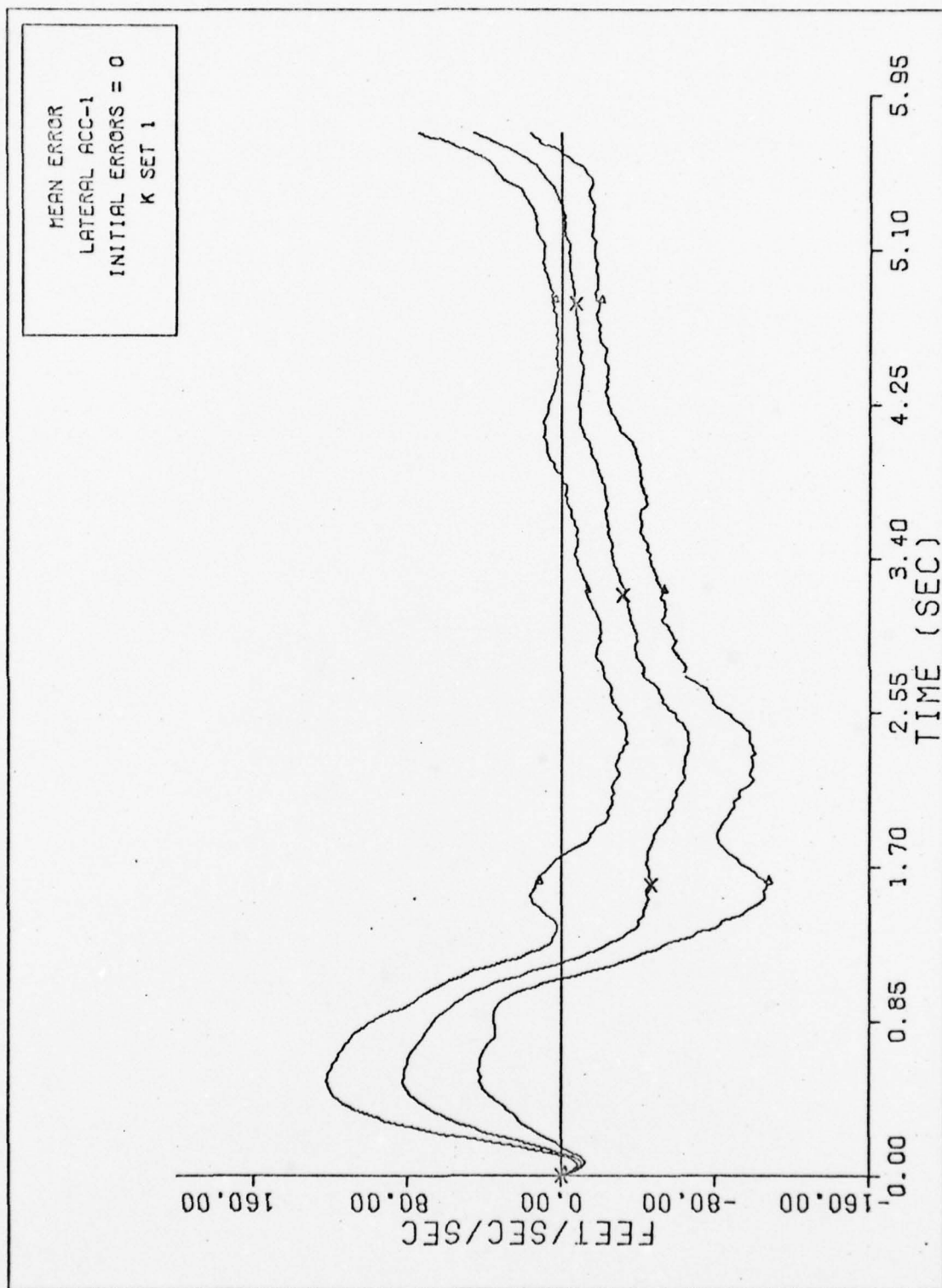


Fig. E-53

LATERAL ACC-1 MEAN ERROR, 11 STATE FILTER

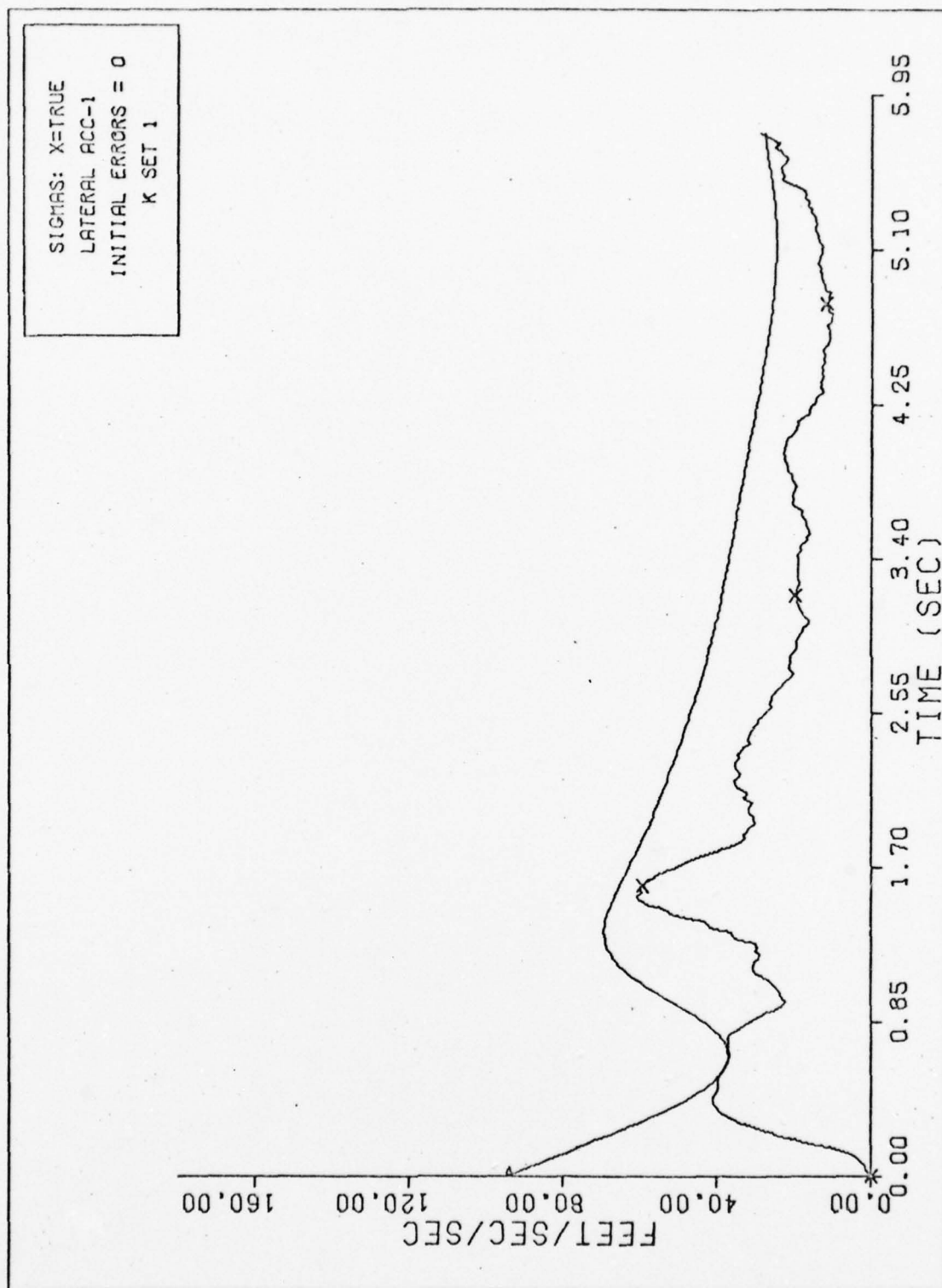


Fig. E-54 LAT ACC-1 FILTER & TRUE SIGMAS, L1 STATE FILTER

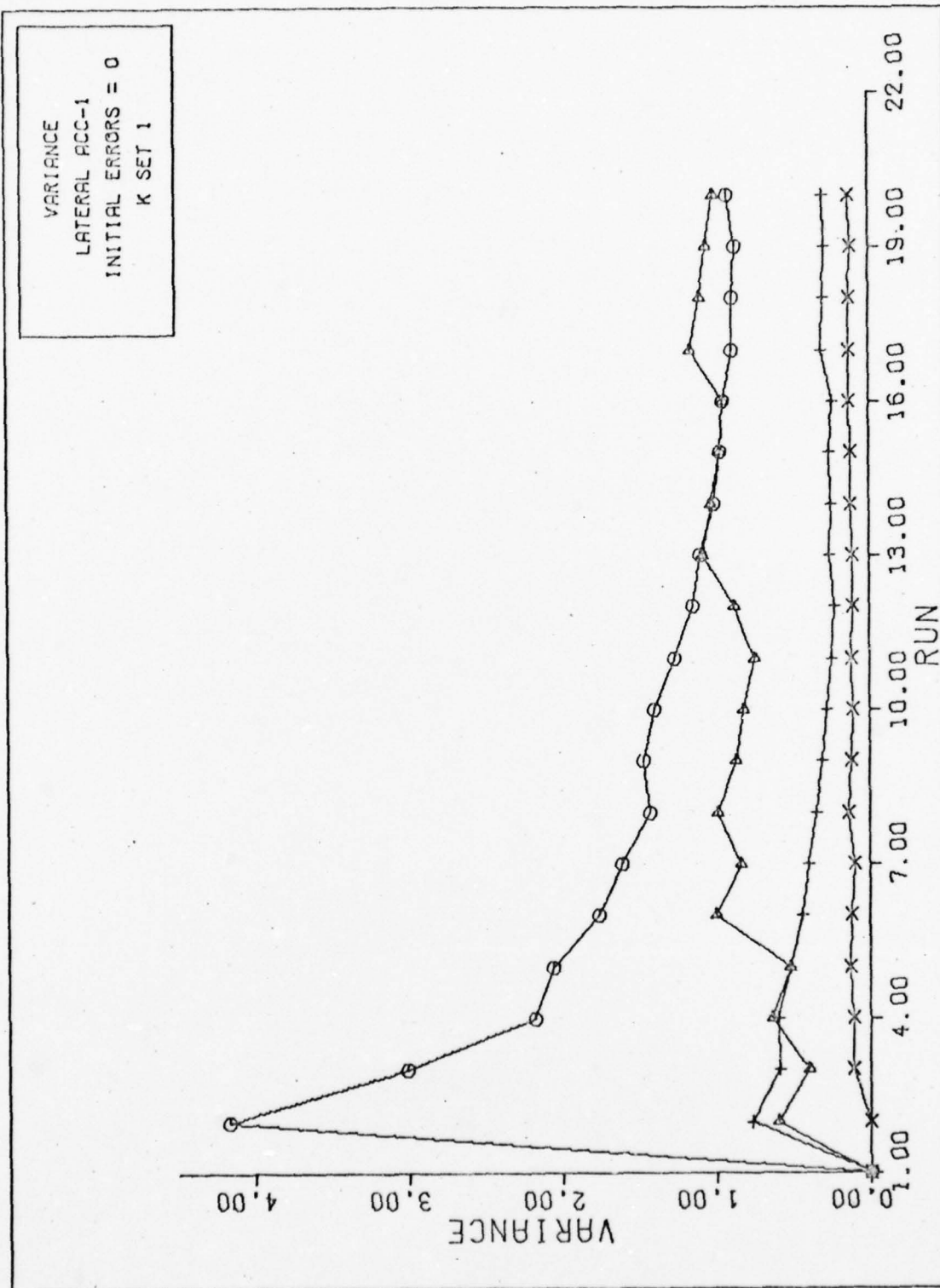


Fig. E-55

VARIANCE CONVERGENCE

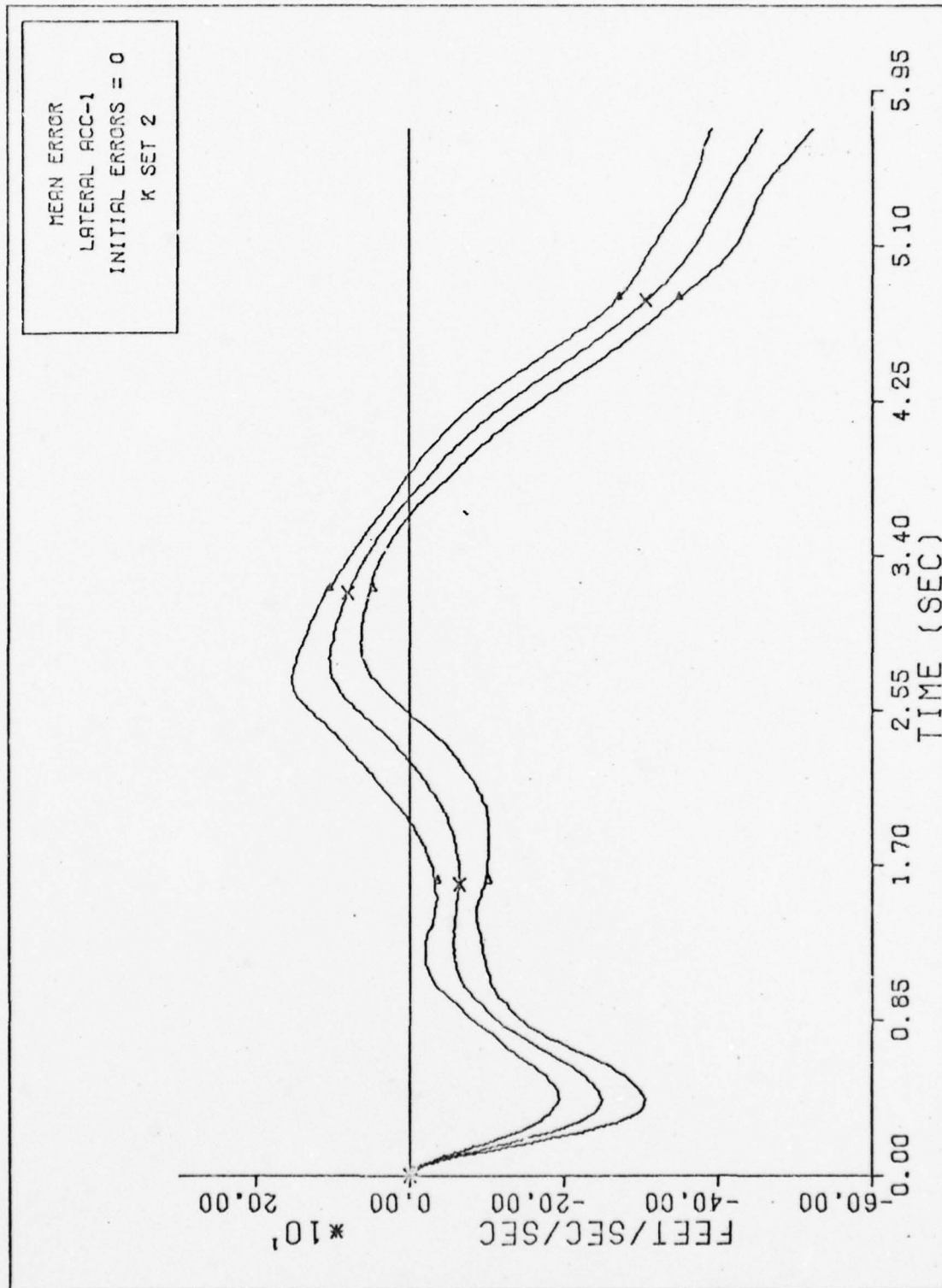


Fig. E-56

LATERAL ACC-1 MEAN ERROR, 11 STATE FILTER

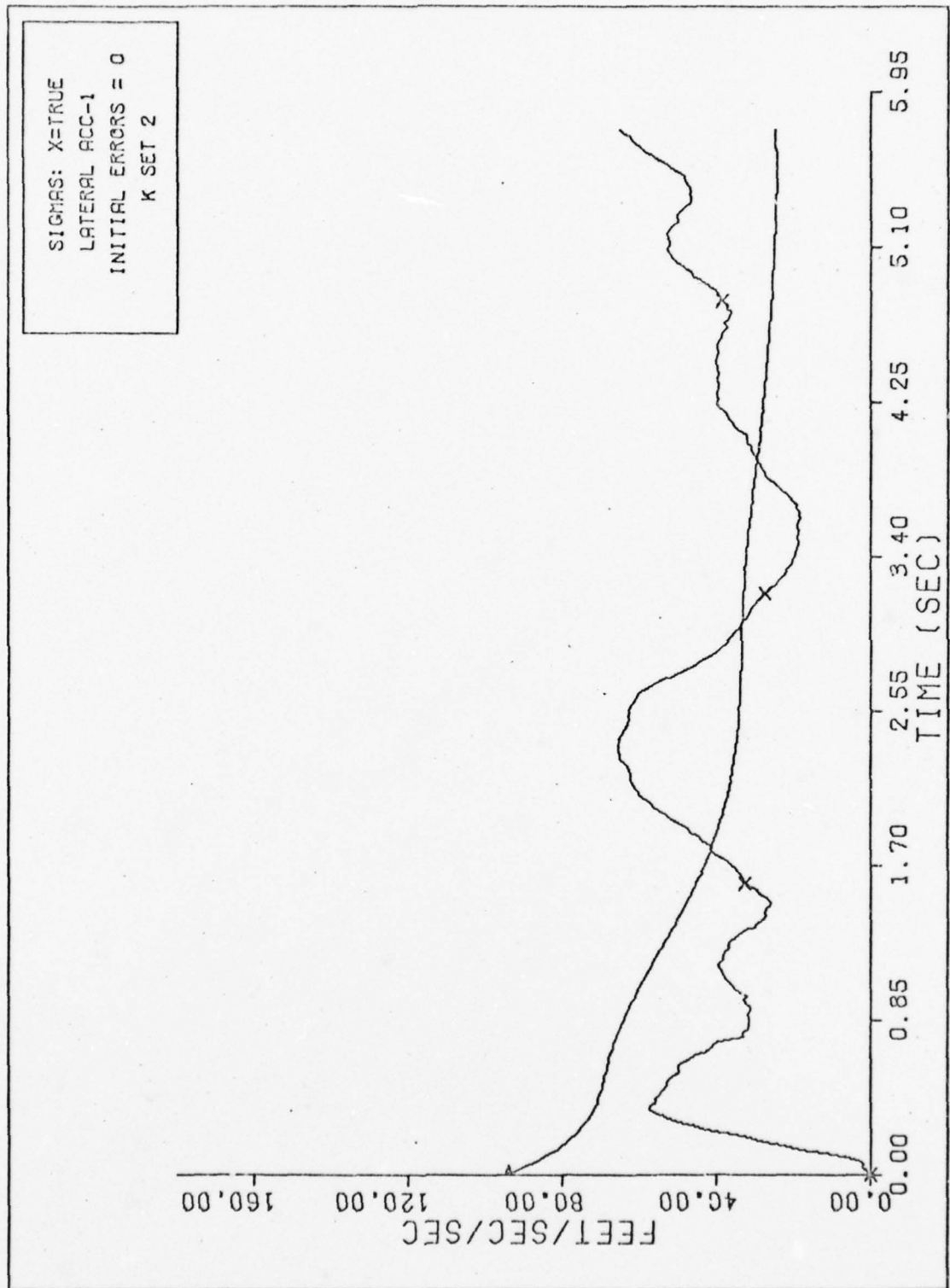


Fig. E-57 LAT ACC-1 FILTER & TRUE SIGMAS, 11 STATE FILTER

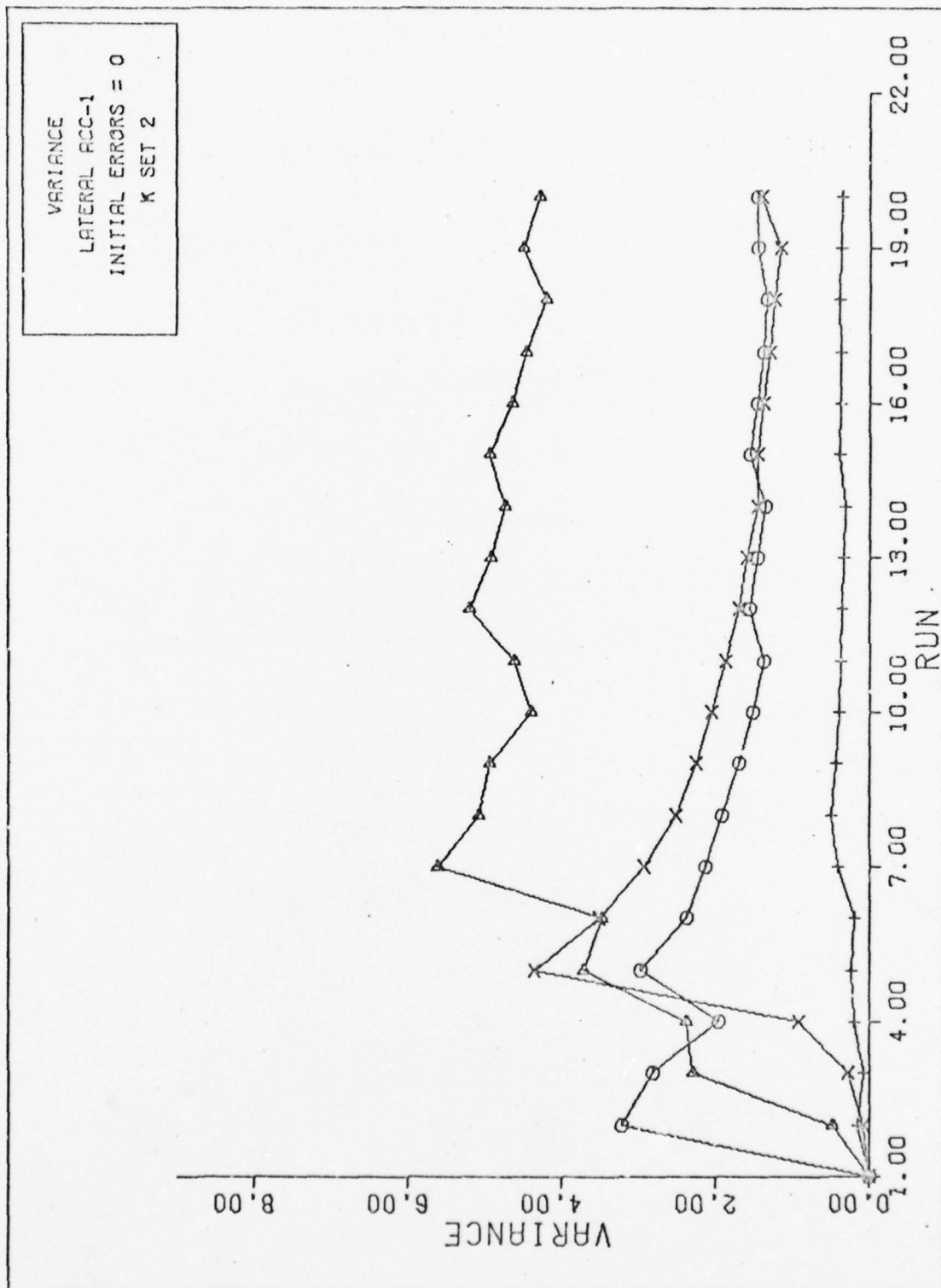


Fig. E-58

VARIANCE CONVERGENCE

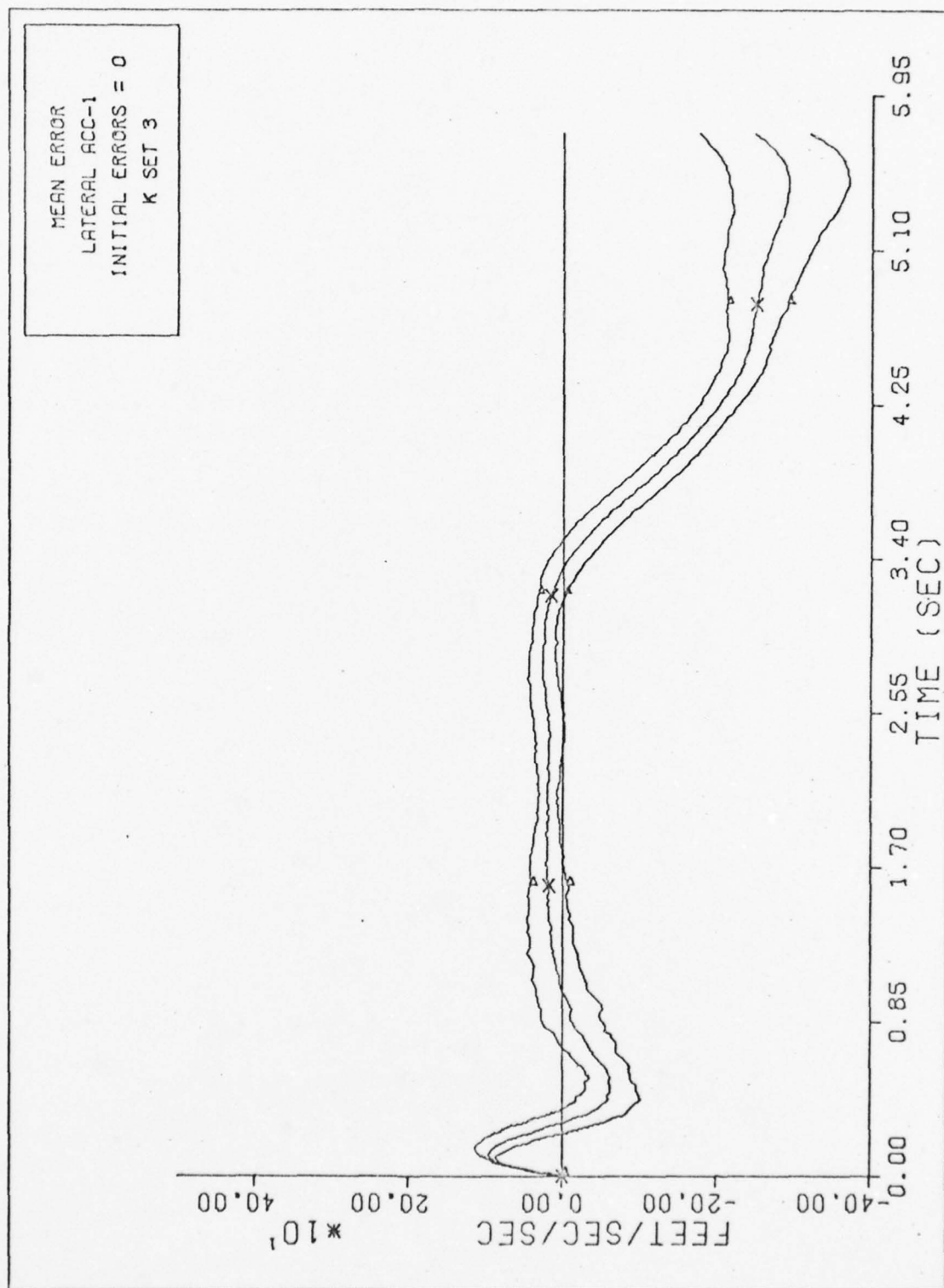


Fig. E-59

LATERAL ACC-1 MEAN ERROR, 11 STATE FILTER

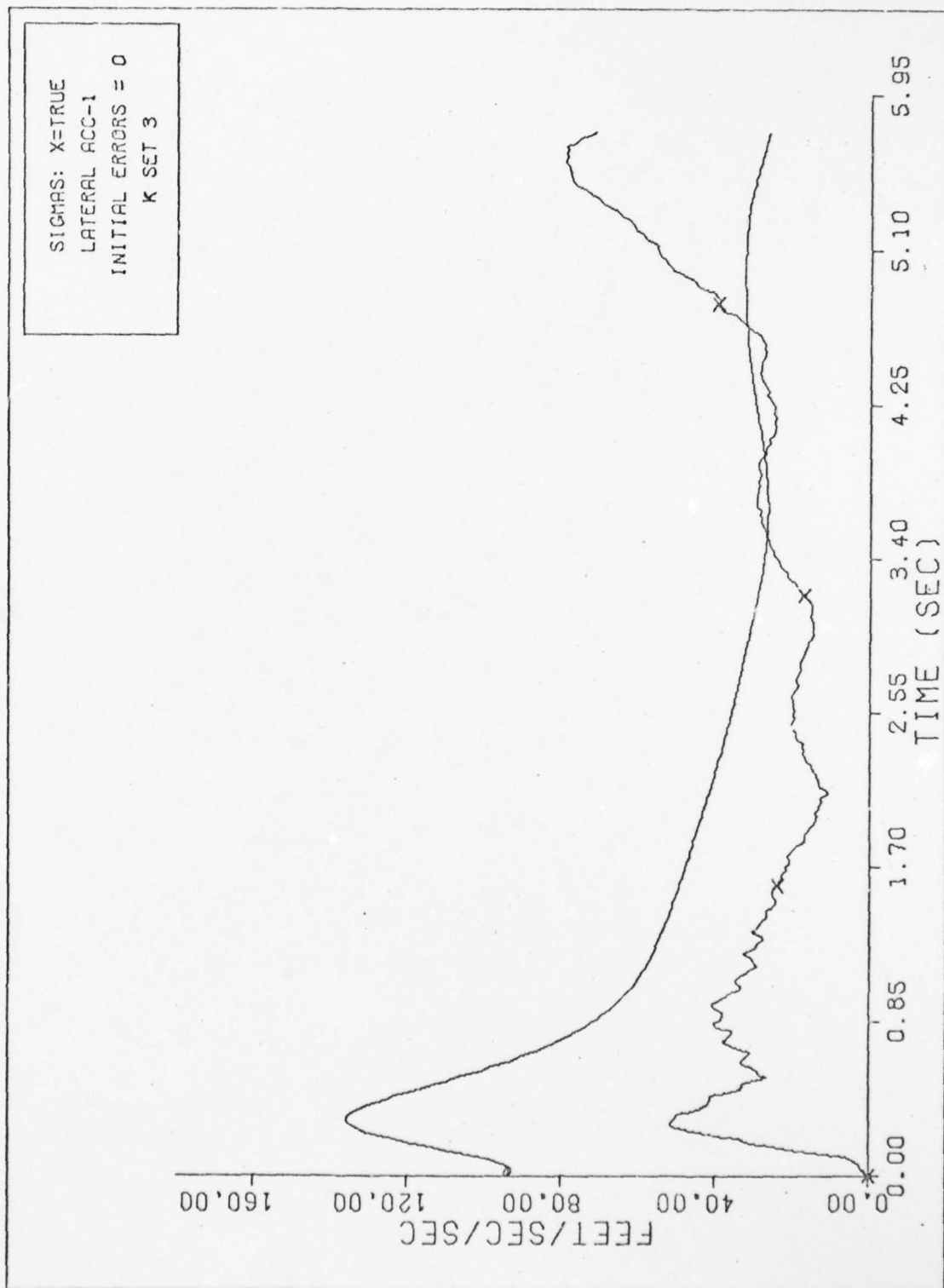


Fig. E-60 LAT ACC-1 FILTER & TRUE SIGMAS, 11 STATE FILTER

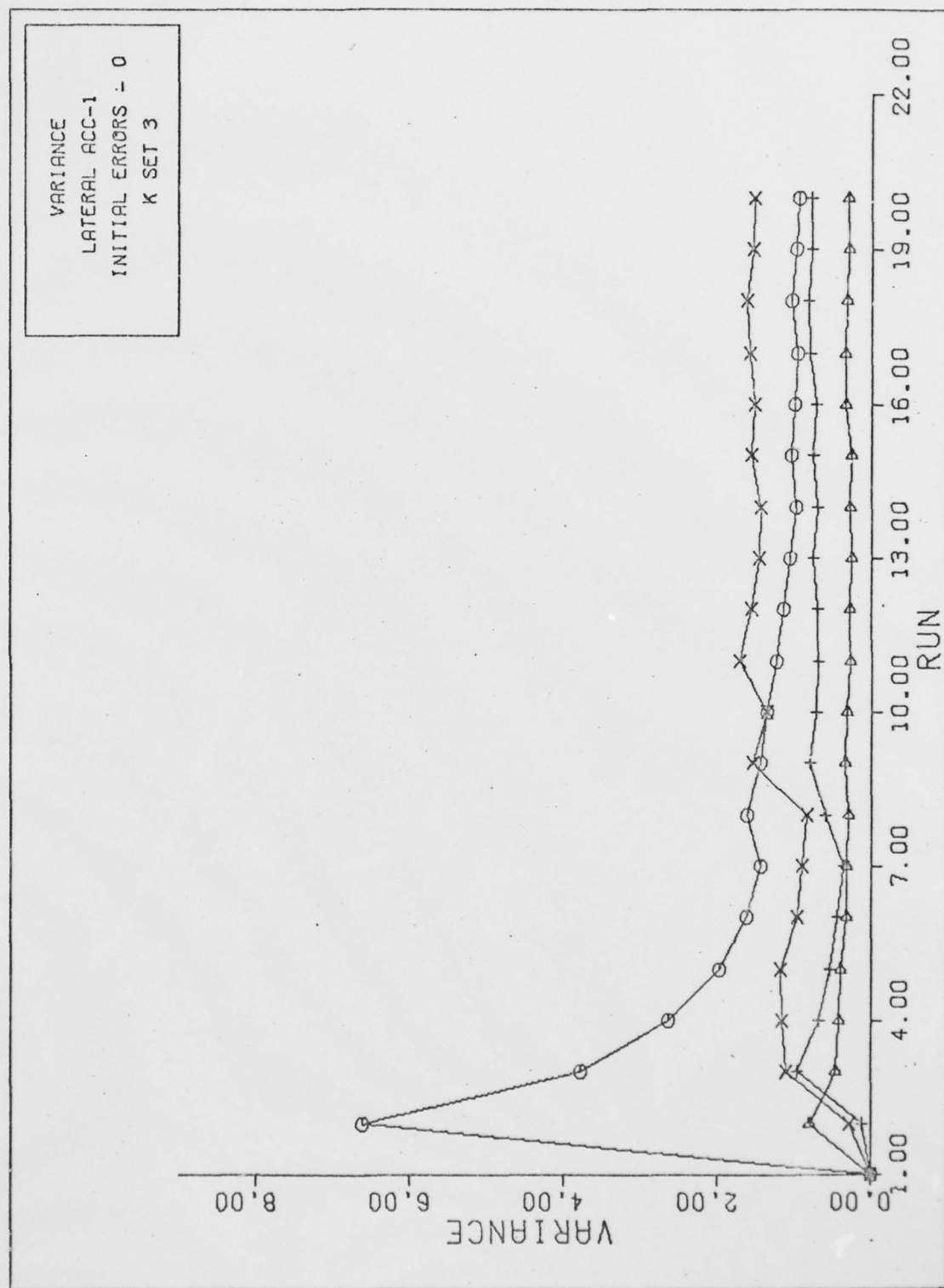


Fig. E-61

VARIANCE CONVERGENCE

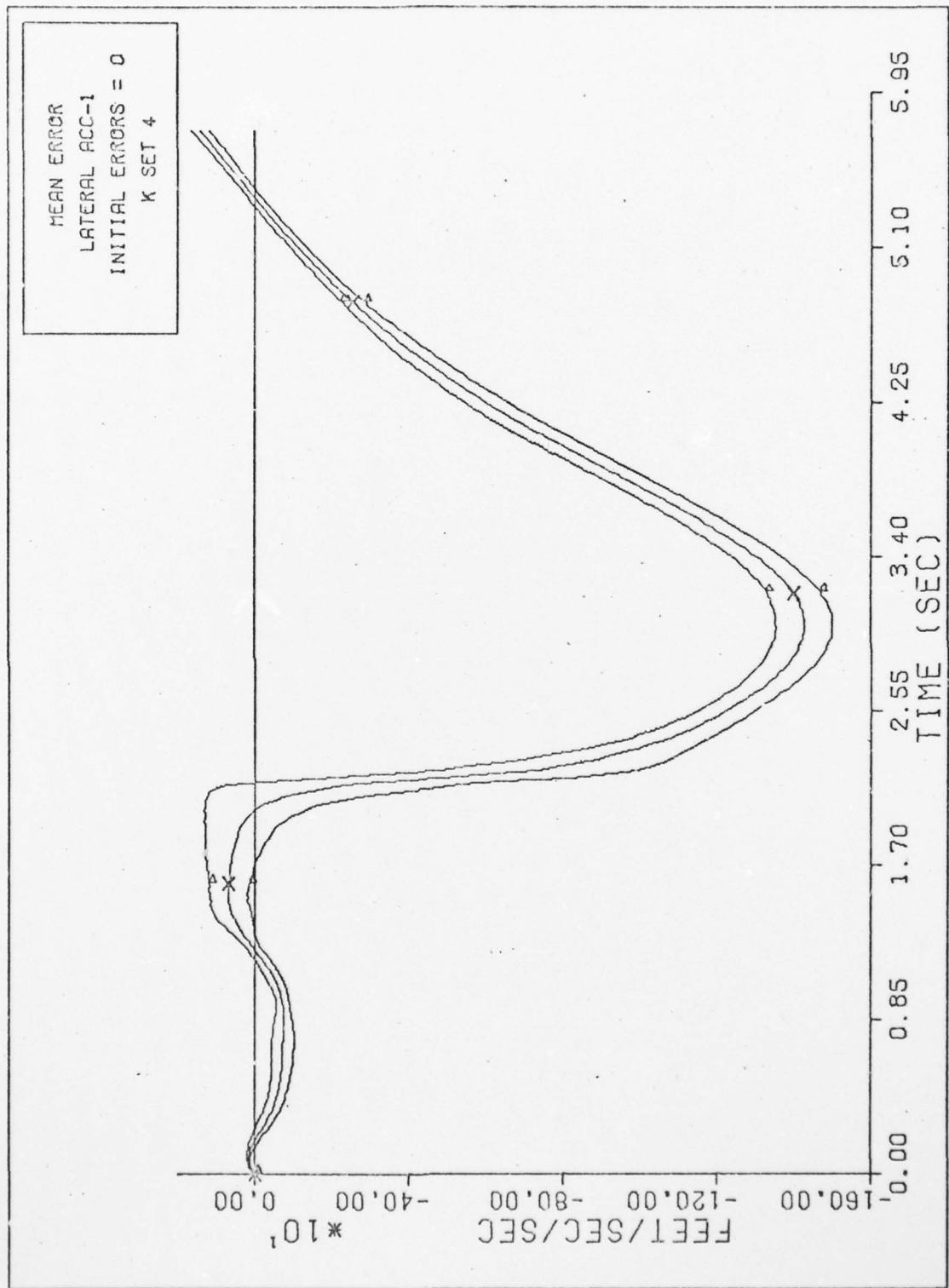


Fig. E-62

LATERAL ACC-1 MEAN ERROR, 11 STATE FILTER

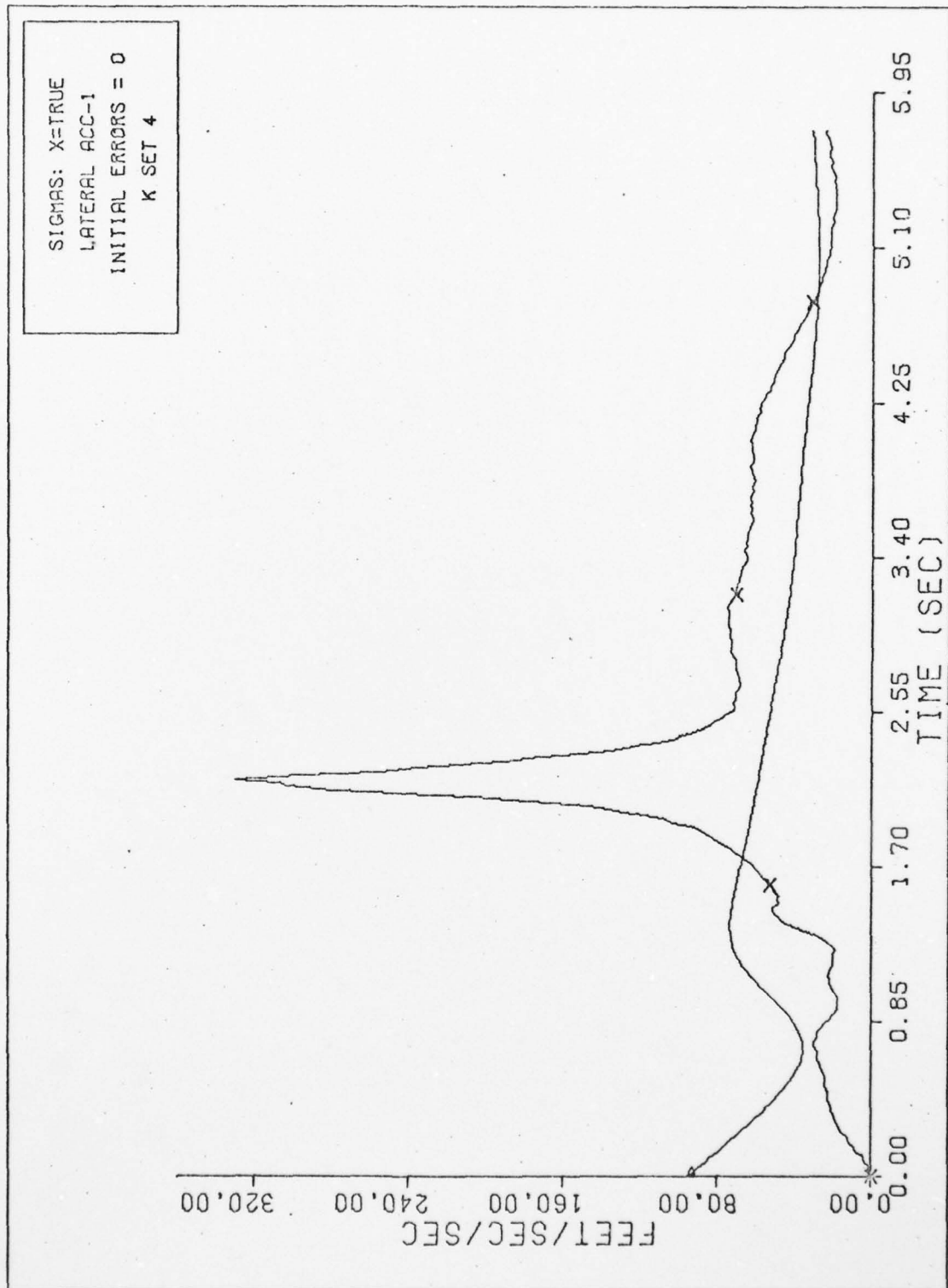


Fig. E-63 LAT ACC-1 FILTER & TRUE SIGMAS, 11 STATE FILTER

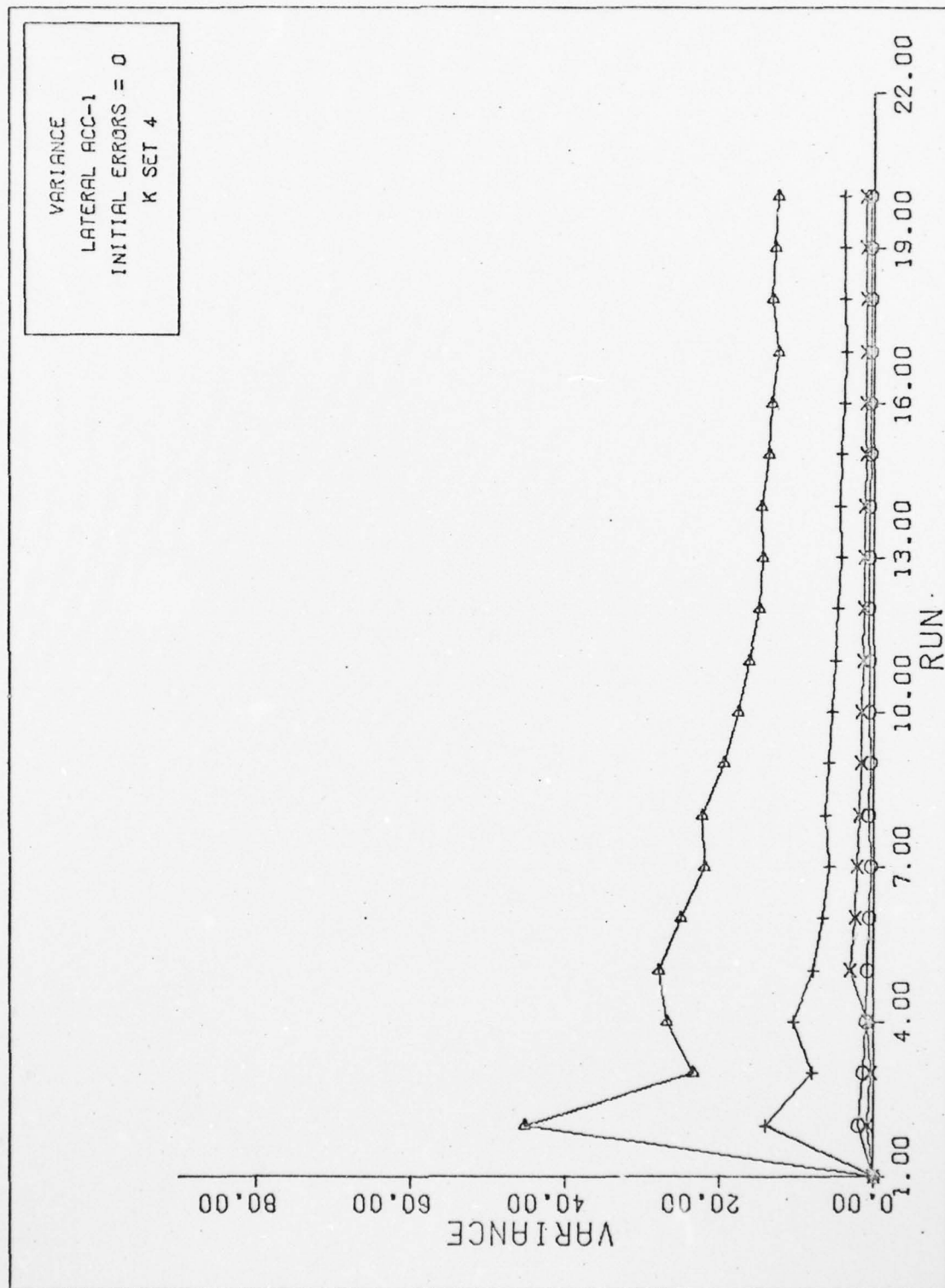


Fig. E-64

VARIANCE CONVERGENCE

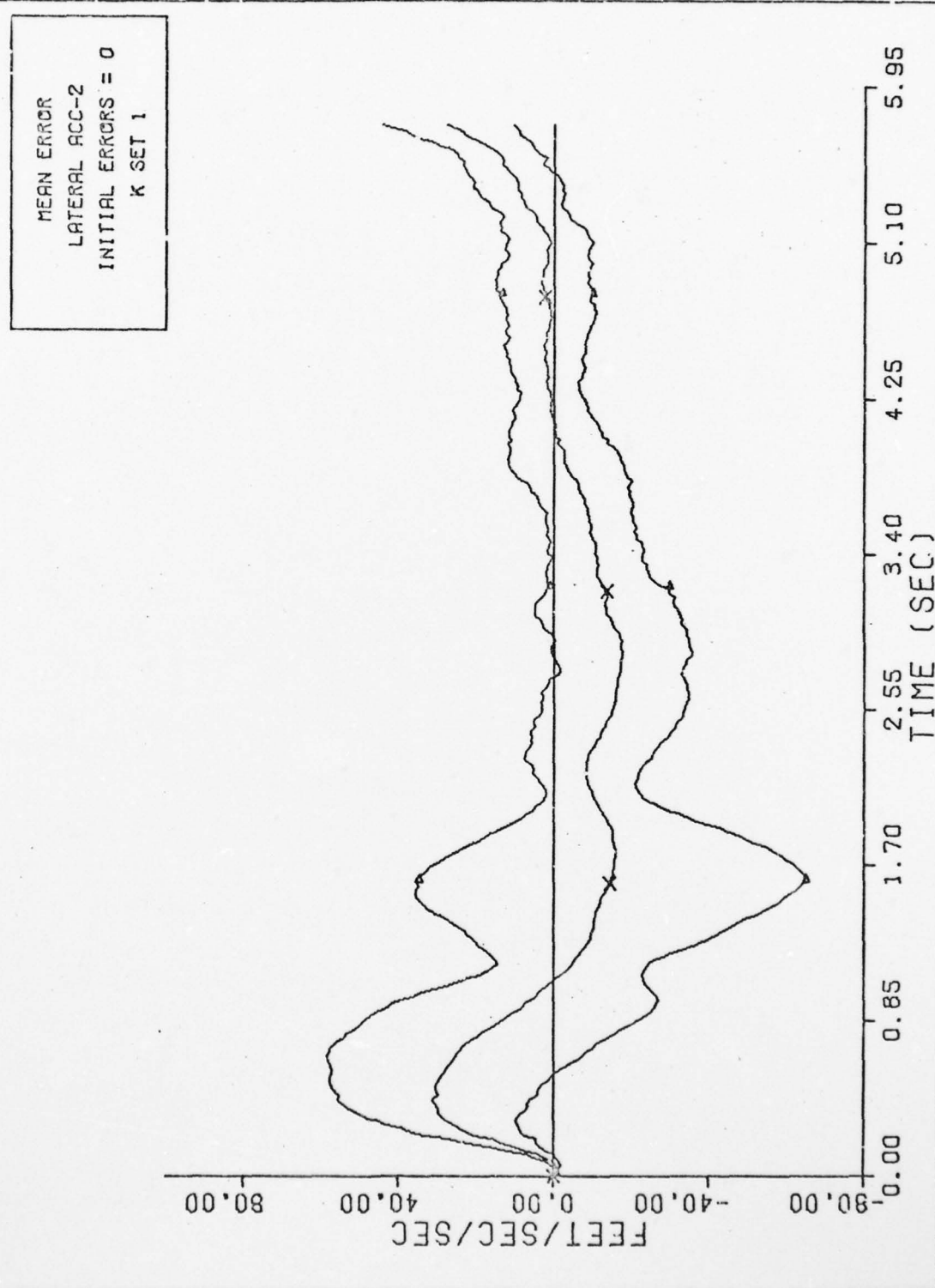


Fig. E-65

LATERAL ACC-2 MEAN ERROR, 11 STATE FILTER

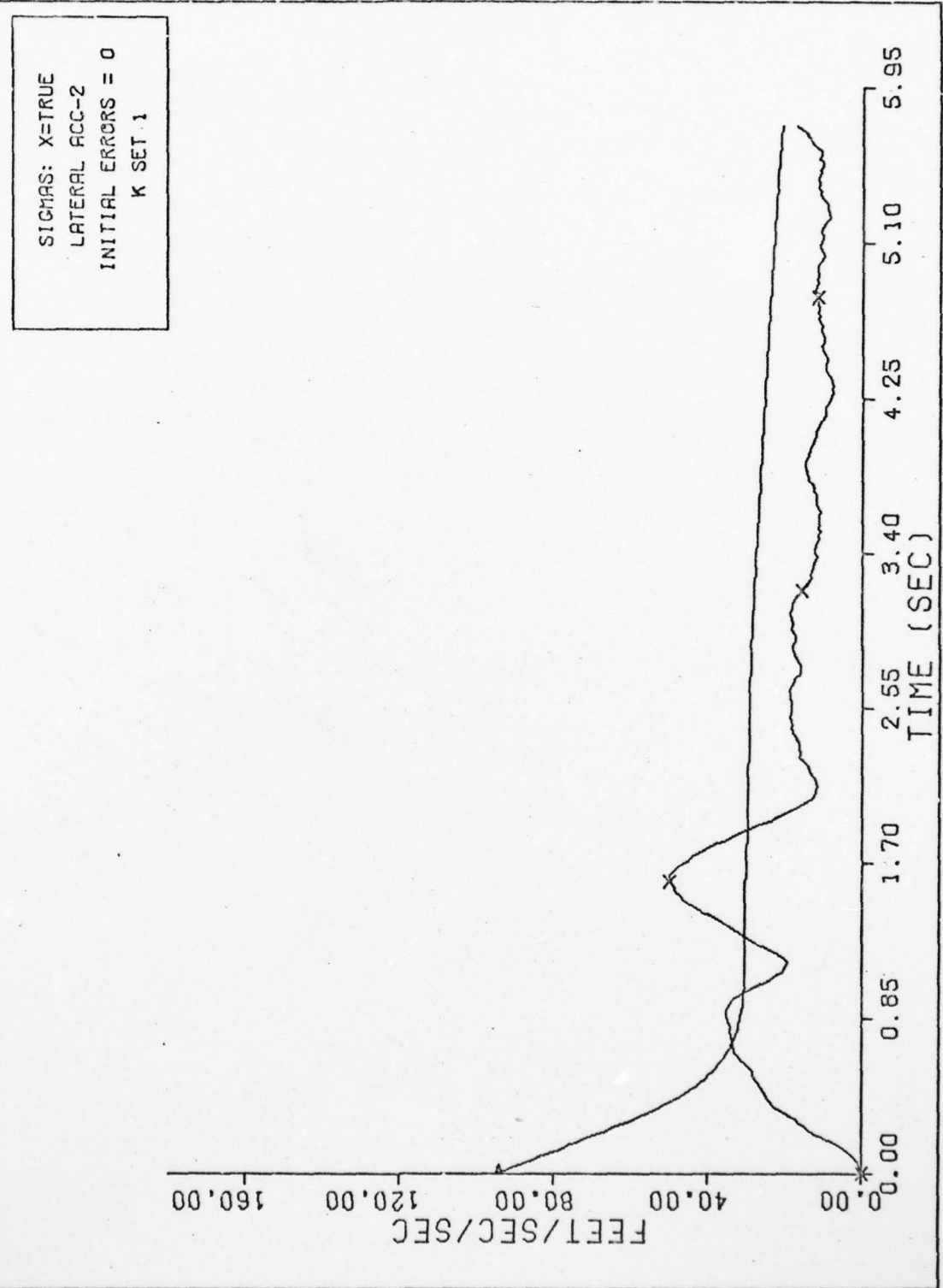


Fig. E-66 LAT ACC-2 FILTER & TRUE SIGMAS, L1 STATE FILTER

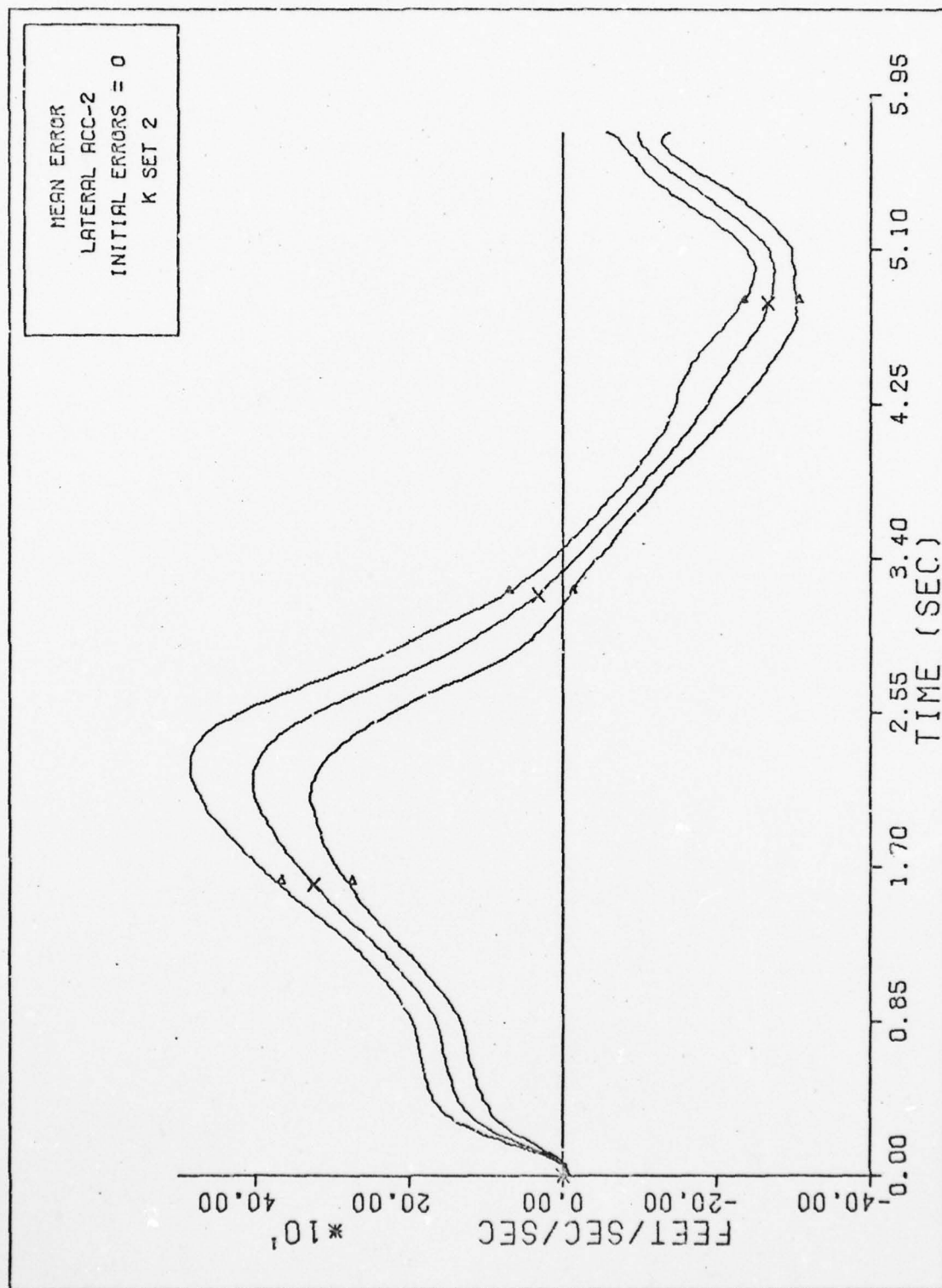


Fig. E-67

LATERAL ACC-2 MEAN ERROR, 11 STATE FILTER

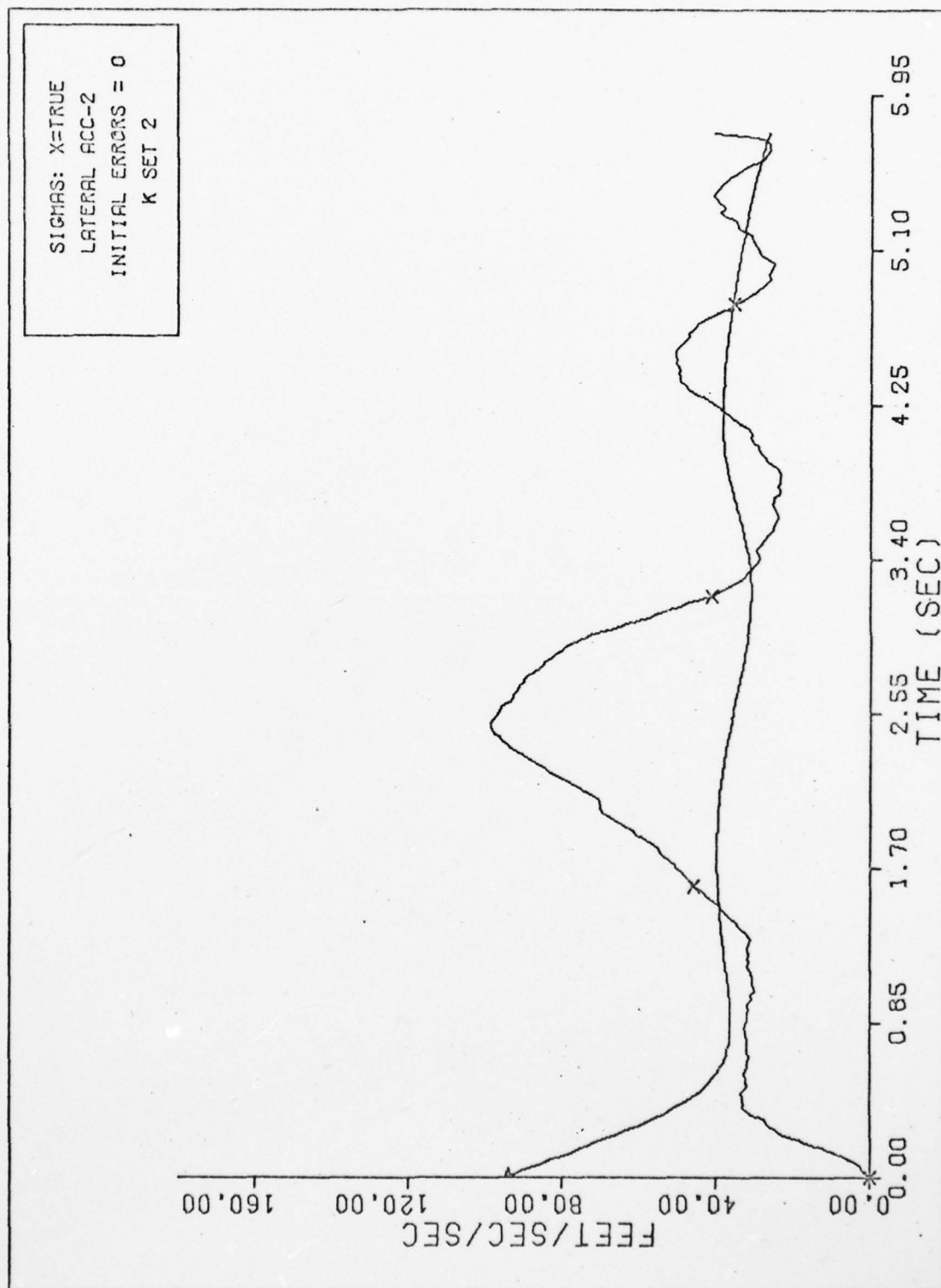


Fig. E-68 LAT ACC-2 FILTER & TRUE SIGMAS, 11 STATE FILTER

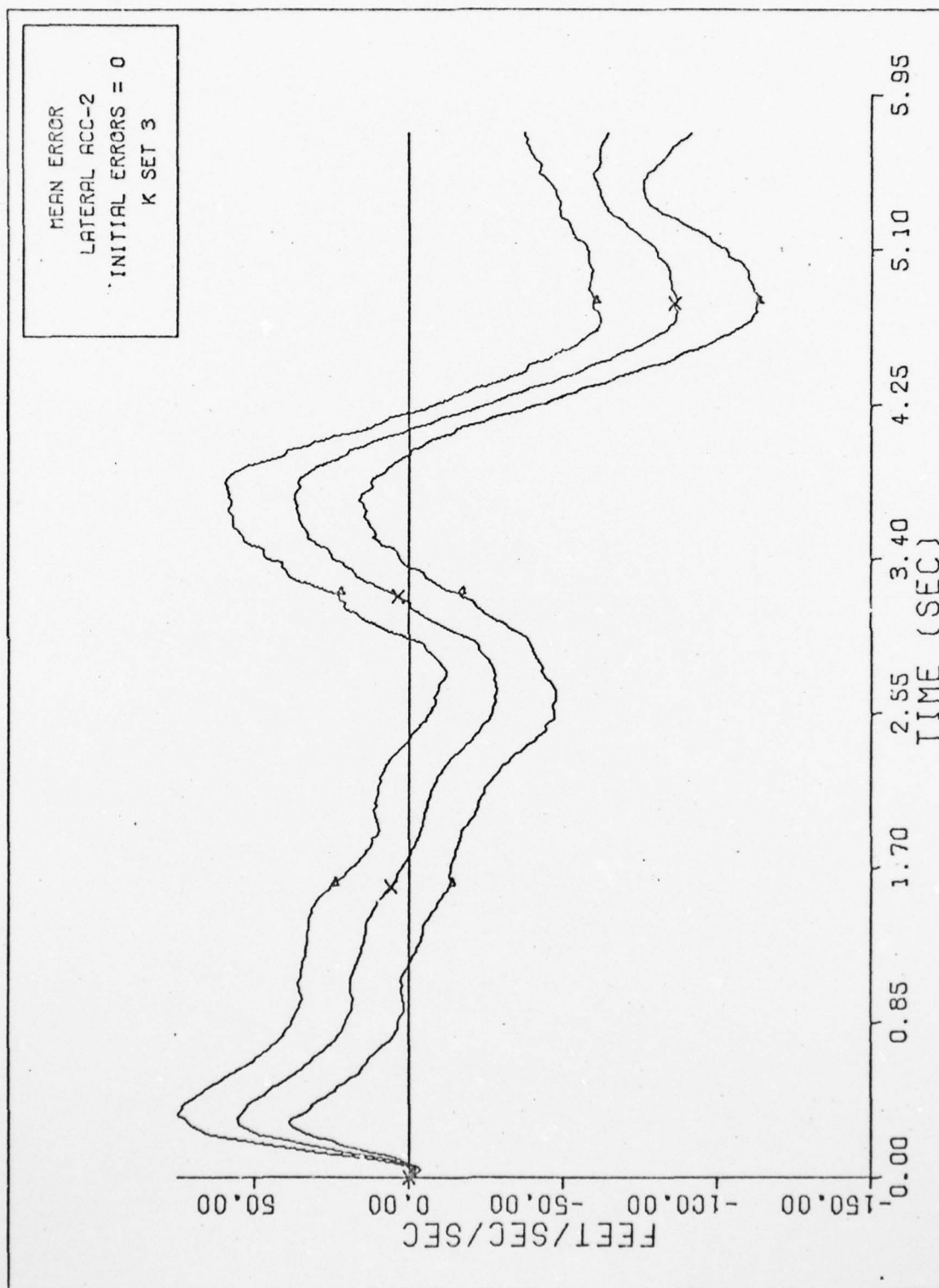


Fig. E-69

LATERAL ACC-2 MEAN ERROR, 11 STATE FILTER

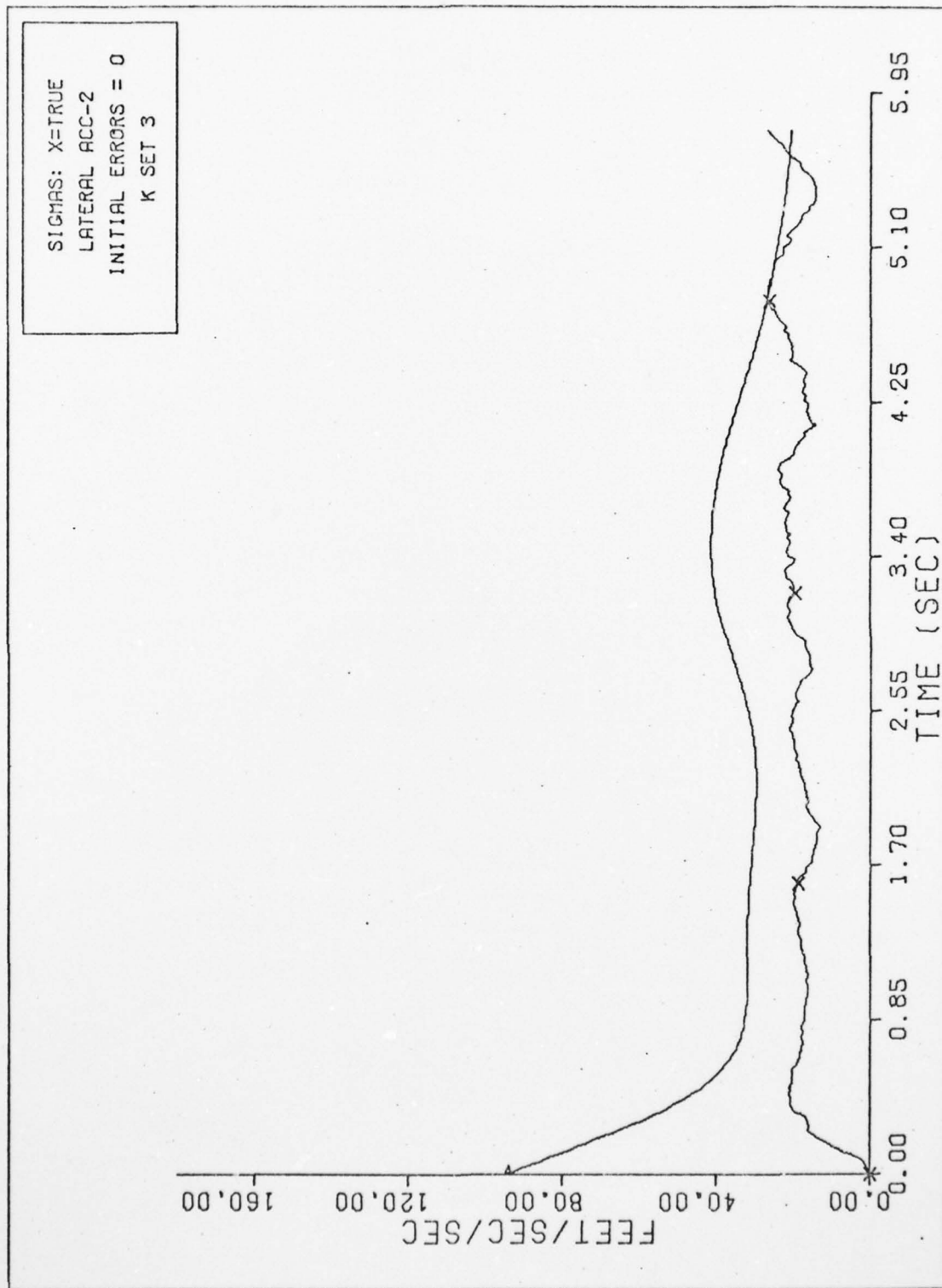


Fig. E-70 LAT ACC-2 FILTER & TRUE SIGMAS, L1 STATE FILTER

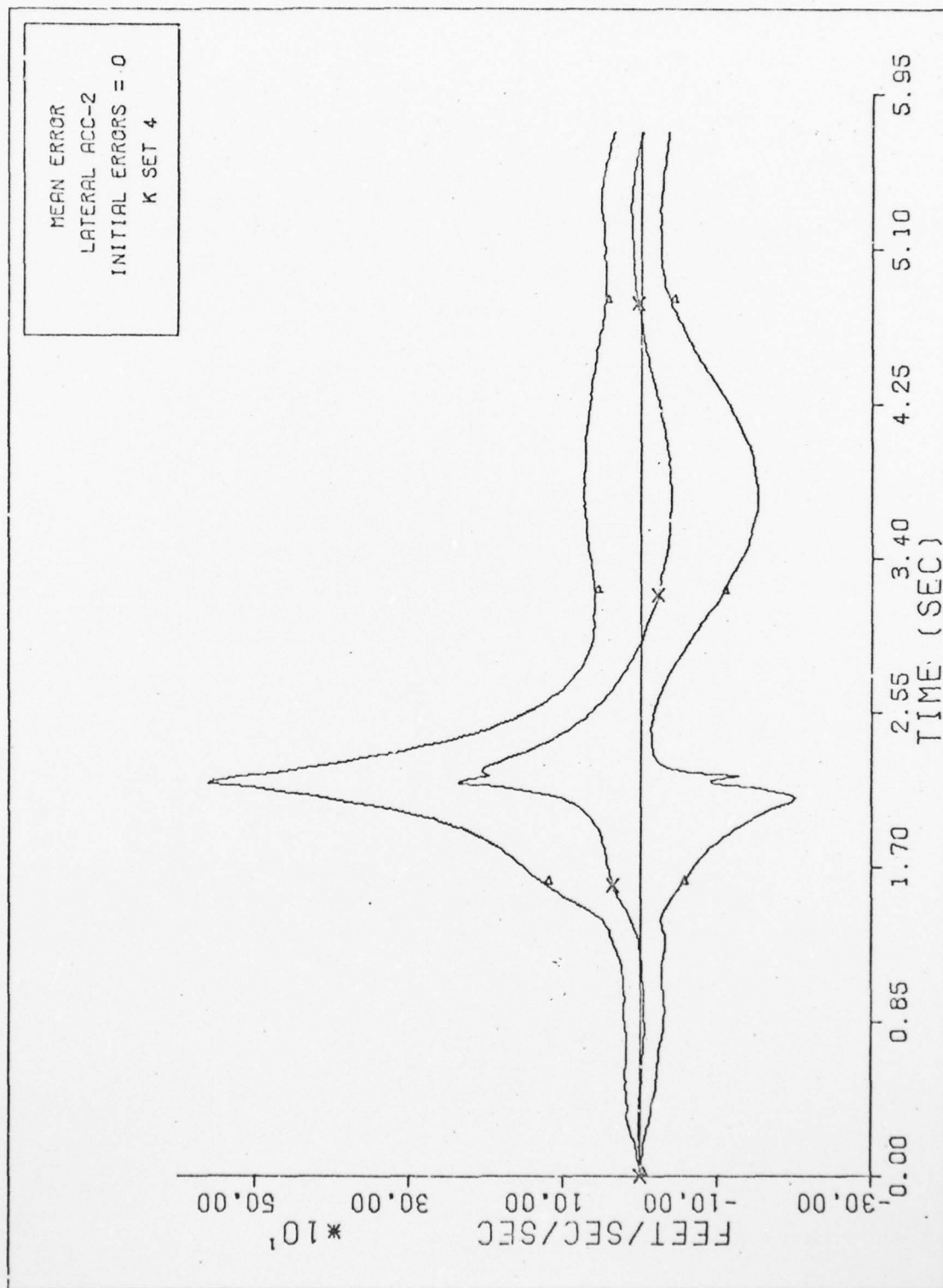


Fig. E-71

LATERAL ACC-2 MEAN ERROR, 11 STATE FILTER

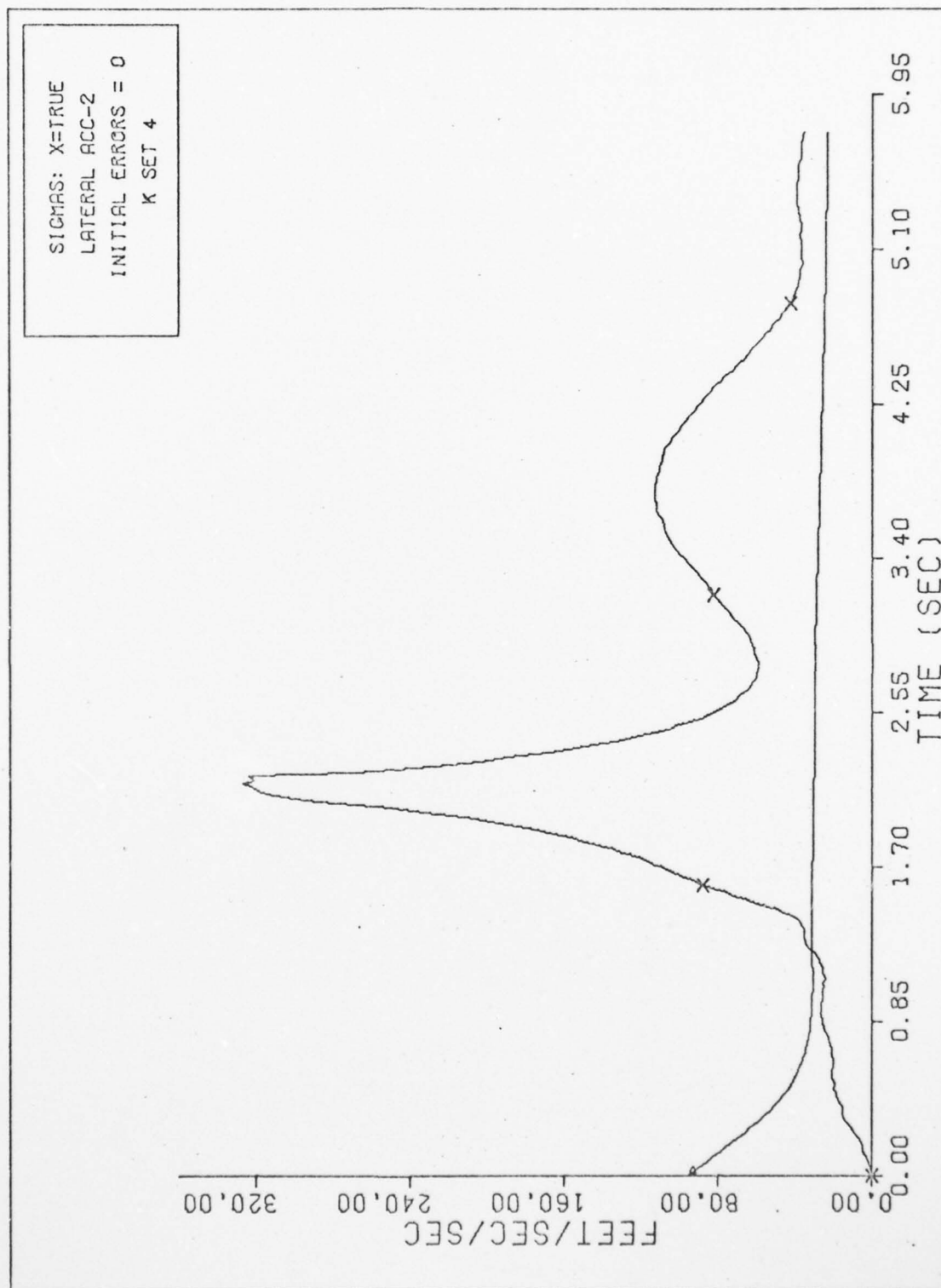


Fig. E-72 LAT ACC-2 FILTER & TRUE SIGMAS, L1 STATE FILTER

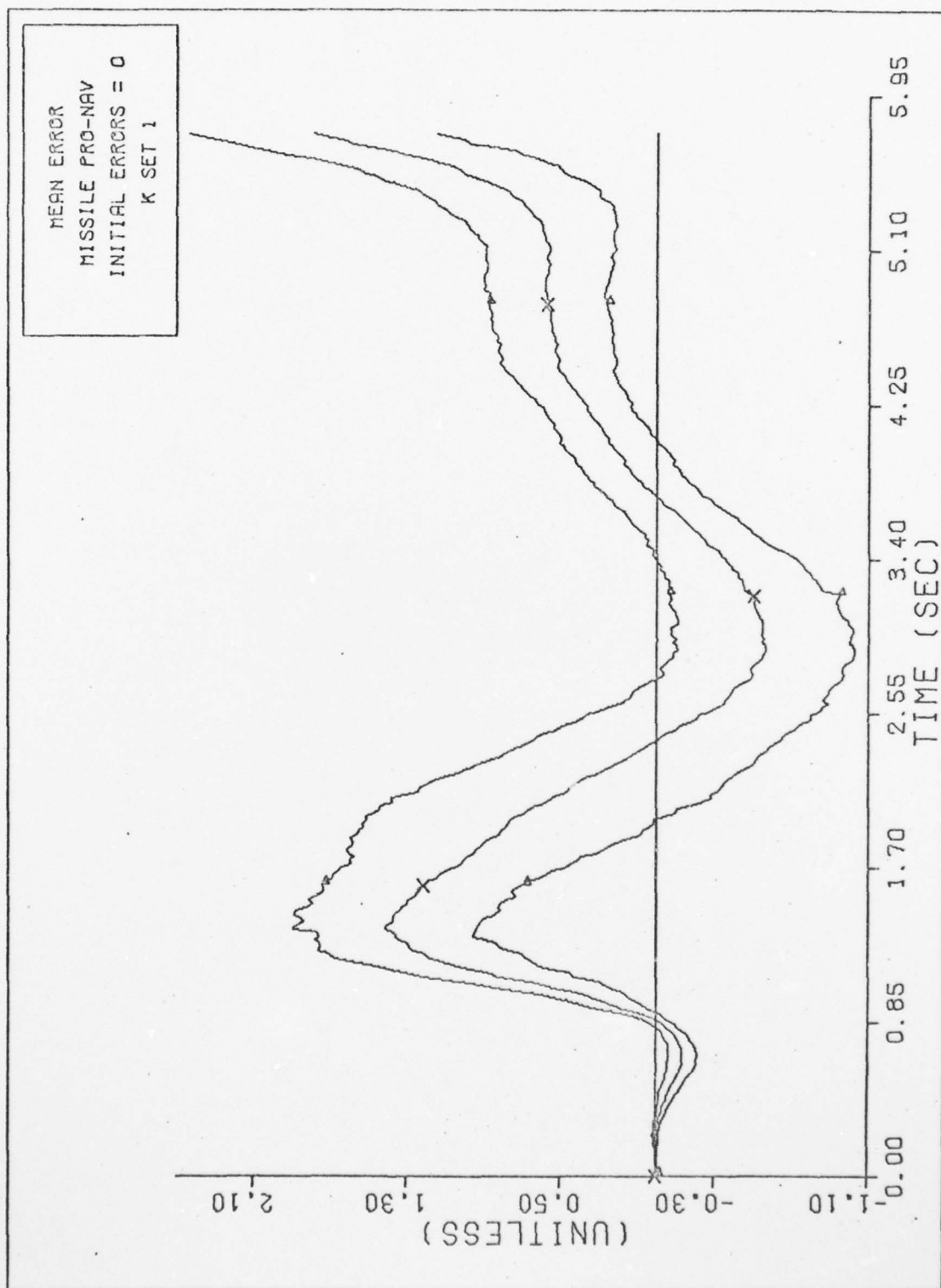


Fig. E-73 MISSILE PRO-NAV MEAN ERROR, 11 STATE FILTER

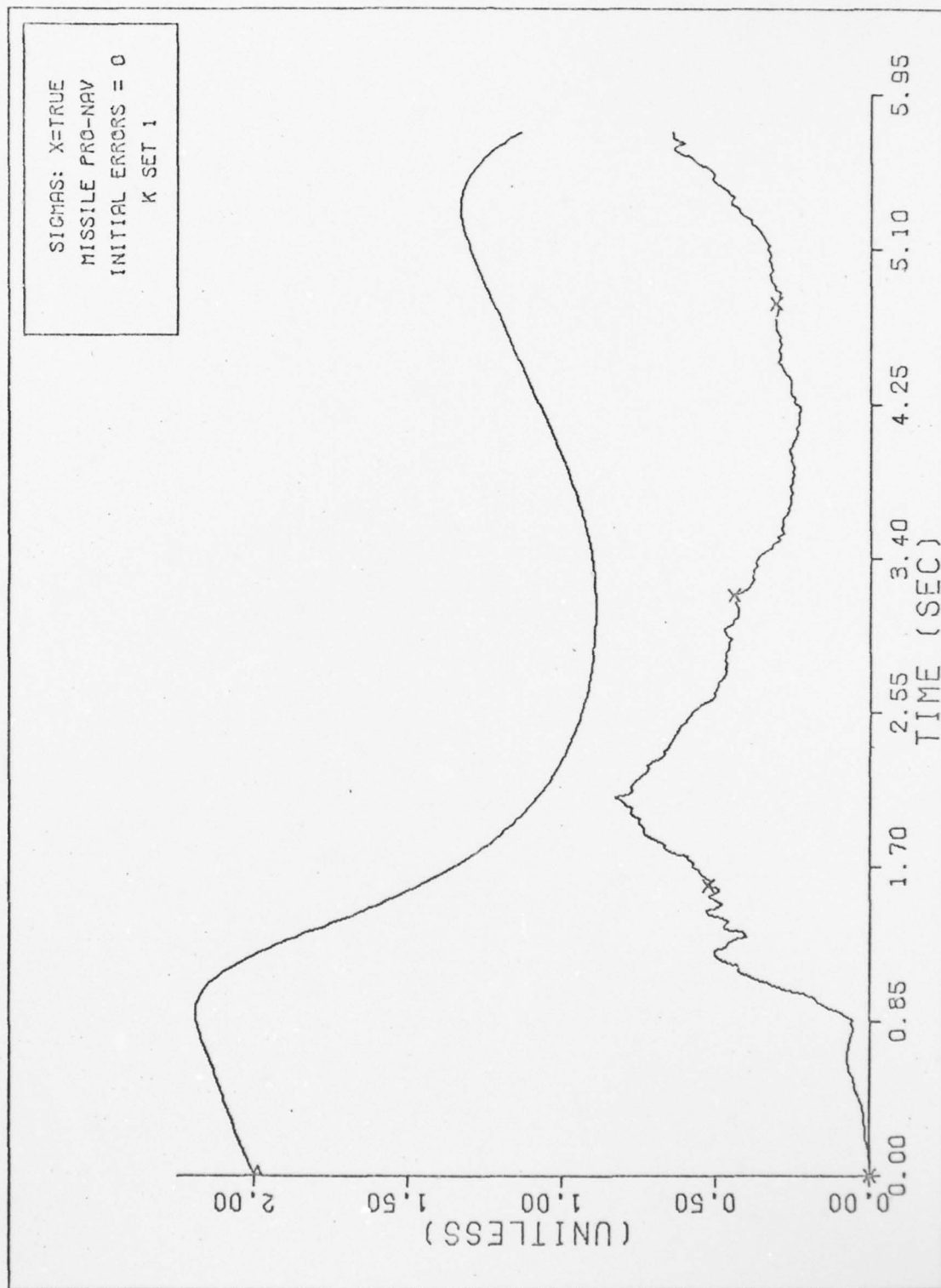


Fig. E-74

PRO-NAV FILTER & TRUE SIGMAS, 11 STATE FILTER

AD-A064 760

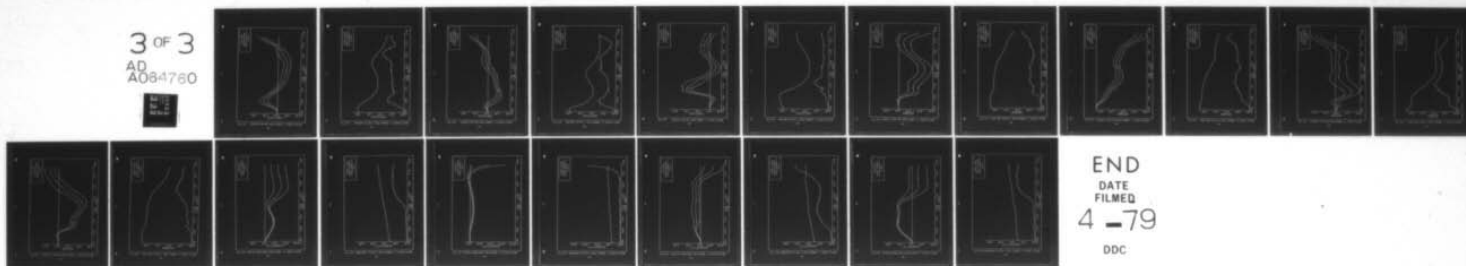
AIR FORCE INST OF TECH WRIGHT-PATTERSON AFB OHIO SCH--ETC F/G 15/3.1
A PRACTICAL THREE DIMENSIONAL, 11 STATE EXTENDED KALMAN FILTER --ETC(U)
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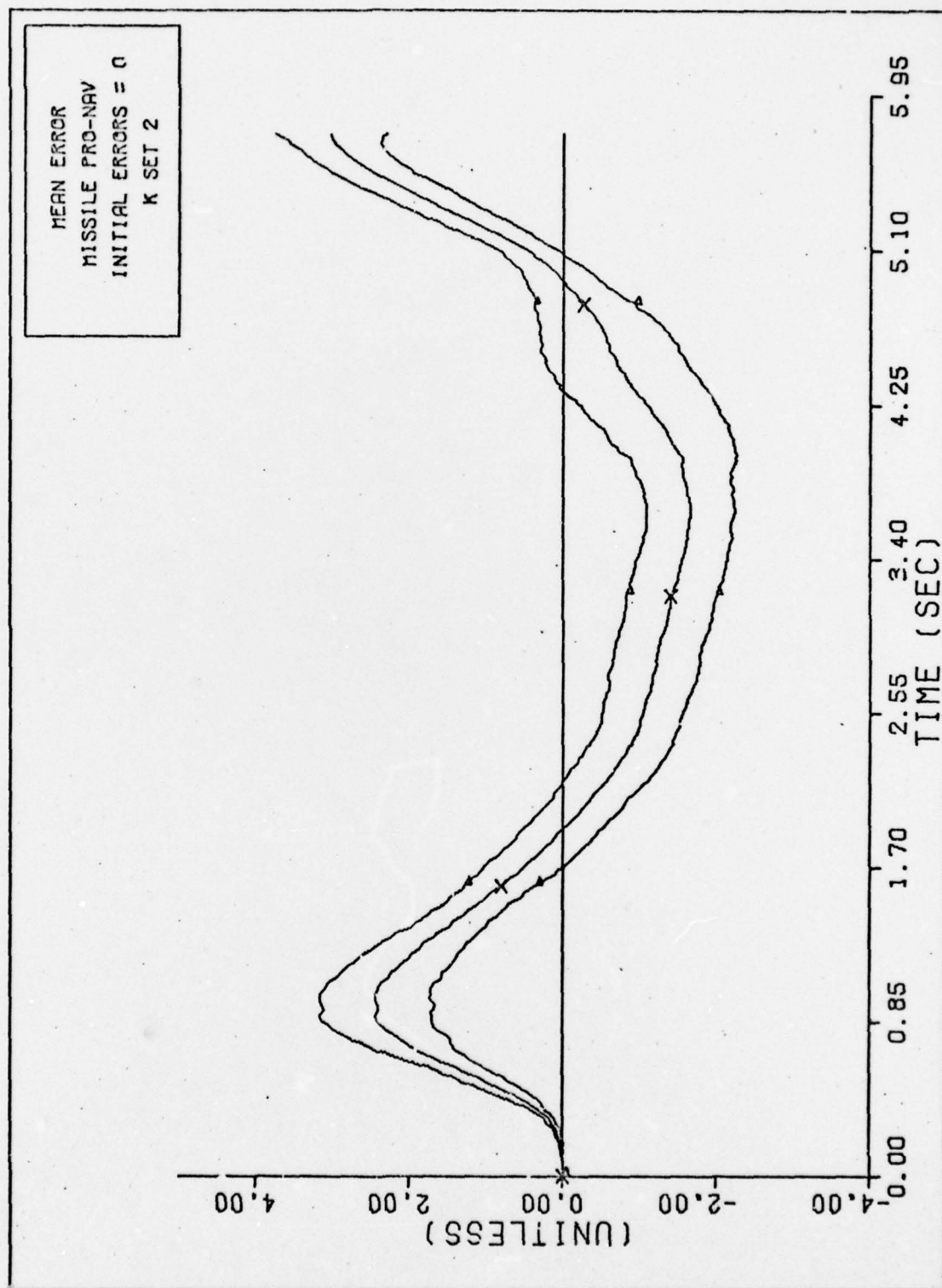


Fig. E-75 MISSILE PRO-NAV MEAN ERROR, 11 STATE FILTER

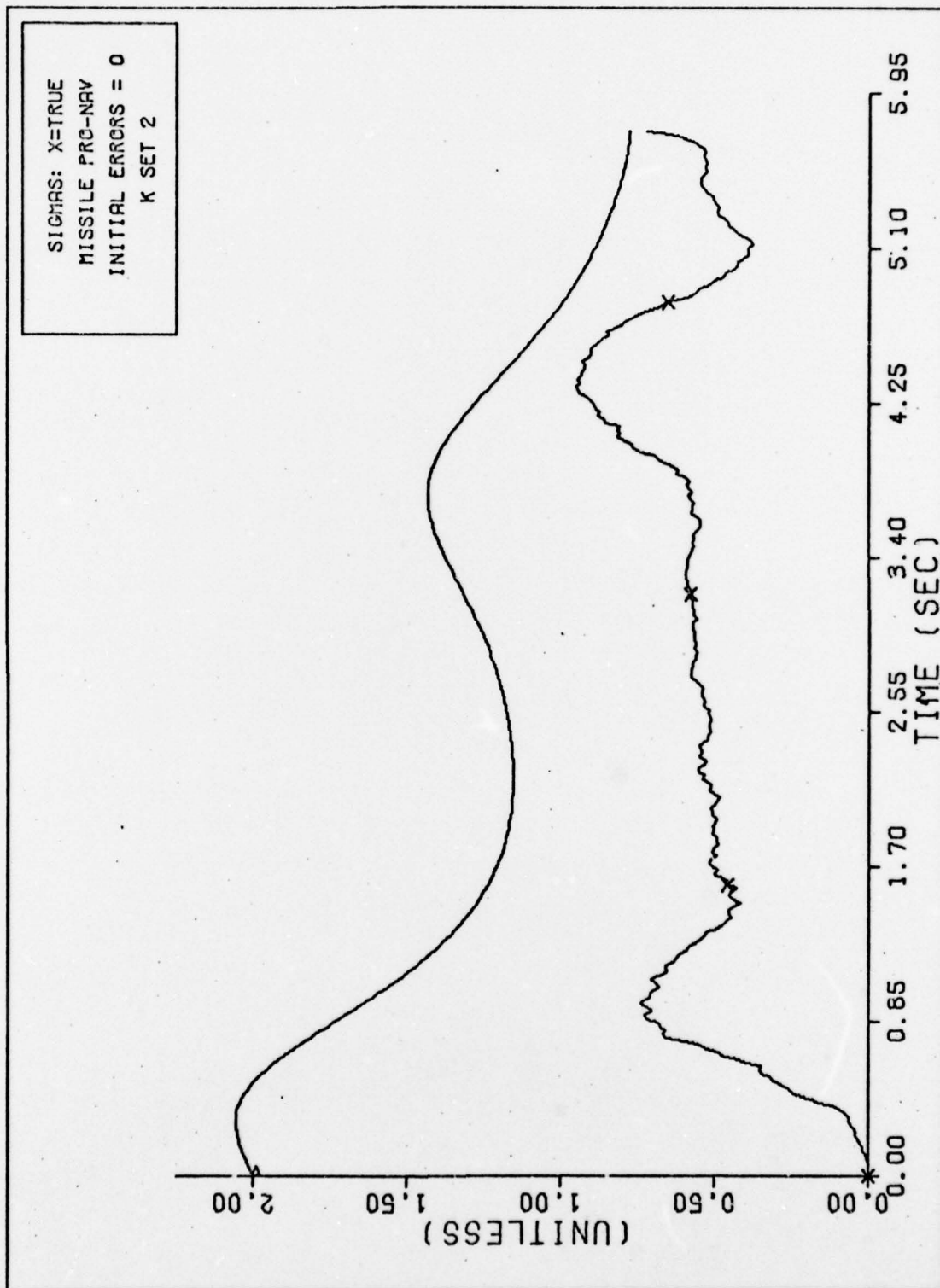


Fig. E-76

PRO-NAV FILTER & TRUE SIGMAS, 11 STATE FILTER

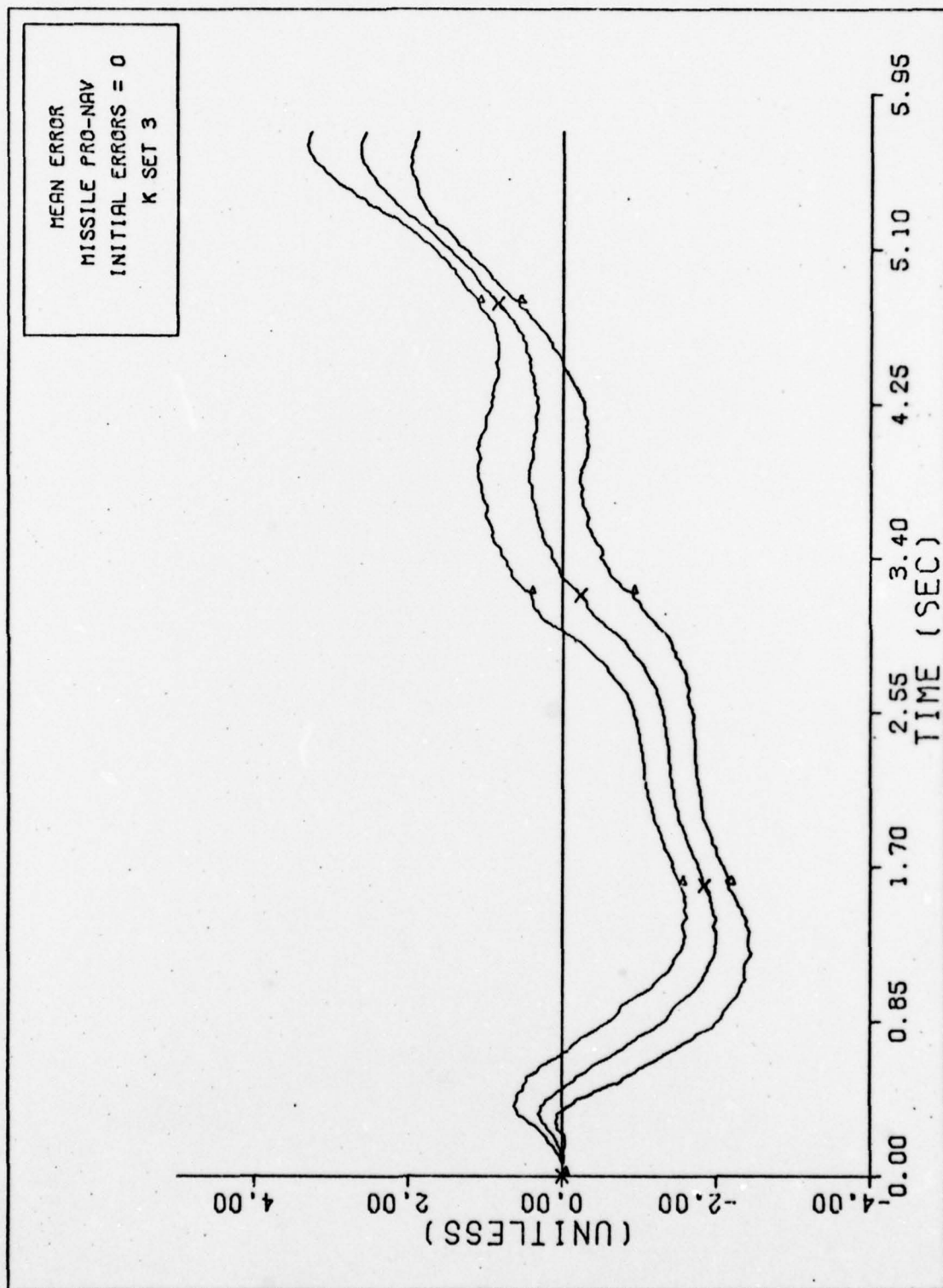


Fig. E-77

MISSILE PRO-NAV MEAN ERROR, L1 STATE FILTER

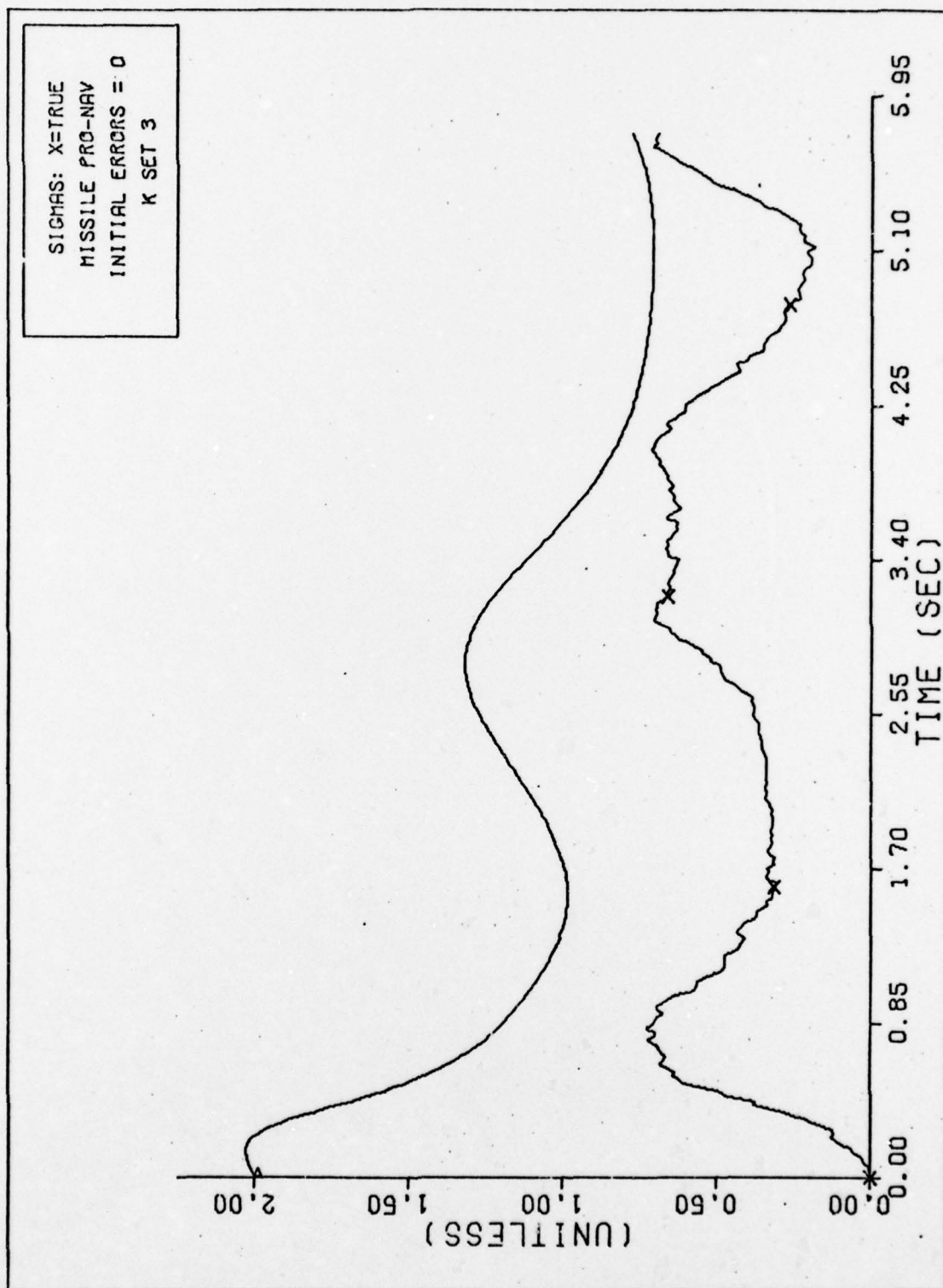


Fig. E-78 PRO-NAV FILTER & TRUE SIGMAS, 11 STATE FILTER

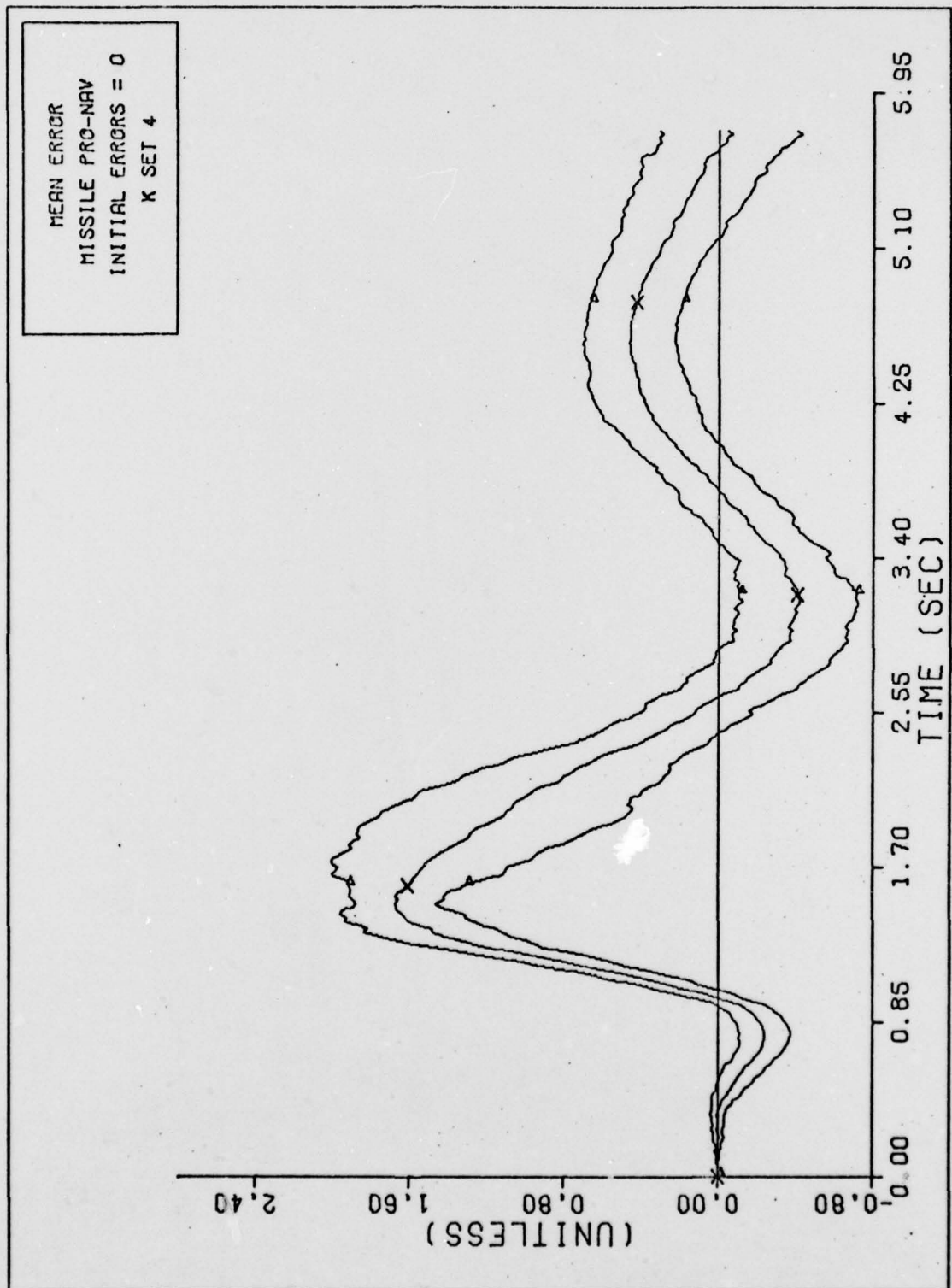


Fig. E-79

MISSILE PRO-NAV MEAN ERROR, 11 STATE FILTER

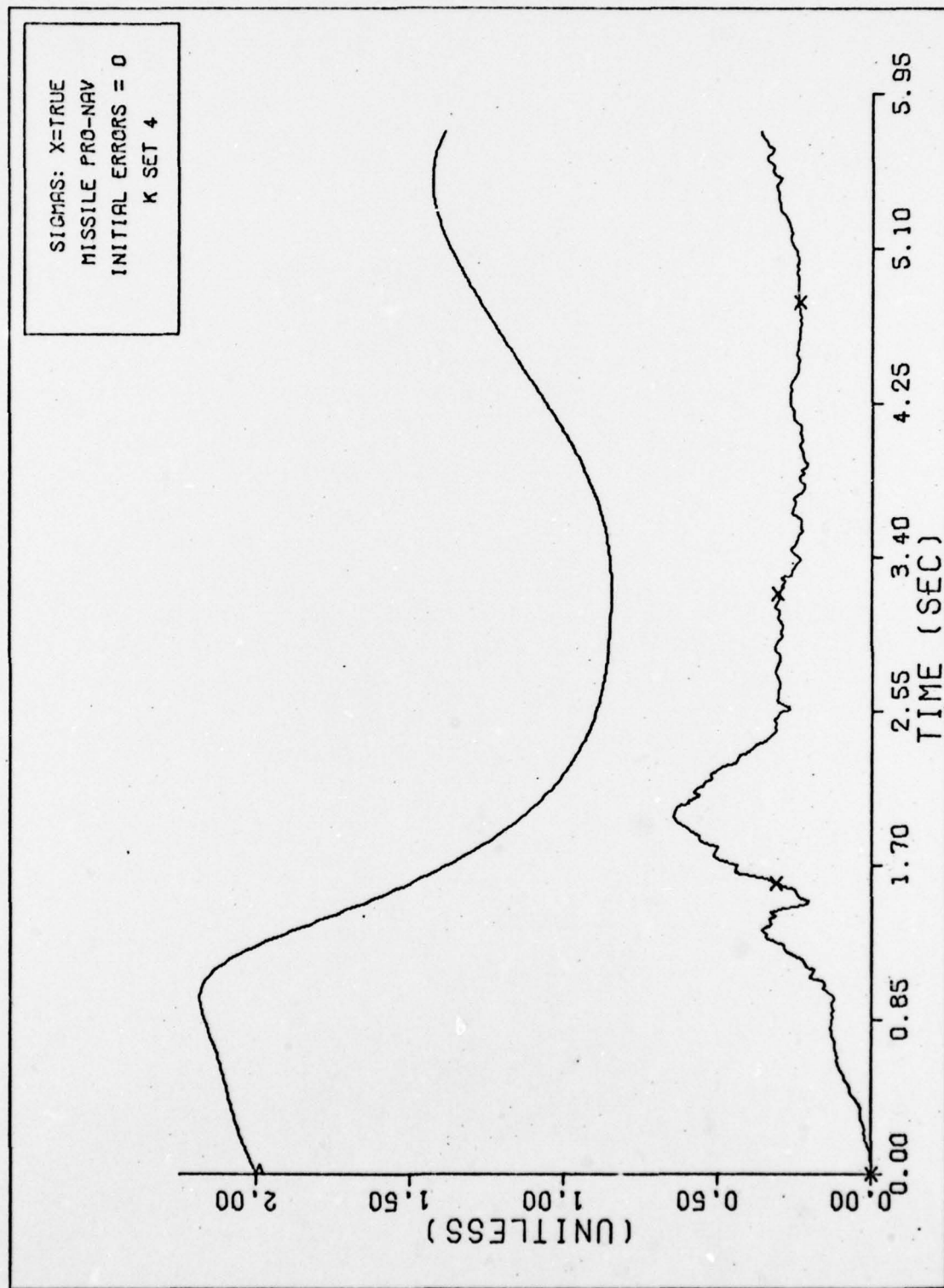


Fig. E-80 PRO-NAV FILTER & TRUE SIGMAS, 11 STATE FILTER

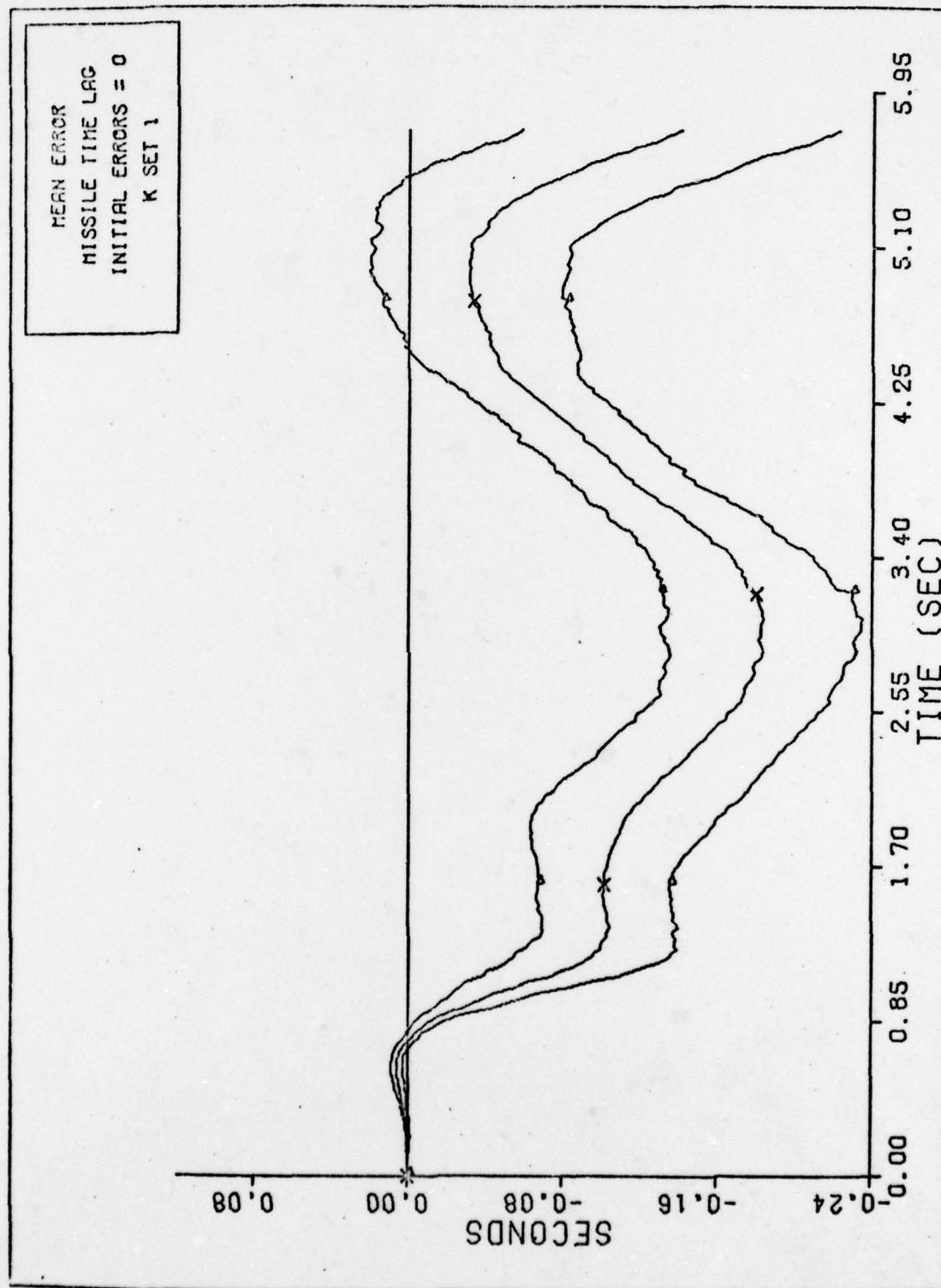


Fig. E-81 MISSILE TIME LAG MEAN ERROR, 11 STATE FILTER

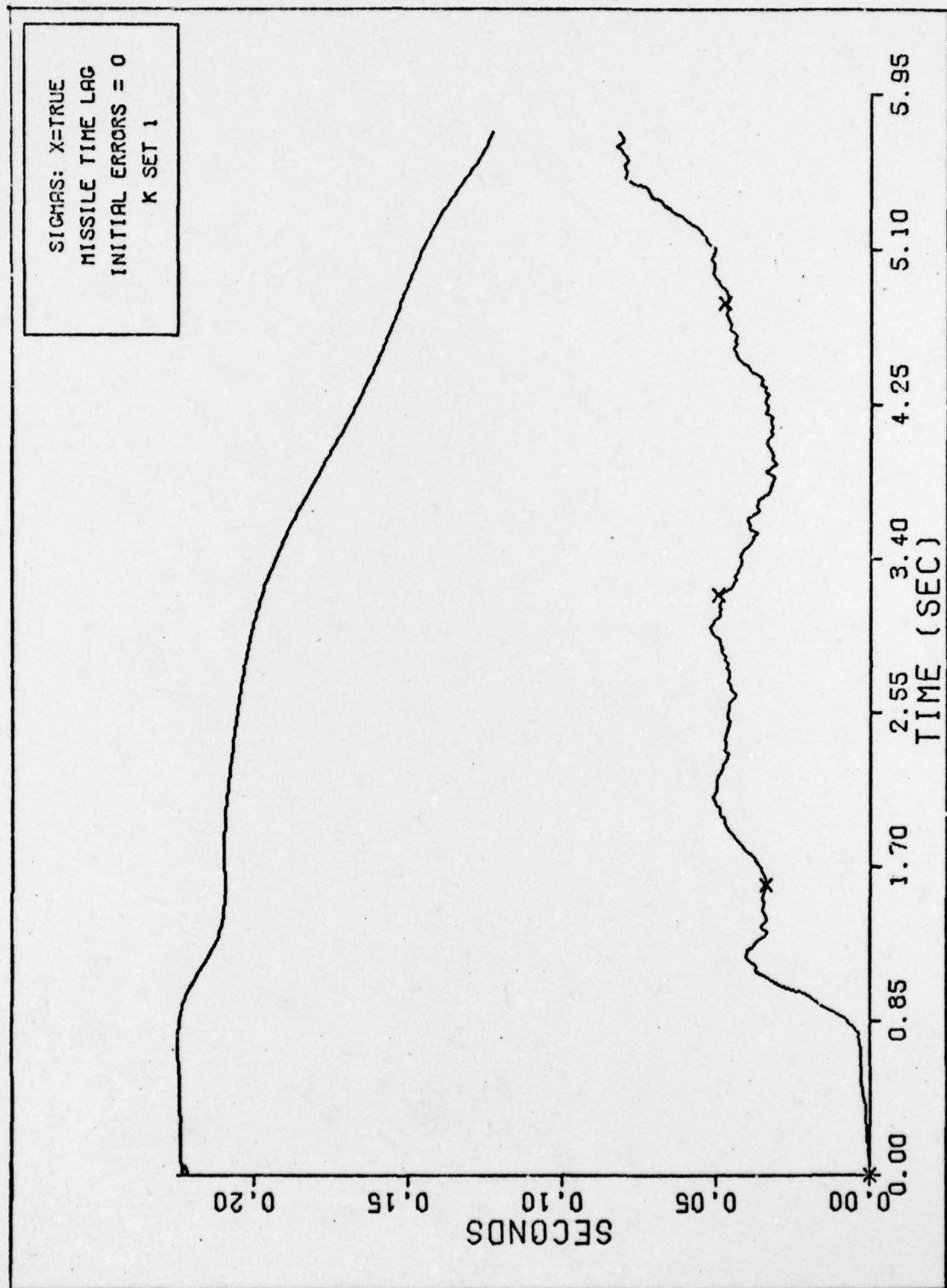


Fig. E-82 TIME LAG FILTER & TRUE SIGMAS, 11 STATE FILTER

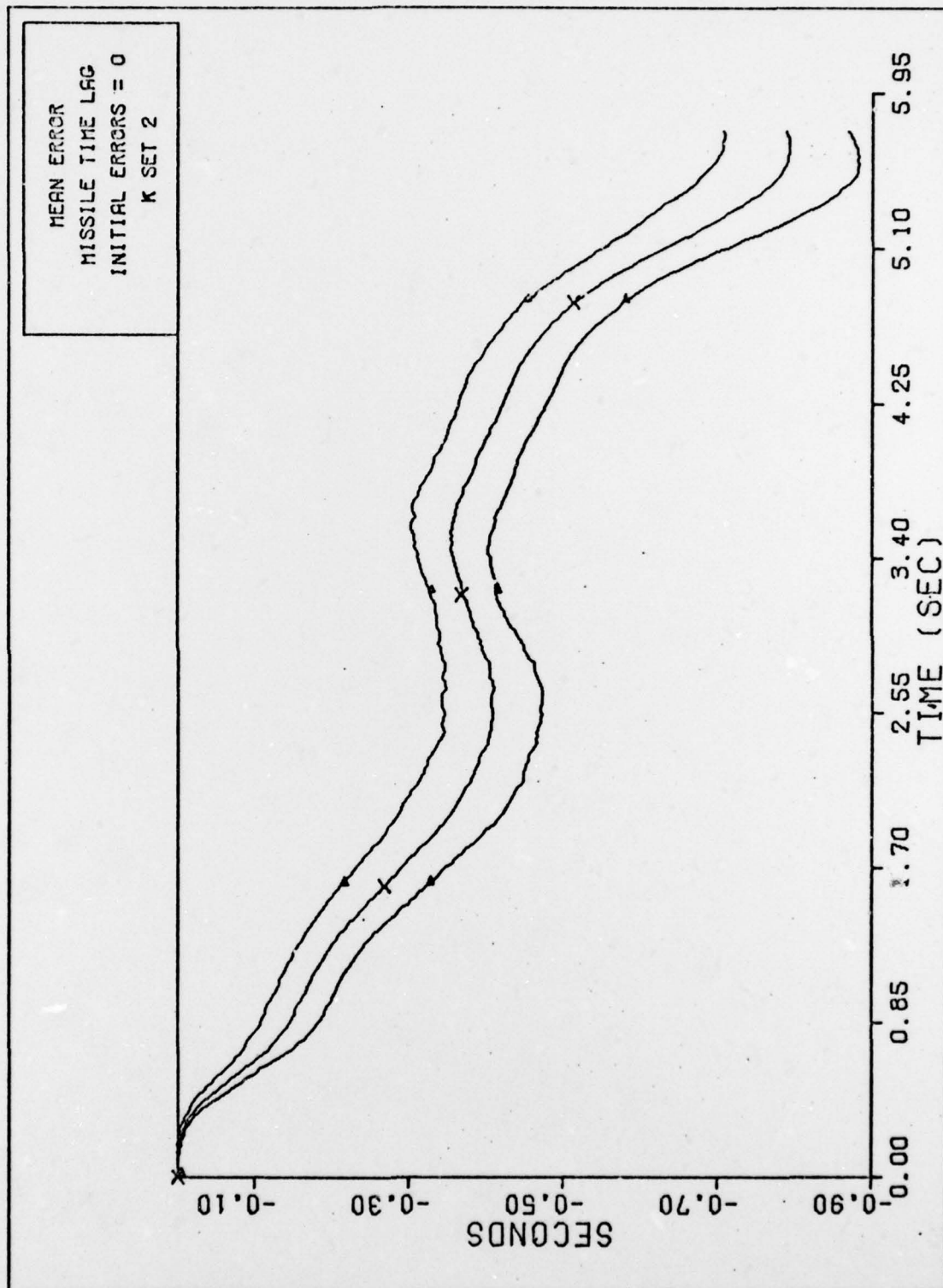


Fig. E-83 MISSILE TIME LAG MEAN ERROR, 11 STATE FILTER

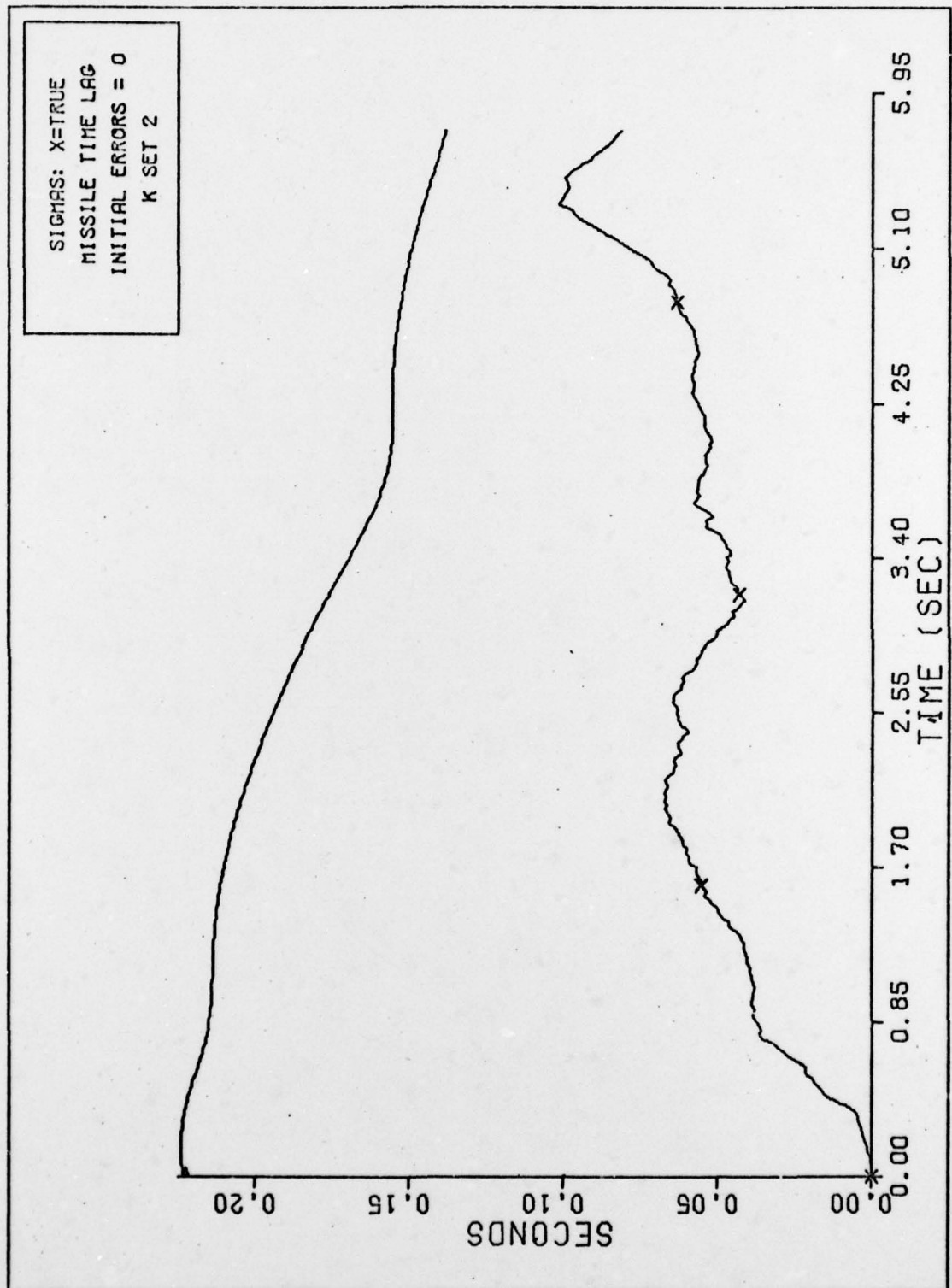


Fig. E-84 TIME LAG FILTER & TRUE SIGMAS, 11 STATE FILTER

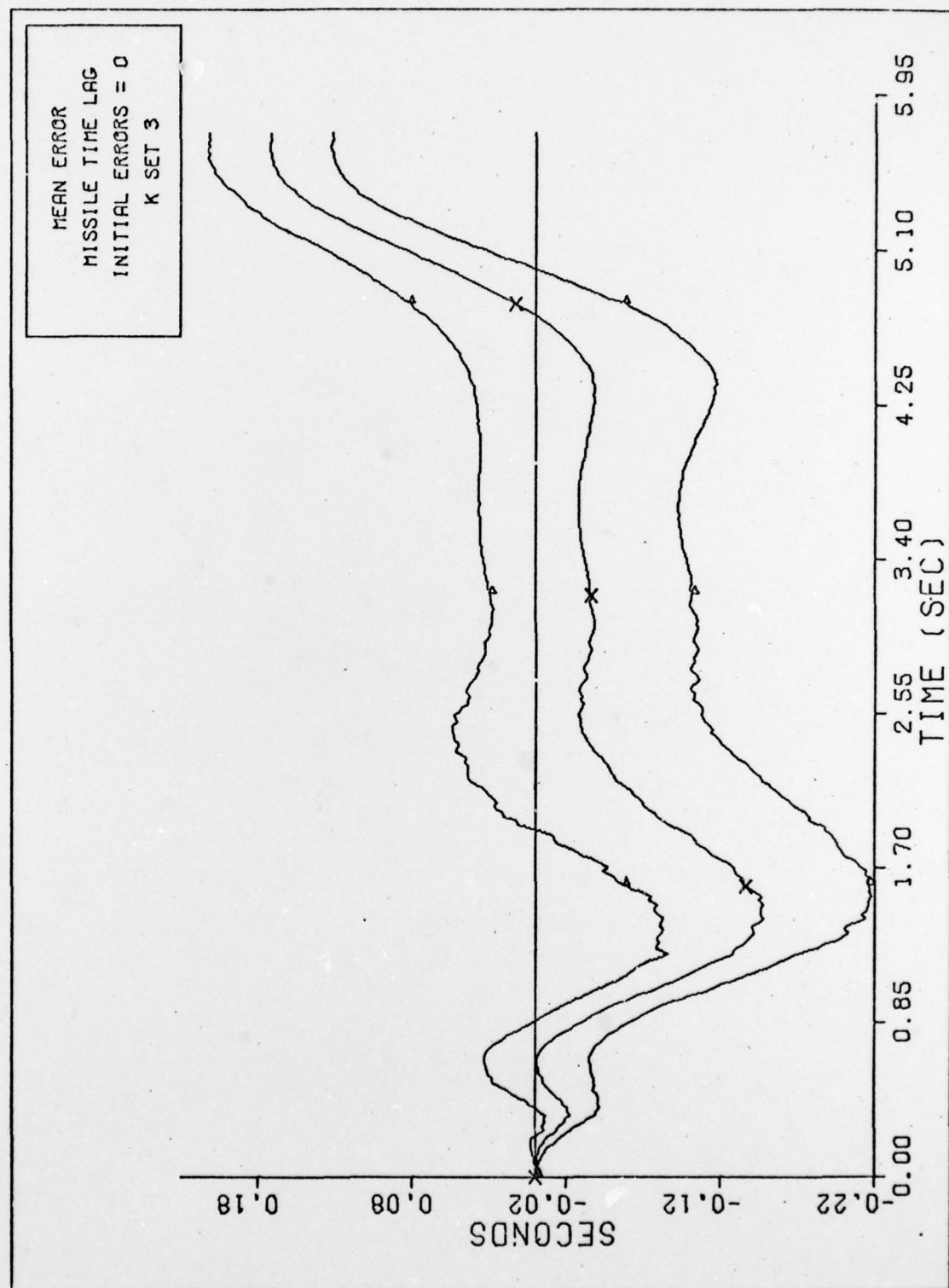


Fig. E-85 MISSILE TIME LAG MEAN ERROR, I1 STATE FILTER

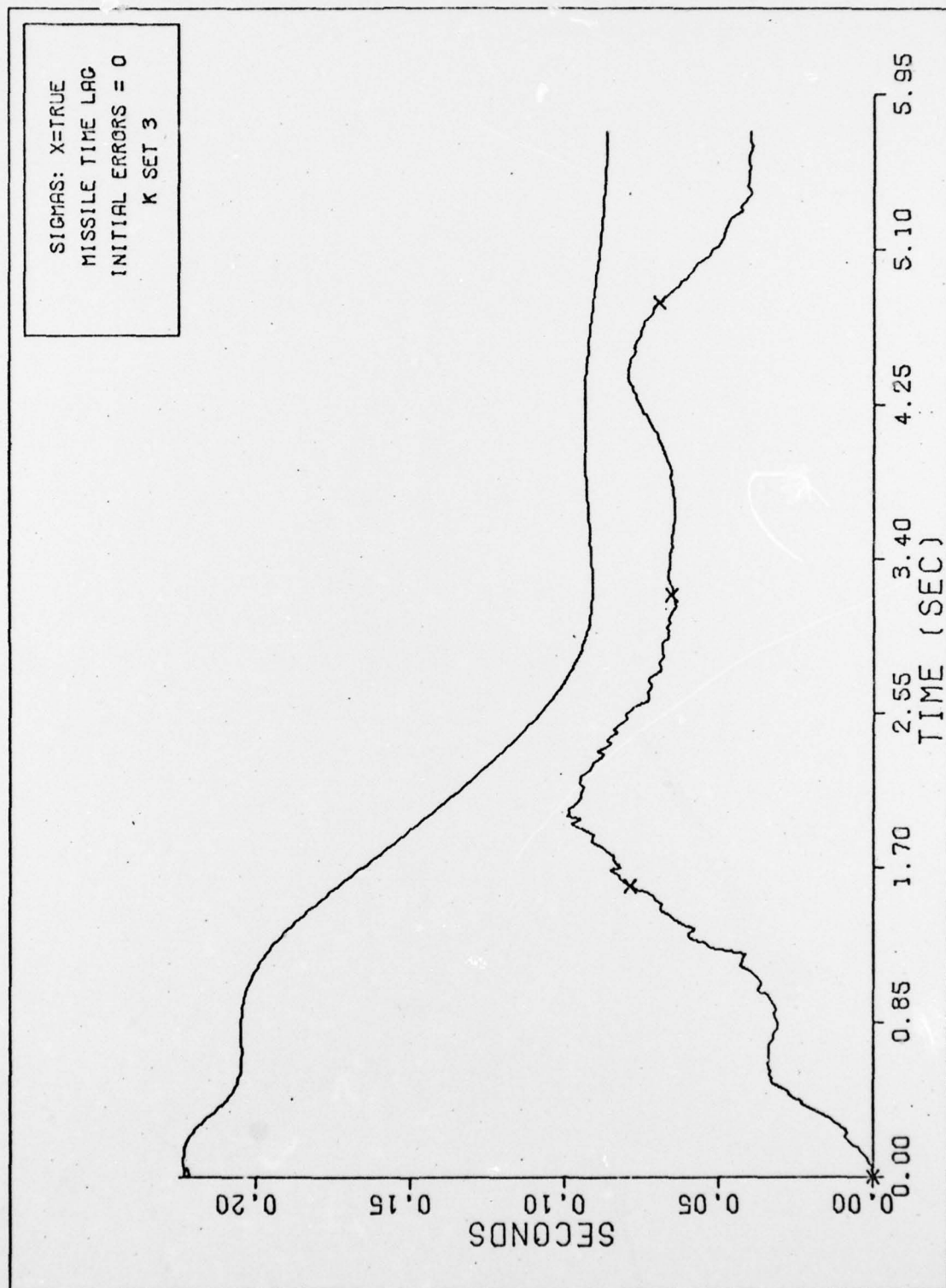


Fig. E-86 TIME LAG FILTER & TRUE SIGMAS, LI STATE FILTER

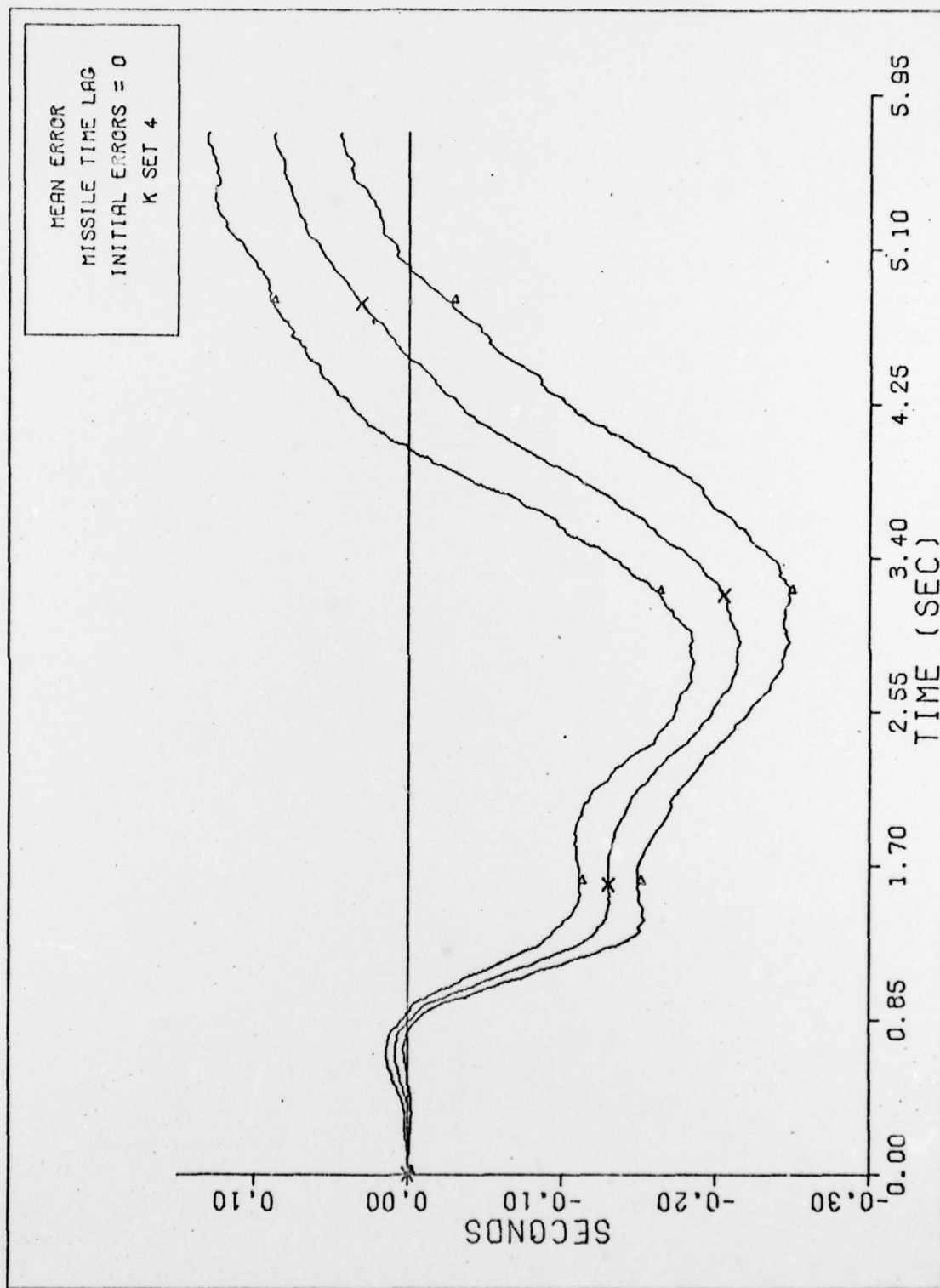


Fig. E-87 MISSILE TIME LAG MEAN ERROR, 11 STATE FILTER

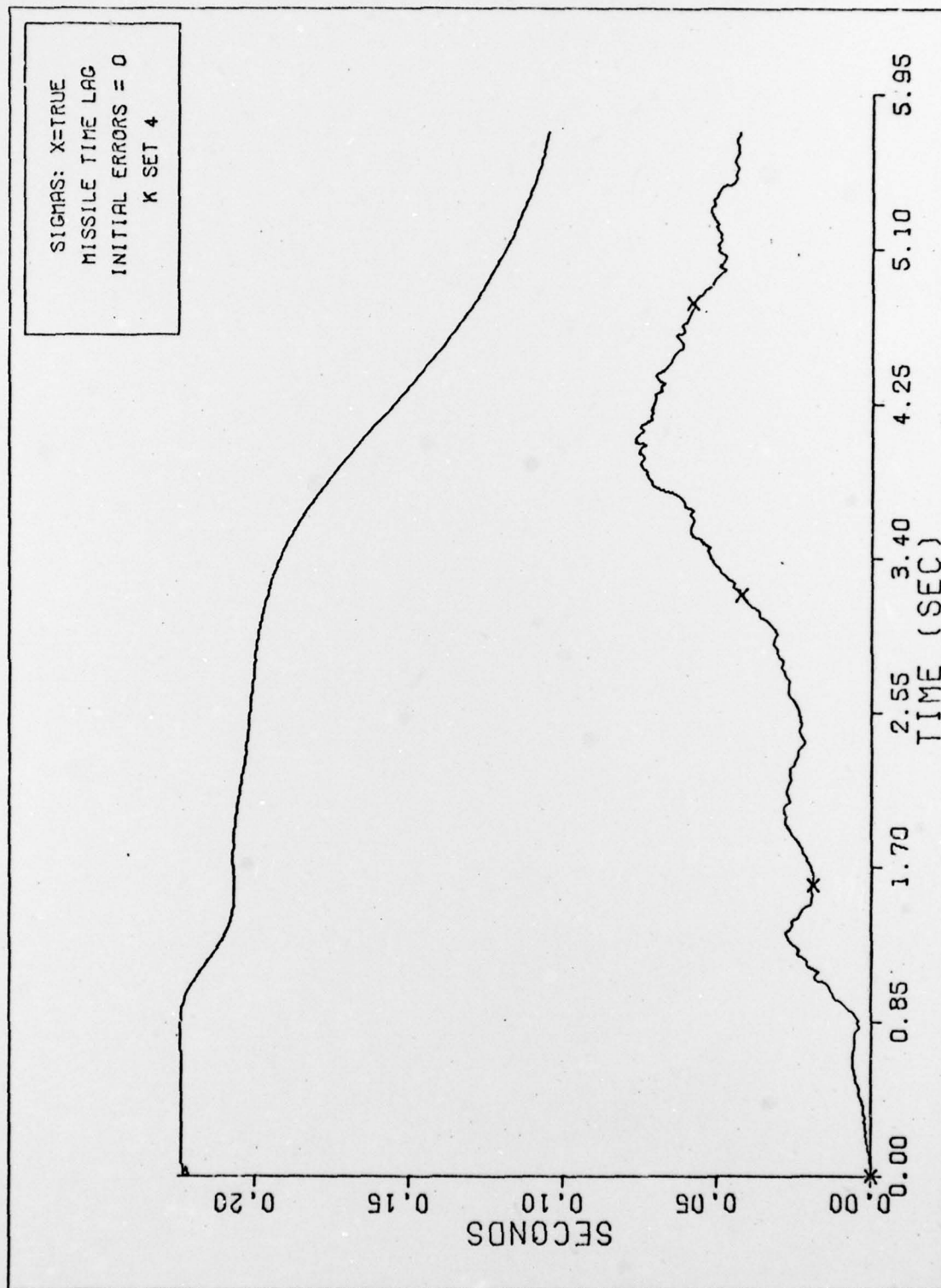


Fig. E-88 TIME LAG FILTER & TRUE SIGMAS, 11 STATE FILTER

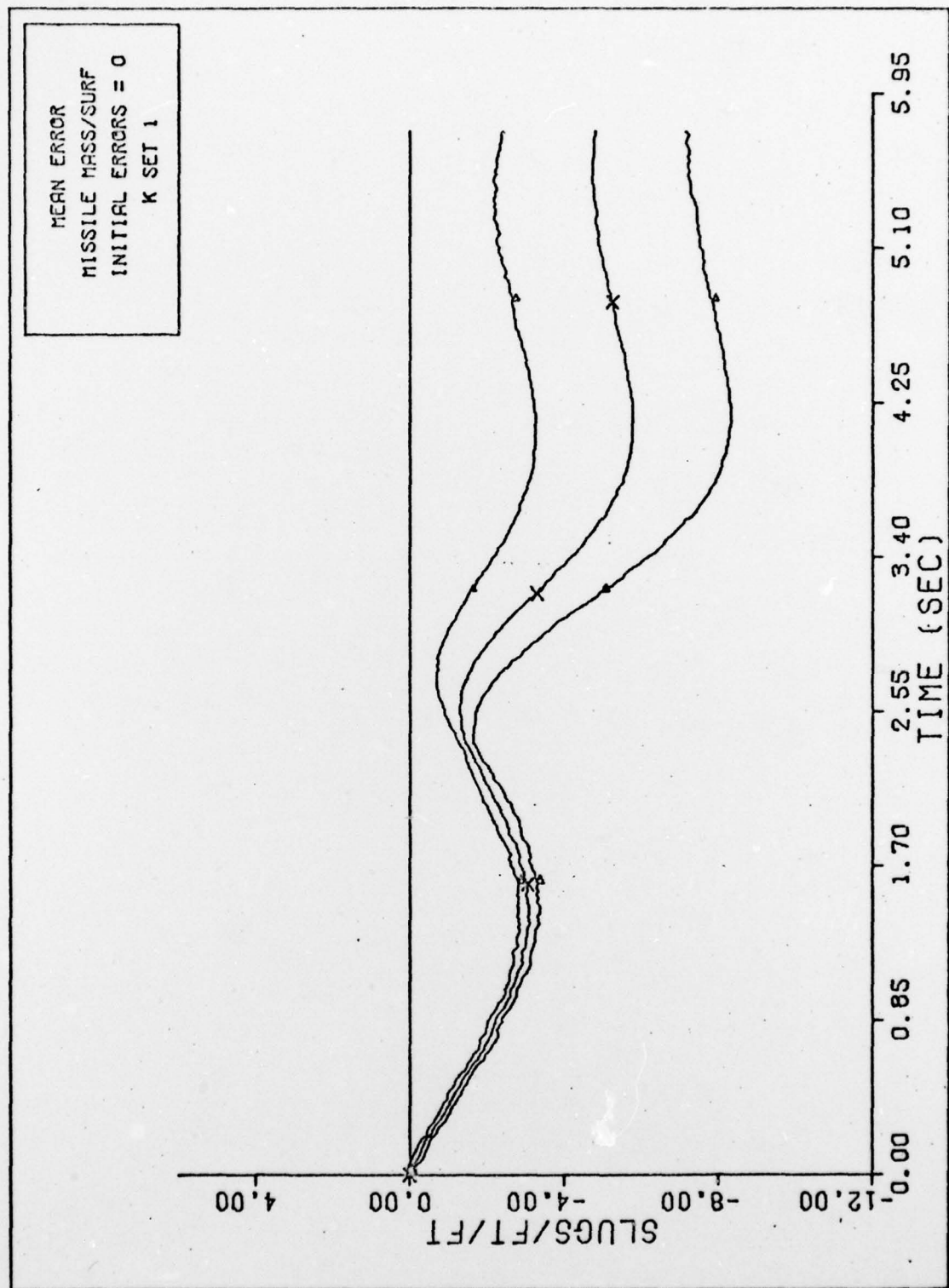


Fig. E-89 MISSILE MASS/SURF MEAN ERROR, 11 STATE FILTER

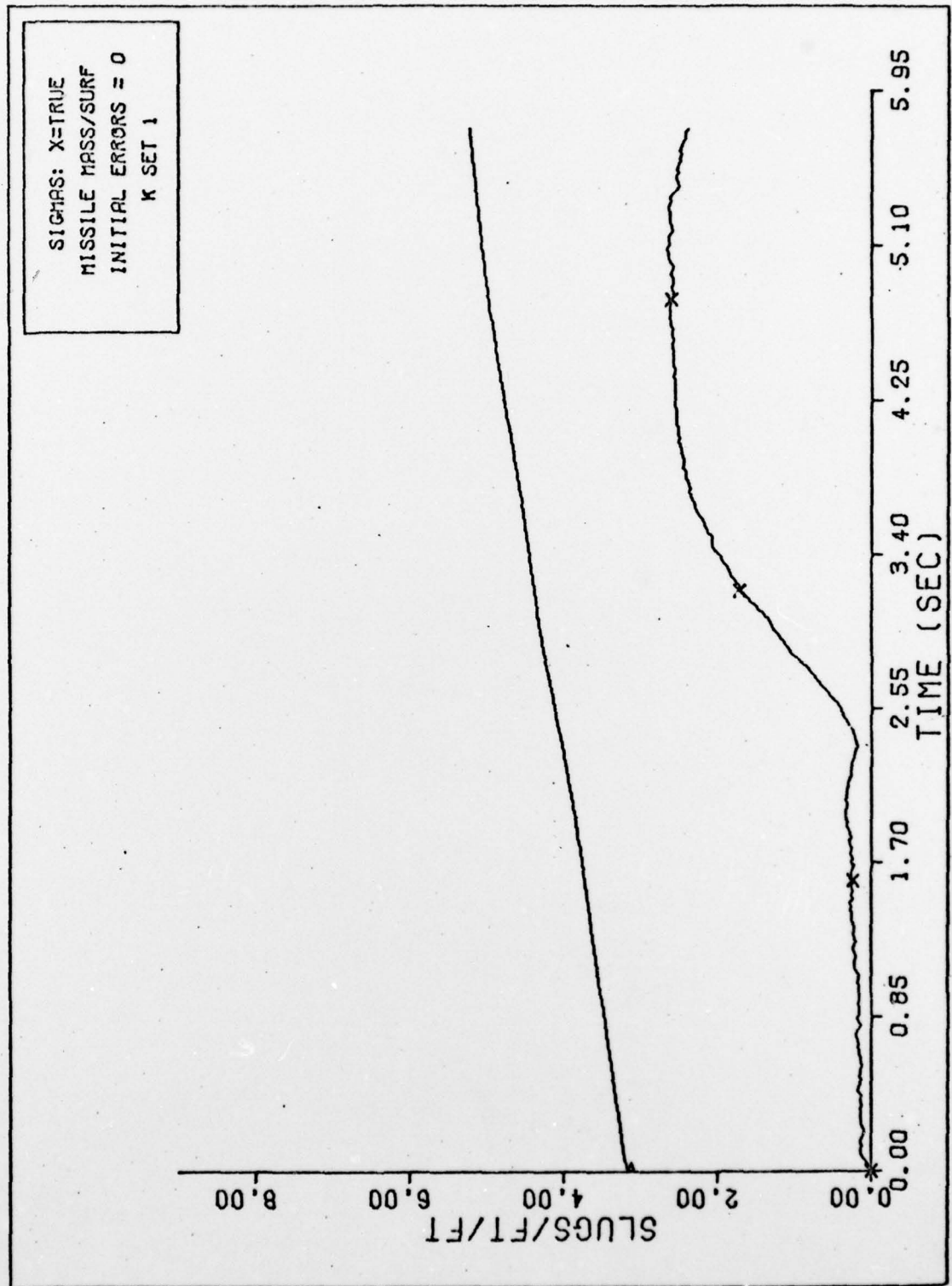


Fig. E-90 MASS/SURF FILTER & TRUE SIGMAS, 11 STATE FILTER

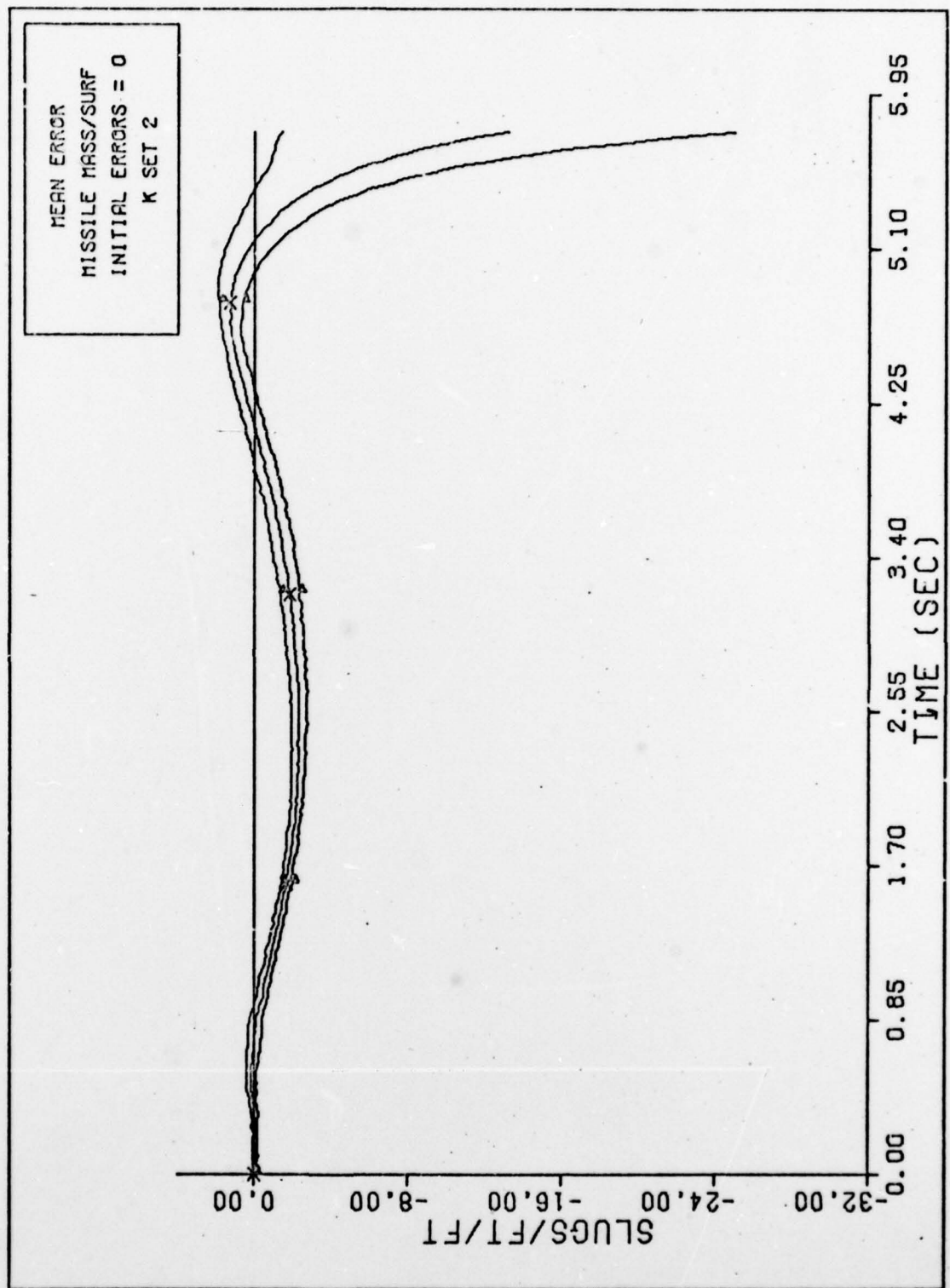


Fig. E-91 MISSILE MASS/SURF MEAN ERROR, 11 STATE FILTER

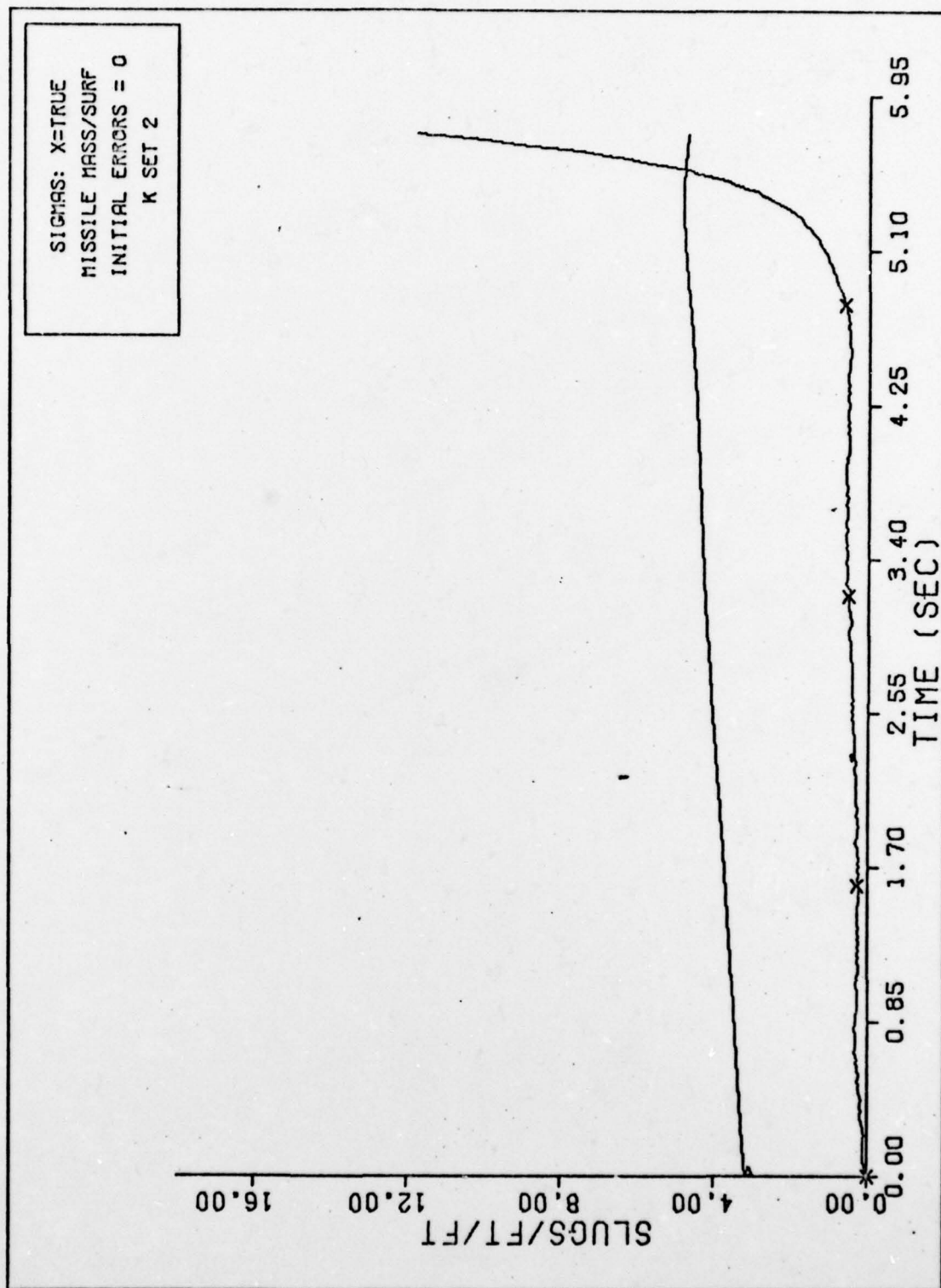


Fig. E-92 MASS/SURF FILTER & TRUE SIGMAS, L1 STATE FILTER

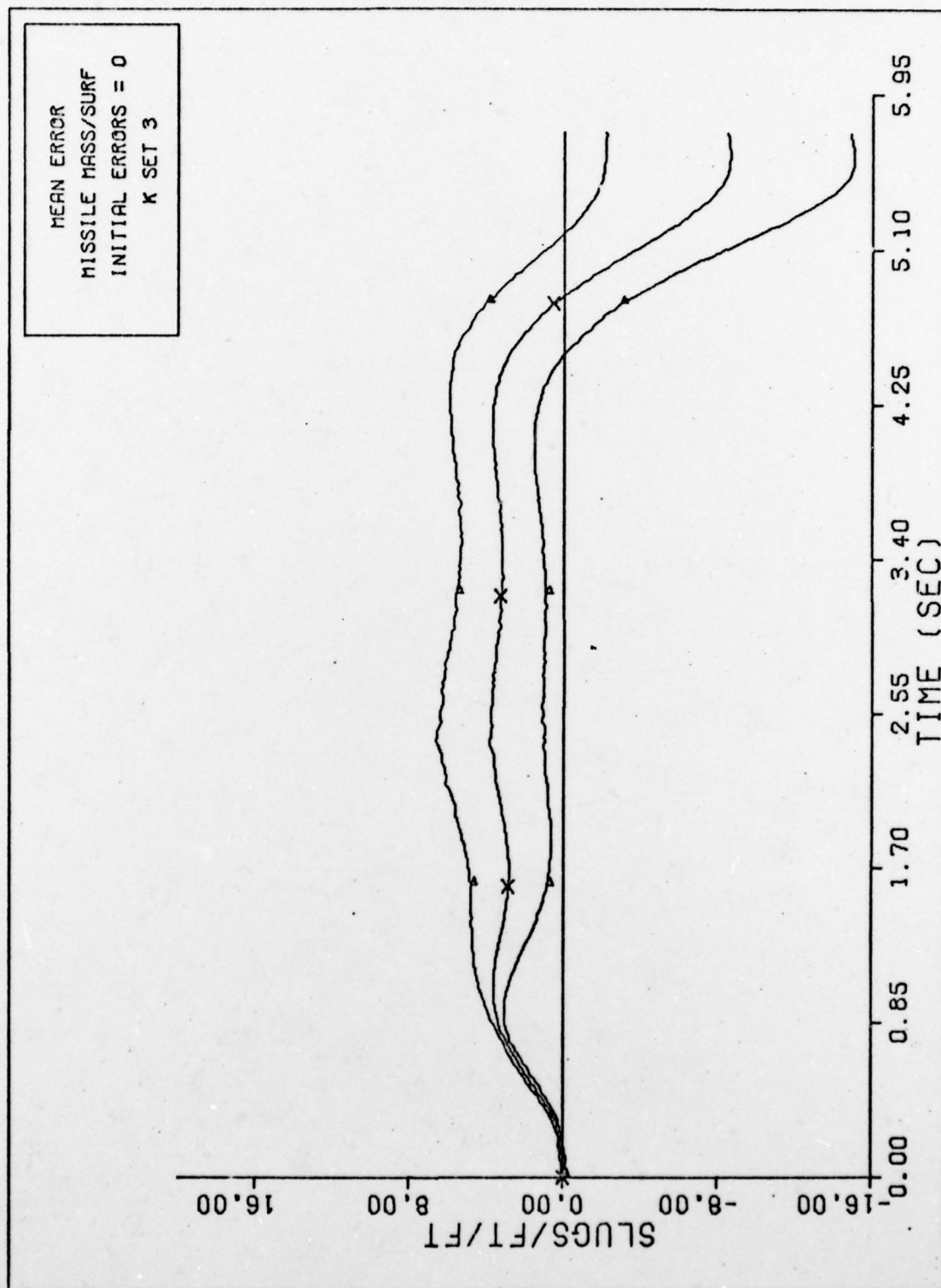


Fig. E-93 MISSILE MASS/SURF MEAN ERROR, 11 STATE FILTER

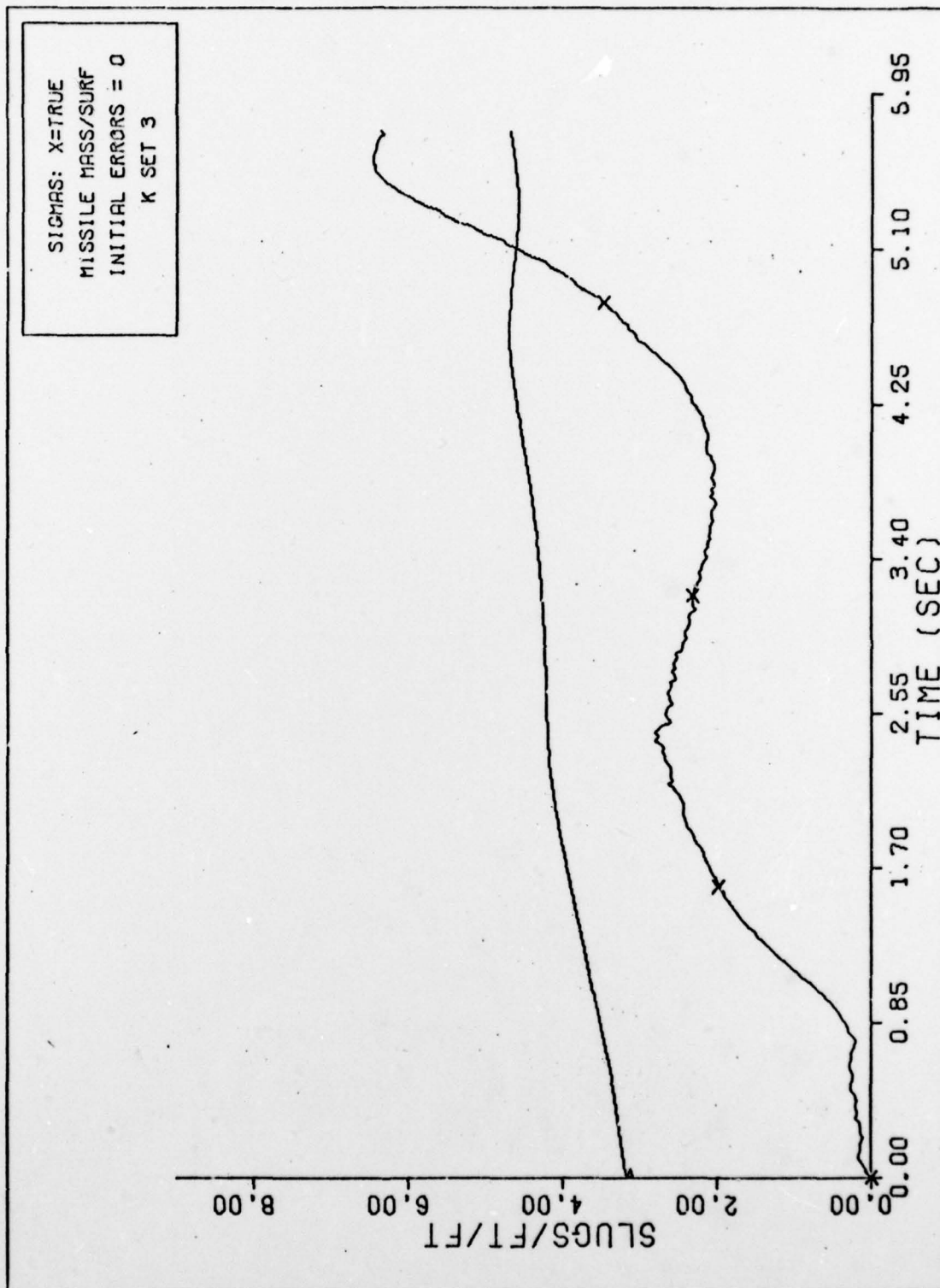


Fig. E-94 MASS/SURF FILTER & TRUE SIGMAS. 11 STATE FILTER

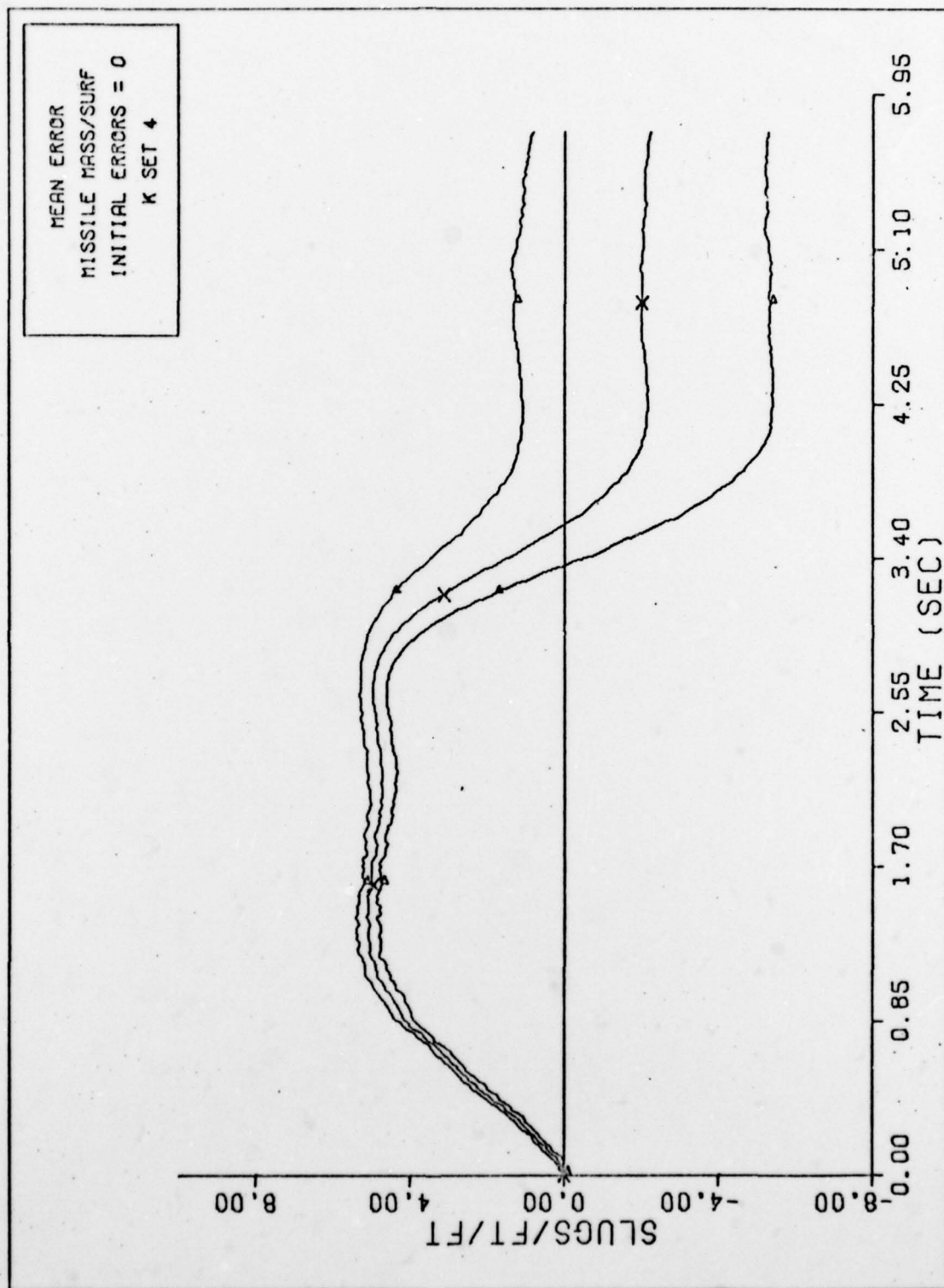


Fig. E-95 MISSILE MASS/SURF MEAN ERROR, 11 STATE FILTER

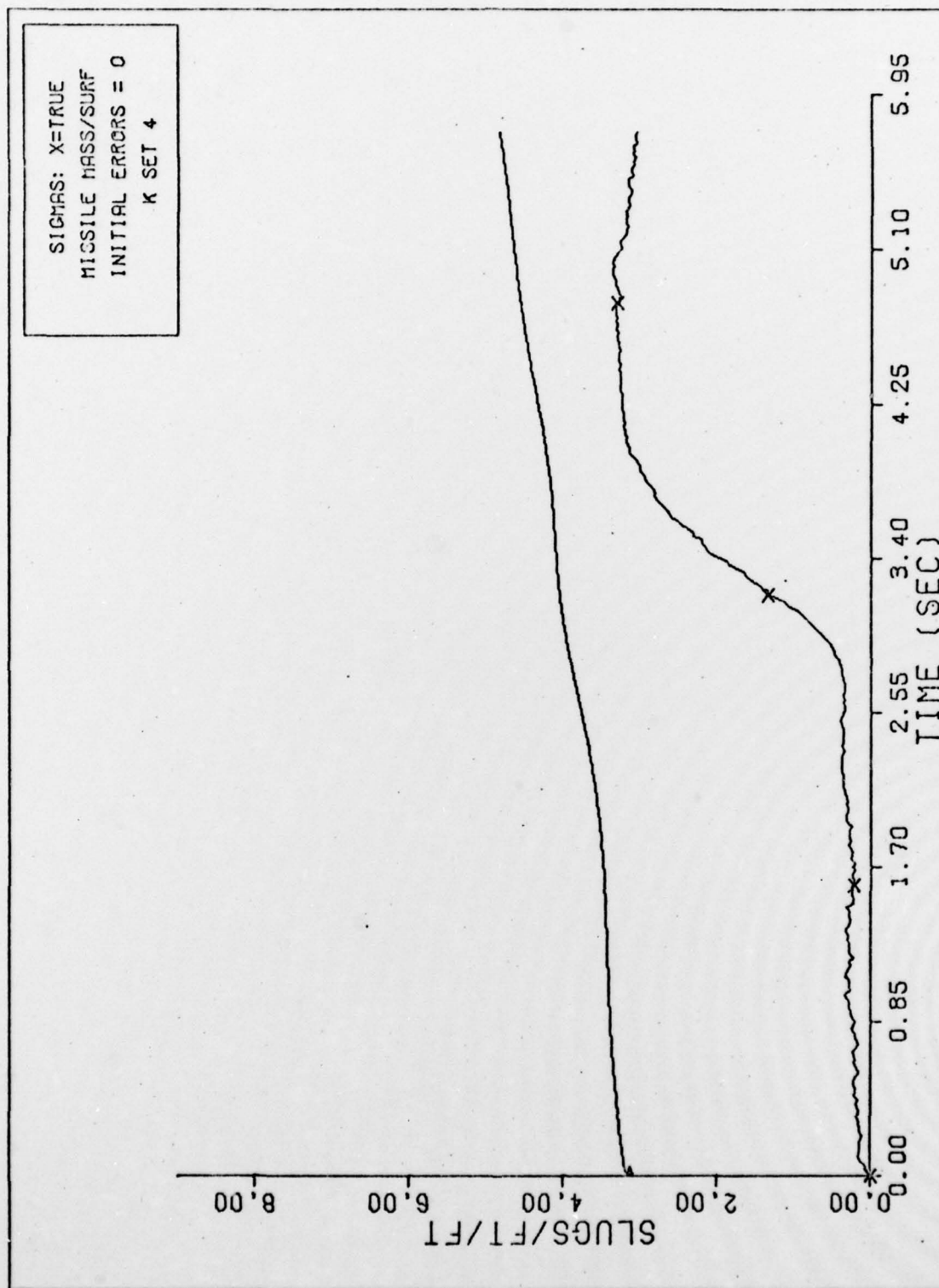


Fig. E-96 MASS/SURF FILTER & TRUE SIGMAS, 11 STATE FILTER